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Physics Opportunities at a Muon Collider

Kirk T. McDonald
Joseph Henry Laboratories, Princeton University, Princeton, NJ 08544

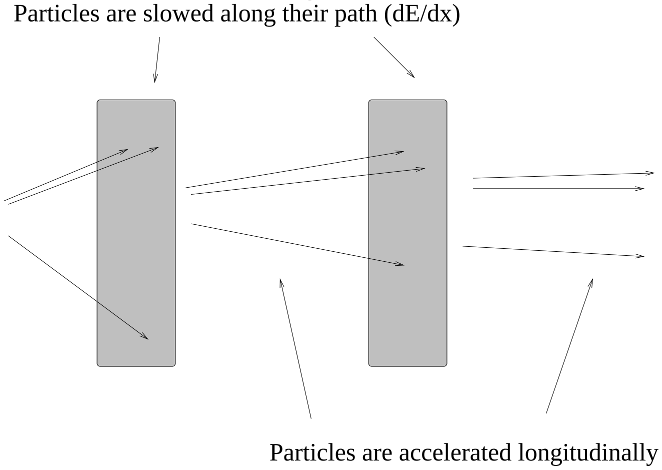
The case for a future high-energy collider based on muon beams is briefly reviewed.

1 I Want to Believe...

- That elementary particle physics will prosper for a 2nd century with laboratory experiments based on innovative particle sources.
- That a full range of new phenomena will be investigated:
  - mass ⇒ a 2nd 3×3 (or larger?) mixing matrix.
  - Precision studies of Higgs bosons.
  - A rich supersymmetric sector.
  - ... And more ...
- That our investment in future accelerators will result in more cost-effective technology, capable of extension to 10's of TeV of constituent CoM energy.
- That a **Muon Collider** [1, 2] based on ionization cooling is the best option to accomplish the above.

2 Ionization Cooling (An Idea So Simple It Might Just Work)

- Ionization: takes momentum away.
- RF acceleration: puts momentum back along z axis.
- ⇒ Transverse "cooling".



Origin: G.K. O'Neill (1956) [3]

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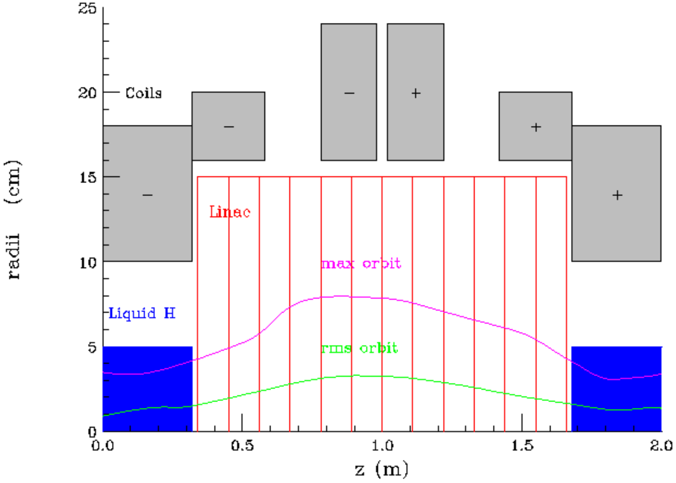
- This won't work for electrons or protons.
- So use muons: Balbekov [4], Budker [5], Skrinsky [6], late 1960's.

3 The Details are Delicate

Use channel of LH_2 absorbers, rf cavities and alternating solenoids (to avoid buildup of angular momentum).

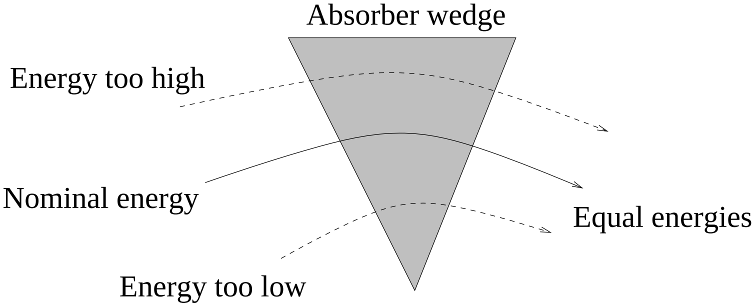
One cell of the cooling channel:



But, the energy spread rises due to "straggling".

⇒ Must exchange longitudinal and transverse emittance frequently to avoid beam loss due to bunch spreading.

Can reduce energy spread by a wedge absorber at a momentum dispersion point:



[6-D emittance constant (at best) in this process.]

4 What is a Muon Collider?

An accelerator complex in which

- Muons (both μ^+ and μ^-) are collected from pion decay following a pN interaction.
- Muon phase volume is reduced by 10^6 by ionization cooling.

- The cooled muons are accelerated and then stored in a ring.
- $\mu^+\mu^-$ collisions are observed over the useful muon life of ≈ 1000 turns at any energy.
- Intense neutrino beams and spallation neutron beams are available as byproducts.

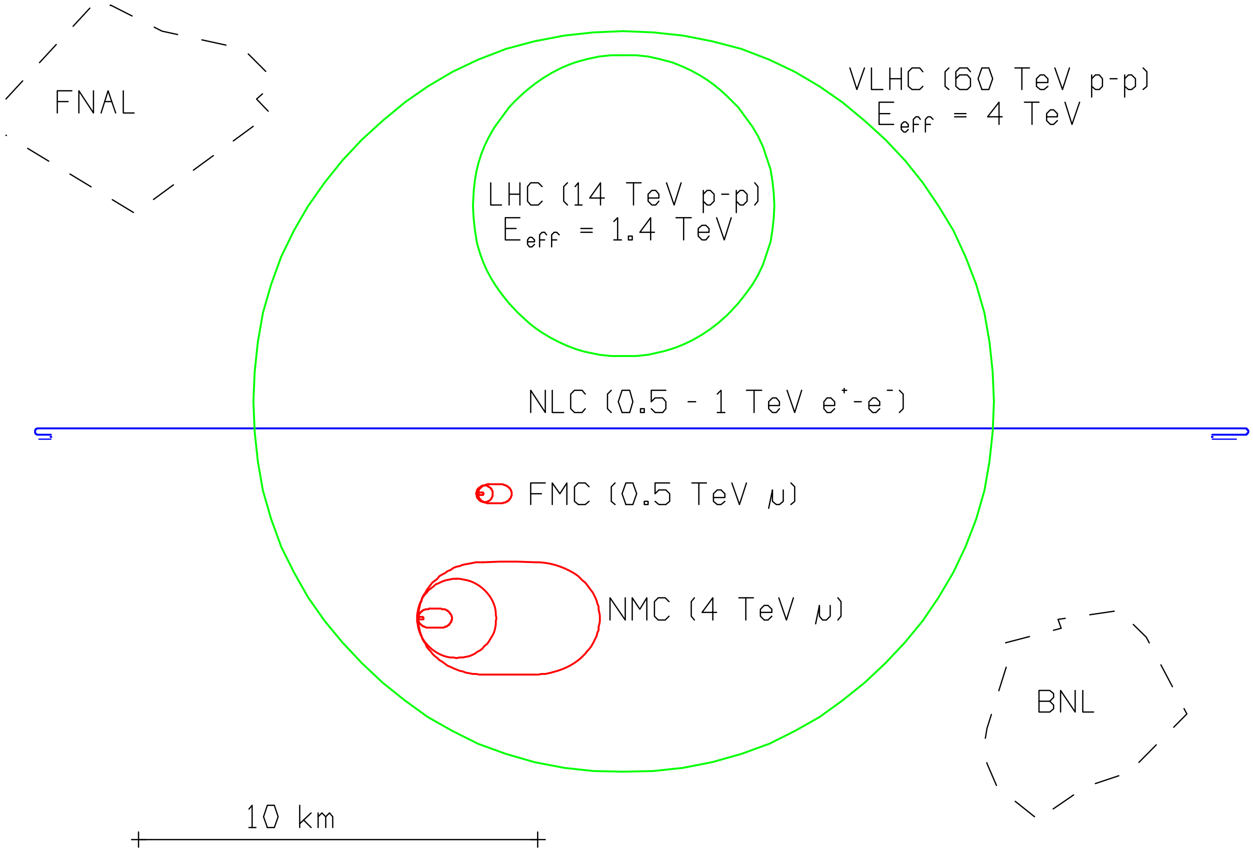
Muons decay: $\mu \rightarrow e\nu \quad \Rightarrow$

- Must cool muons quickly (stochastic cooling won't do).
- Detector backgrounds at LHC level.
- Potential personnel hazard from ν interactions.

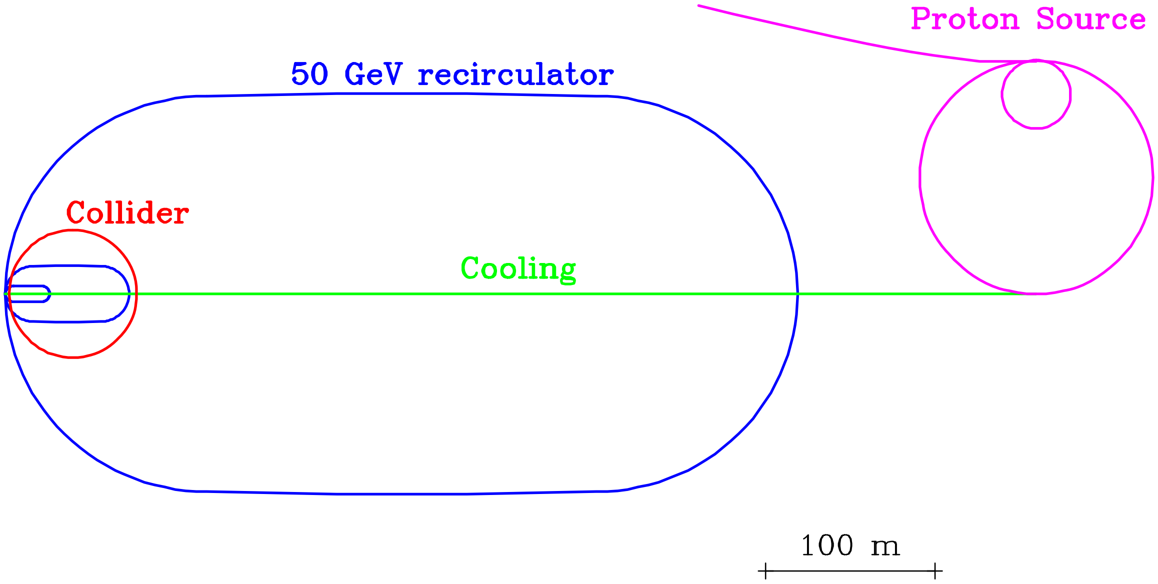
Table 1: Baseline parameters for high- and low-energy muon colliders. Higgs/year assumes a cross section $\sigma = 5 \times 10^4$ fb; a Higgs width $\Gamma = 2.7$ MeV; 1 year $= 10^7$ s.

CoM energy	TeV	3	0.4		0.1	
p energy	GeV	16	16		16	
p's/bunch		2.5×10^{13}	2.5×10^{13}		5×10^{13}	
Bunches/fill		4	4		2	
Rep. rate	Hz	15	15		15	
p power	MW	4	4		4	
μ/bunch		2×10^{12}	2×10^{12}		4×10^{12}	
μ power	MW	28	4		1	
Wall power	MW	204	120		81	
Collider circum.	m	6000	1000		350	
Ave bending field	T	5.2	4.7		3	
Depth	m	500	100		10	
Rms $\Delta P/P$	%	0.16	0.14	0.12	0.01	0.003
6d ϵ_6	$(\pi \mathrm{m})^3$	1.7×10^{-10}	1.7×10^{-10}	1.7×10^{-10}	1.7×10^{-10}	1.7×10^{-10}
Rms ϵ_n	π mm-mrad	50	50	85	195	290
β^*	cm	0.3	2.6	4.1	9.4	14.1
σ_z	cm	0.3	2.6	4.1	9.4	14.1
σ_r spot	μm	3.2	26	86	196	294
σ_θ IP	mrad	1.1	1.0	2.1	2.1	2.1
Tune shift		0.044	0.044	0.051	0.022	0.015
n_{turns} (effective)		785	700	450	450	450
Luminosity	$\mathrm{cm}^{-2}\mathrm{s}^{-1}$	7×10^{34}	10^{33}	1.2×10^{32}	2.2×10^{31}	10^{31}
Higgs/year				1.9×10^3	4×10^3	3.9×10^3

Comparison of footprints of various future colliders:



A First Muon Collider to study light-Higgs production:



5 The Case for a Muon Collider

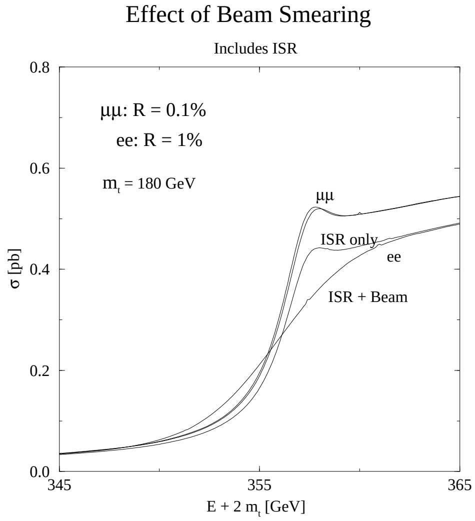
- More affordable than an e^+e^- collider at the TeV (LHC) scale.

- More affordable than either a hadron or an e^+e^- collider for (effective) energies beyond the LHC.

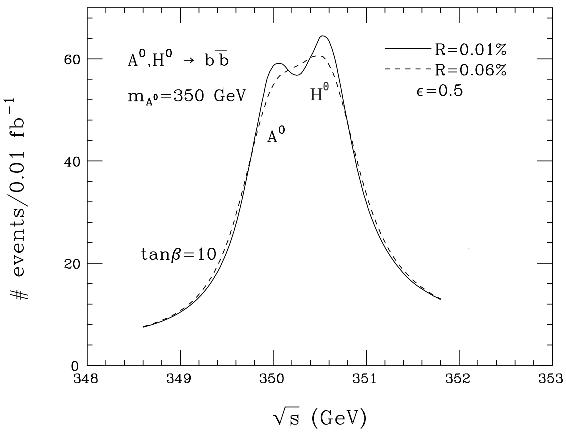
- Precision initial state superior even to e^+e^- .

  Muon polarization $\approx 25\%$, $\Rightarrow$ can determine E_{beam} to 10^{-5} via $g-2$ spin precession [7].

  $t\bar{t}$ threshold:

  Nearly degenerate A^0 and H^0:

- Initial machine could produce light Higgs via s-channel [8]:

  Higgs coupling to μ is $(m_\mu/m_e)^2 \approx 40,000\times$ that to e.

  Beam energy resolution at a muon collider $< 10^{-5}$,

  $\Rightarrow$ Measure Higgs width.

  Add rings to 3 TeV later.

- Neutrino beams from μ decay about 10^4 hotter than present.

  Possible initial scenario in a low-energy muon storage ring [9].

$$\text{Study } CP \text{ violation via } CP \text{ conjugate initial states:} \begin{cases} \mu^+ \to e^+\overline{\nu}_\mu\nu_e \\ \mu^- \to e^-\nu_\mu\overline{\nu}_e \end{cases}.$$

6 Future Frontier Facilities

(A Personal Assessment)

- Hadron collider (LHC, SSC): $\approx$ \$100k/m [magnets].

  $\approx$ 2 km per TeV of CM energy.

  Ex: LHC has 14-TeV CM energy, 27 km ring, $\approx$ \$3B.

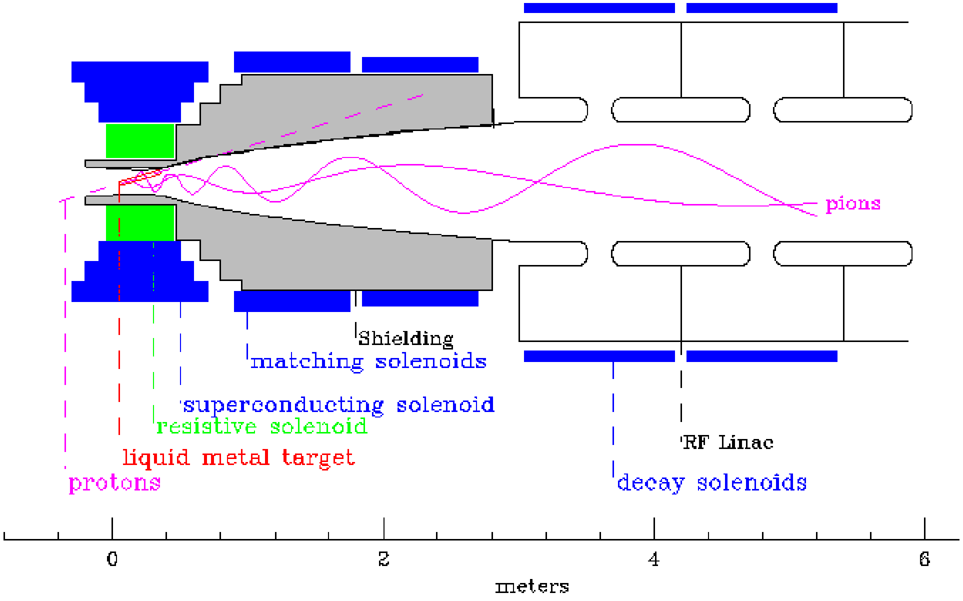
- Linear e^+e^- collider (SLAC, NLC(?)): $\approx$ \$200k/m [rf].
  $\approx$ 20 km per TeV of CM energy;
  But a lepton collider needs only $\approx$ 1/10 the CM energy
  to have equivalent physics reach to a hadron collider.
  Ex: NLC, 1.5-TeV CM energy, 30 km long, $\approx$ \$6B (?).

- Muon collider: $\approx$ \$1B for source/cooler + \$100k/m for rings
  Well-defined leptonic initial state.
  $m_\mu/m_e \approx 200 \Rightarrow$ Little beam radiation.
  $\Rightarrow$ Can use storage rings.
  $\Rightarrow$ Smaller footprint.
  Technology: closer to hadron colliders.
  $\approx$ 6 km of ring per TeV of CM energy.
  Ex: 3-TeV muon collider, $\approx$ \$3B (?), would have physics reach well beyond the LHC.

7 Muon Collider R&D Program

- Targetry and Capture at a Muon Collider Source [10, 11].

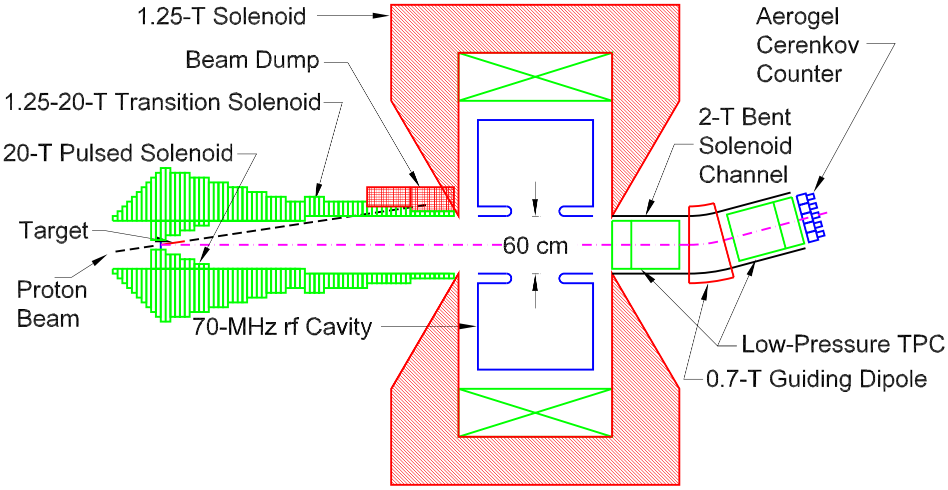
  Baseline scenario:



To achieve useful physics luminosity, a muon collider must produce about 10^{14} μ/sec.

- $\Rightarrow >$ 10^{15} proton/sec onto a high-Z target $\Leftrightarrow$ 4 MW beam power.
- Capture pions of $P_\perp \lesssim 200$ MeV/c in a 20-T solenoid magnet.
- Transfer the pions into a 1.25-T-solenoid decay channel.
- Compress π/μ bunch energy with rf cavities and deliver to muon cooling channel.

Proposed R&D facility:



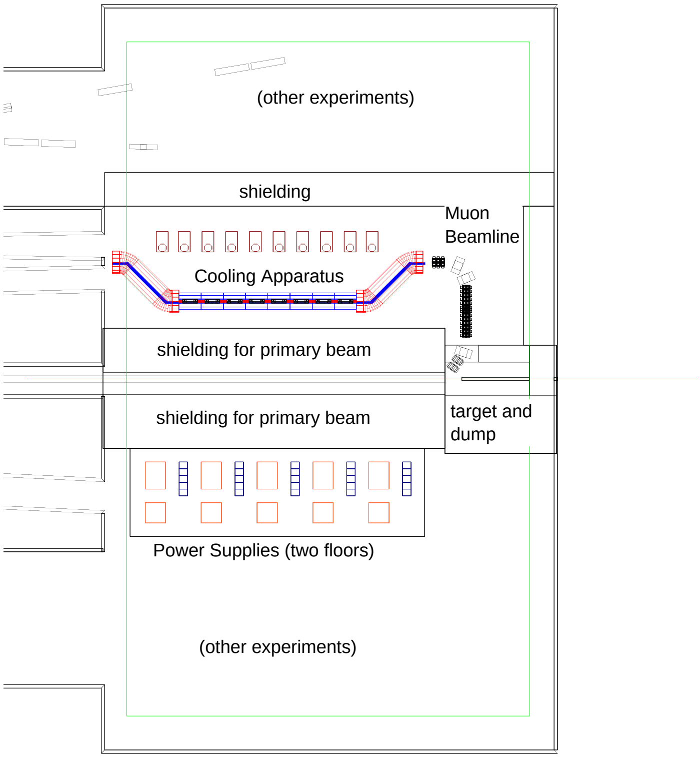
- Ionization Cooling for a High Luminosity Muon Collider [12, 13].

  Test basic cooling components:

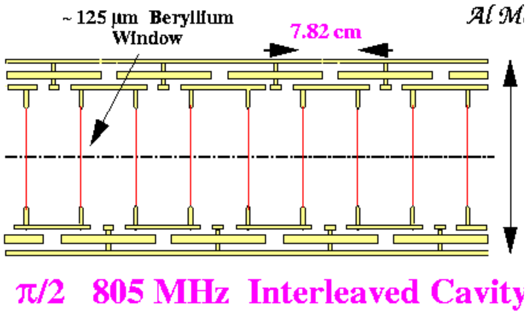
  - Alternating solenoid lattice, RF cavities, LH_2 absorber.
  - Lithium lens (for final cooling).
  - Dispersion + wedge absorbers to exchange longitudinal and transverse phase space.

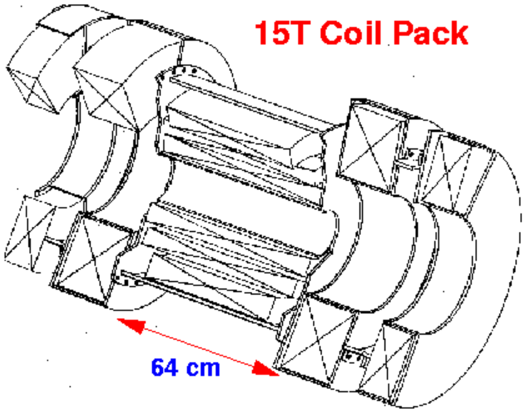
  Track individual muons; simulate a bunch in software.

  Possible site: Meson Lab at Fermilab:



Cooling channel components:





8 Upcoming Workshops

(See http://www.cap.bnl.gov/mumu/table_workshop.html)

- Muon Collider Collaboration Meeting, May 20-26, 1999, St. Croix.
- Neutrino Factories Based on Muon Accumulators, July 5-9, 1999, Lyon/CERN.
- Muon Colliders at the Highest Energies, Sept. 27-Oct. 1, 1999, Montauk, NY.
- Physics Potential and Development of $\mu^+\mu^-$ Colliders, Dec. 14-19, 1999, San Francisco.

9 References

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