

# ALTERNATIVE CAPTURE SOLENOID AND TRANSPORT STUDY FOR THE MUON COLLIDER/NEUTRINO FACTORY TARGET

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# BASELINE OPTIMIZED PARAMETERS (X. DING)

## ➤ Hg Target

- $\theta_{\text{Target}}=0.137$  rad
- $R_{\text{Target}}=0.404$  cm

## ➤ Proton Beam

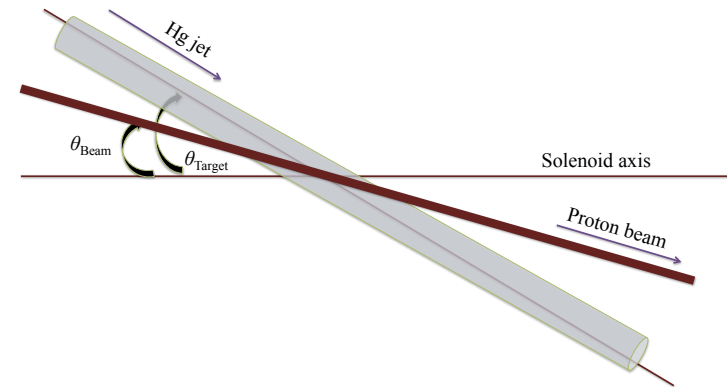
- $E=8$  GeV
- $\theta_{\text{Beam}}=0.117$  rad
- $\sigma_x=\sigma_y=0.1212$  cm (Gaussian Distribution)
- $\sigma_t=\sigma_z=0$  (Pancake Distribution)

## ➤ Solenoid Field

- IDS120h  $\rightarrow$  20 T peak field at target position ( $Z=-37.5$ )
- Aperture at Target  $R=7.5$  cm - End aperture  $R = 30$  cm
- Fixed Field  $Z = 15$  m  $\rightarrow B_z=1.5$  T

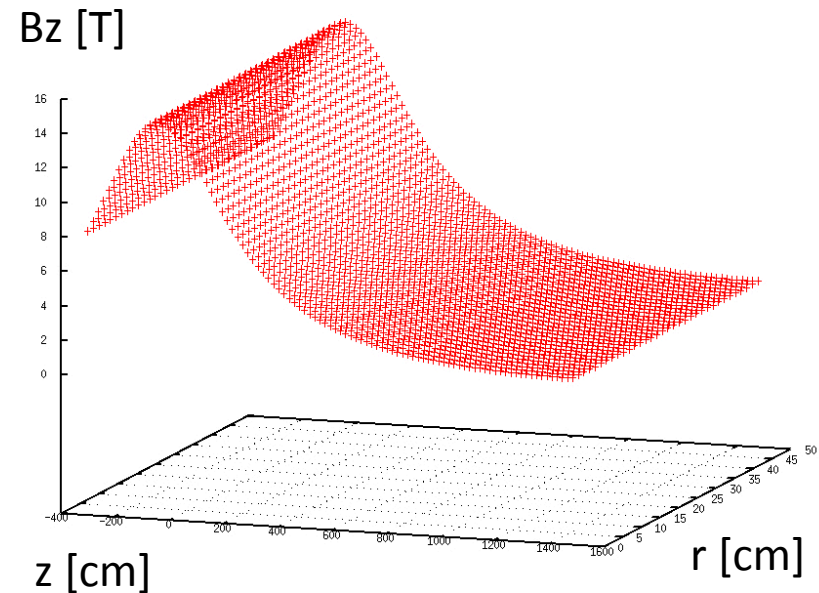
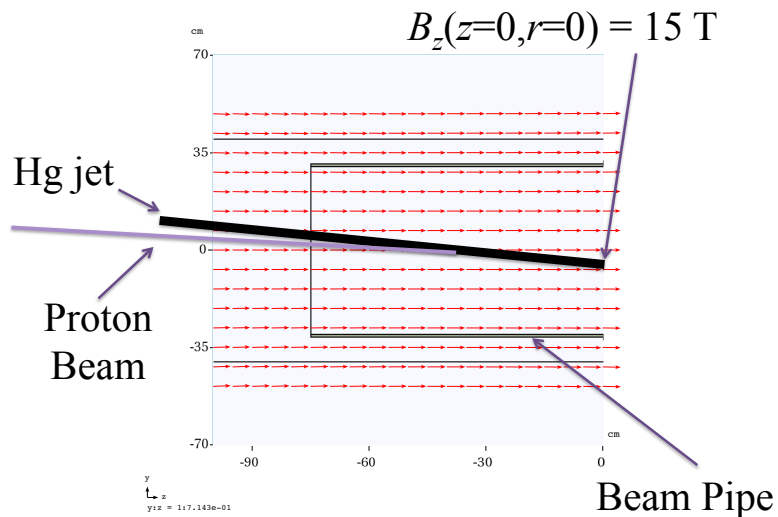
## ➤ Production: Muons within energy KE cut 40-180 MeV

- $3.27 \times 10^4$  ( $N_{\text{ini protons}}=10^5$ )
- $N_{\text{mesons}}/N_{\text{protons}}=0.327$



# MARS SIMULATION SETUP

- Beam Pipe with constant  $R=30$  cm (eliminate particle loss due to scrapping)
- Beam Pipe material changed to balckhole to speed calculations
- Added subroutine to m1510.f (FIELD) to calculate the field using inverse cubic equations



# ANALYTIC FORM FOR TAPERED SOLENOID

Inverse-Cubic Taper

$$B_z(0, z_i < z < z_f) = \frac{B_1}{[1 + a_1(z - z_1) + a_2(z - z_1)^2 + a_3(z - z_1)^3]^p}$$

$$a_1 = -\frac{B_1'}{pB_1} \quad a_2 = 3 \frac{(B_1/B_2)^{1/p} - 1}{(z_2 - z_1)^2} - \frac{2a_1}{z_2 - z_1}$$

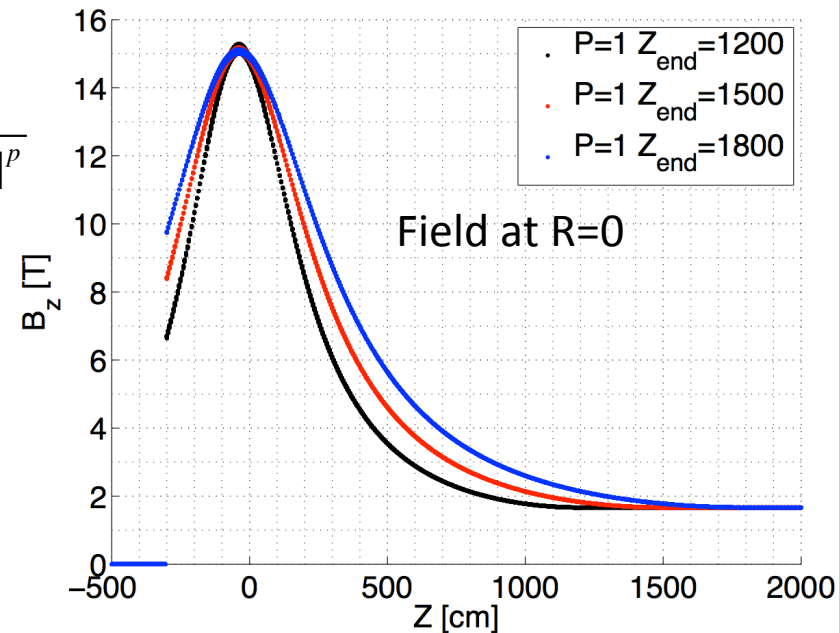
$$a_3 = -2 \frac{(B_1/B_2)^{1/p} - 1}{(z_2 - z_1)^3} + \frac{a_1}{(z_2 - z_1)^2}$$

Off-axis field approximation

$$B_z(r, z) = \sum_n (-1)^n \frac{a_0^{(2n)}(z)}{(n!)^2} \left(\frac{r}{2}\right)^{2n}$$

$$B_r(r, z) = \sum_n (-1)^{n+1} \frac{a_0^{(2n+1)}(z)}{(n+1)(n!)^2} \left(\frac{r}{2}\right)^{2n+1}$$

$$a_0^{(n)} = \frac{d^n a_0}{dz^n} = \frac{d^n B_z(0, z)}{dz^n}$$



! First Order

BZ = B1 / CUBIC\*\*POW

BR = -R / 2. \* DBZ1

! Second Order

BZ = BZ - R\*\*2 / 4. \* DBZ2

BR = BR + R\*\*3 / 16. \* DBZ3

! Third Order

BZ = BZ + R\*\*4 / 64.0 \* DBZ4

BR = BR - R\*\*5 / 384.0 \* DBZ5

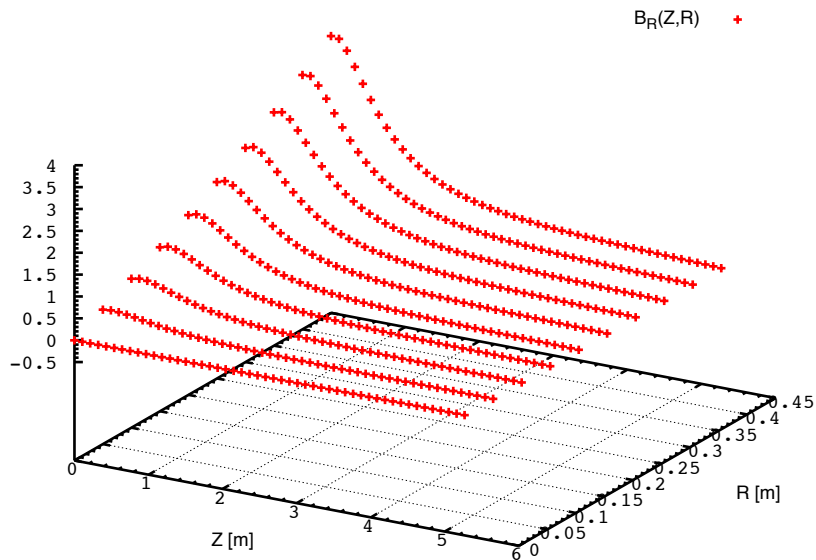
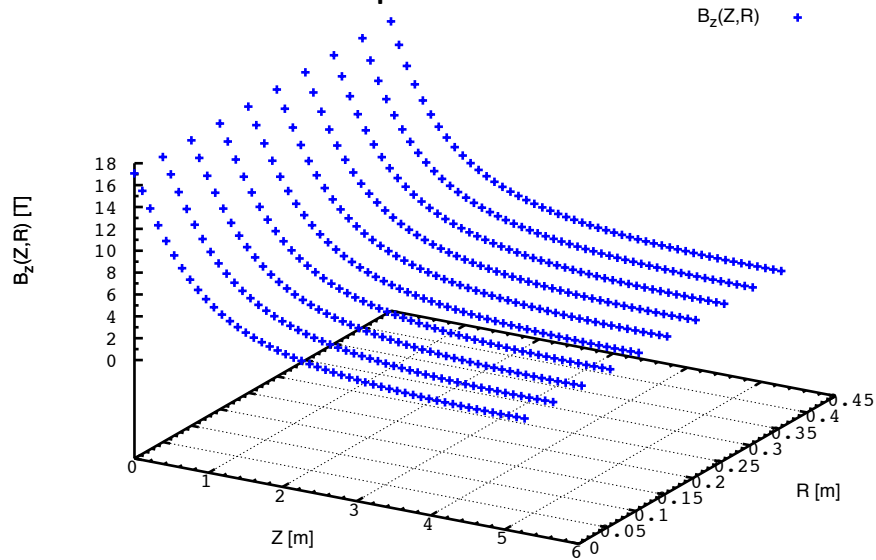
! Fourth Order

BZ = BZ - R\*\*6 / 2304.0 \* DBZ6

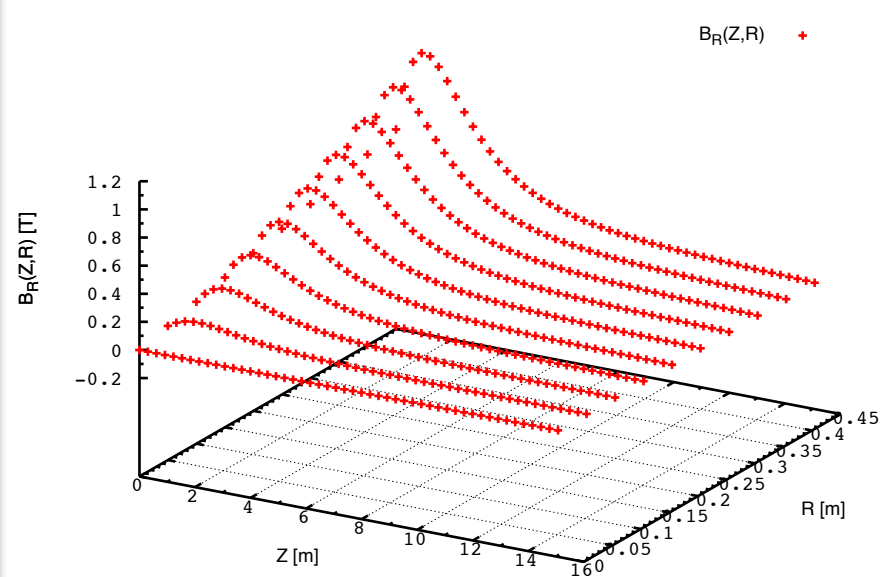
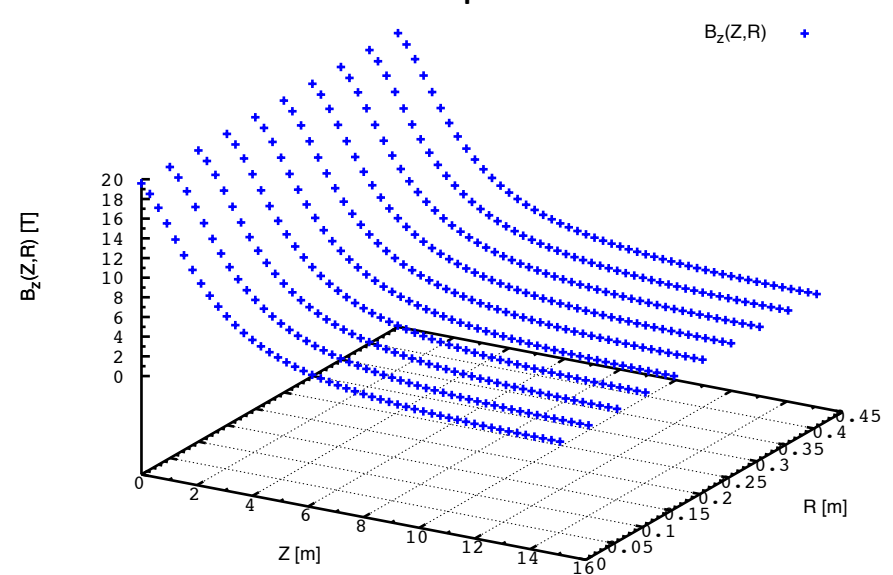
BR = BR + R\*\*7 / 18432.0 \* DBZ7

## SOLENOID TAPERED FIELD

Bz=20-1.5T Ltaper=4 m

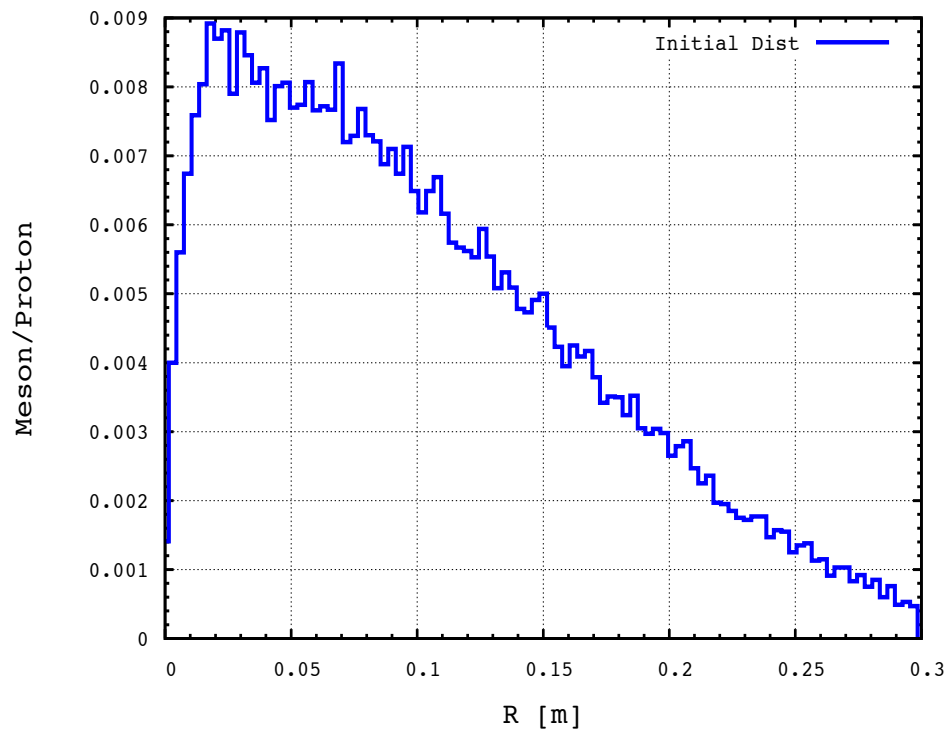


Bz=20-1.5T Ltaper=14 m

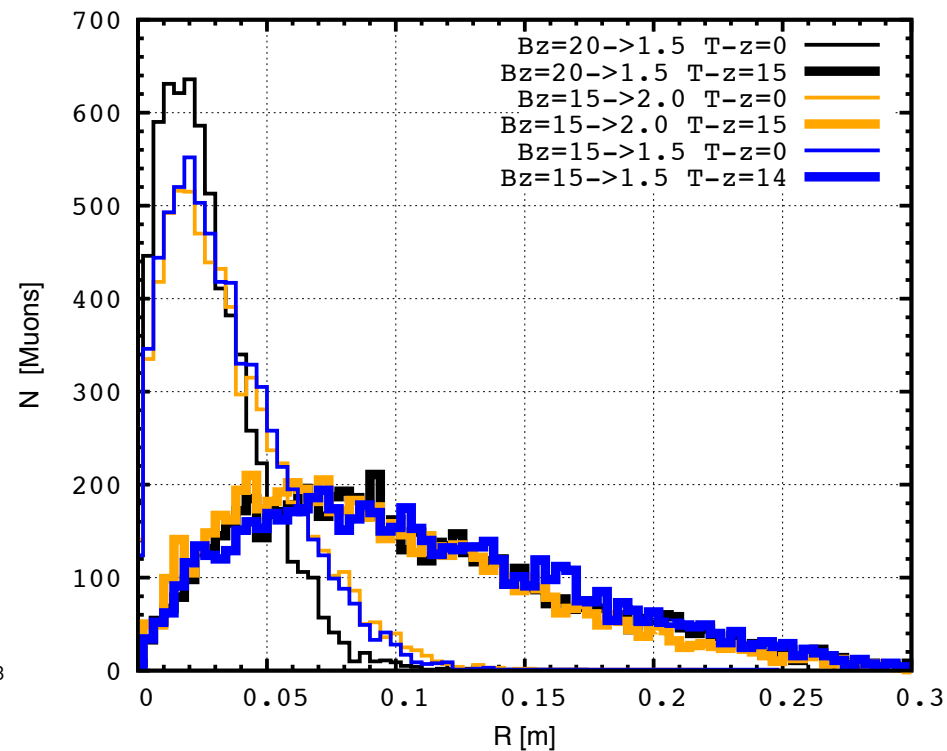


# INITIAL PARTICLE DISTRIBUTIONS

Distribution of all Mesons at  $z=0$

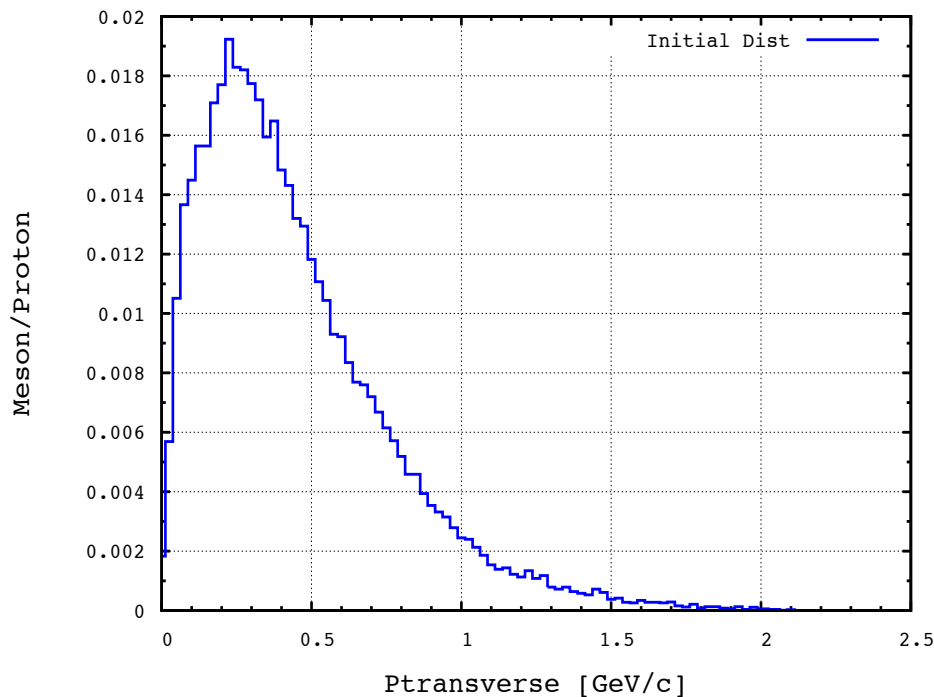


Distribution of Muons which made it to the end of cooling section and satisfied acceleration acceptance cuts  
Taper Length=8 m

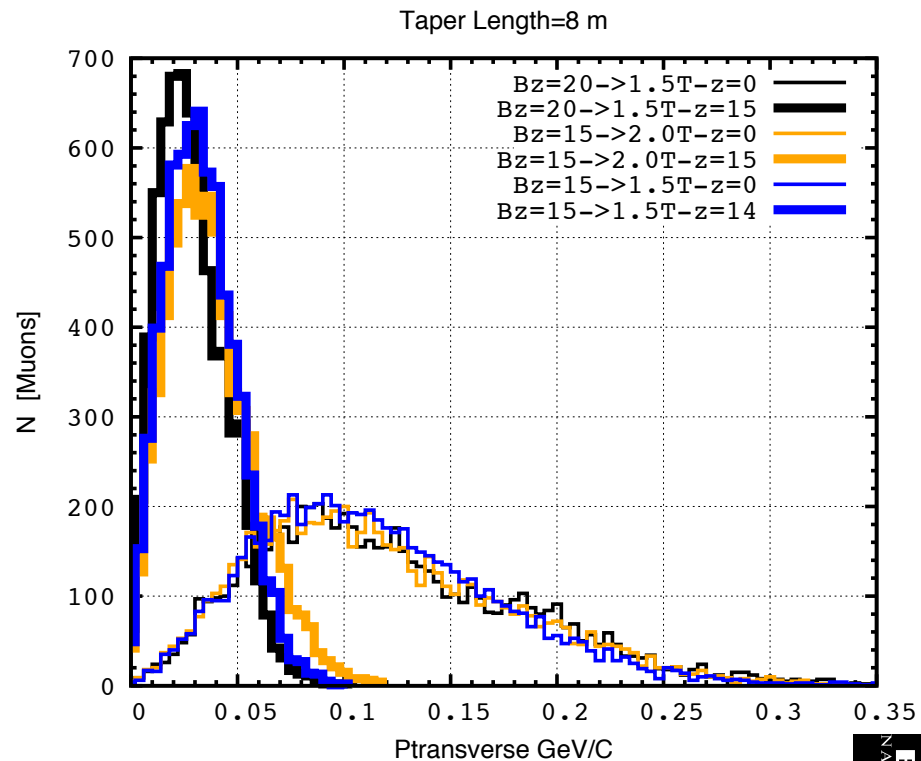


# GOOD MUONS PARTICLE DISTRIBUTIONS

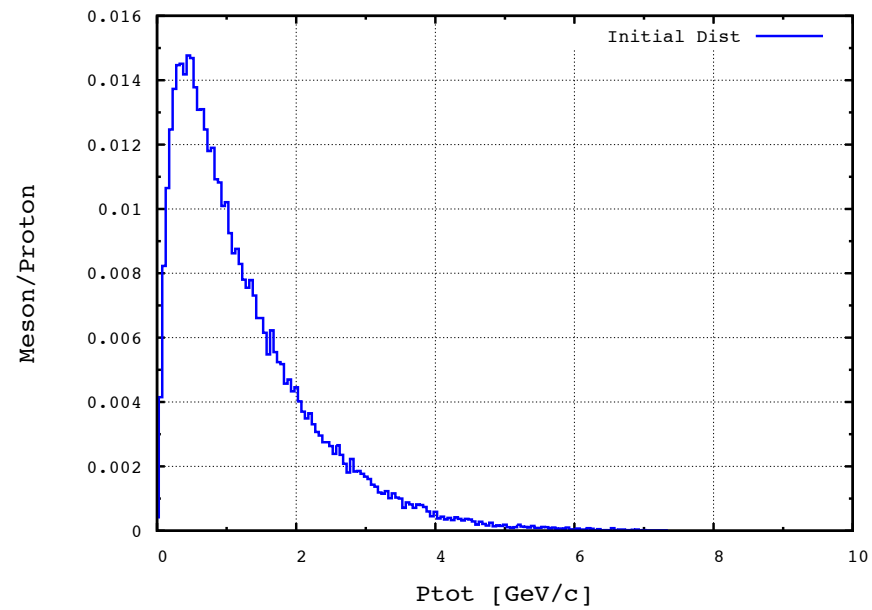
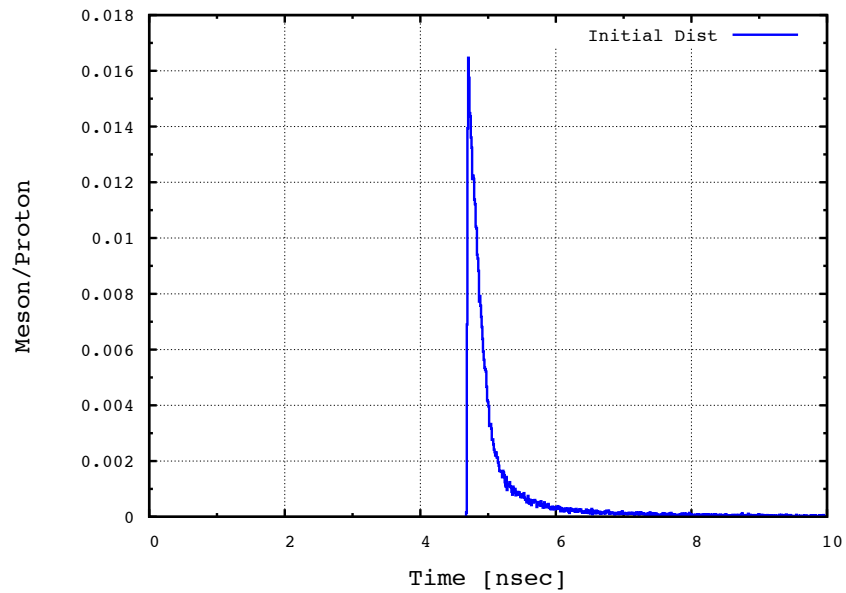
Distribution of all Mesons at  $z=0$



Distribution of Muons which made it to the end of cooling section and satisfied acceleration acceptance cuts



# MESONS INITIAL DISTRIBUTION

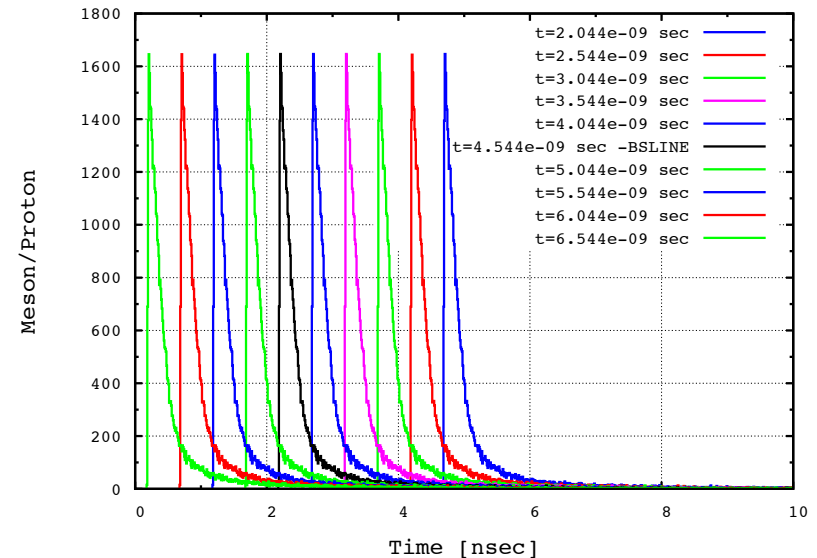
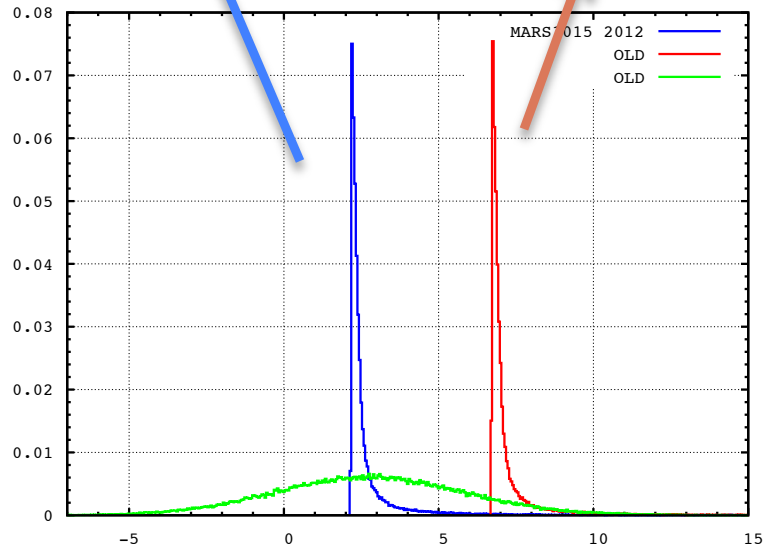




# FIXING TIME OF ARRIVAL

TOA Protons  
at  $z=-75$  cm

TOA Protons  
at  $z=-200$  cm

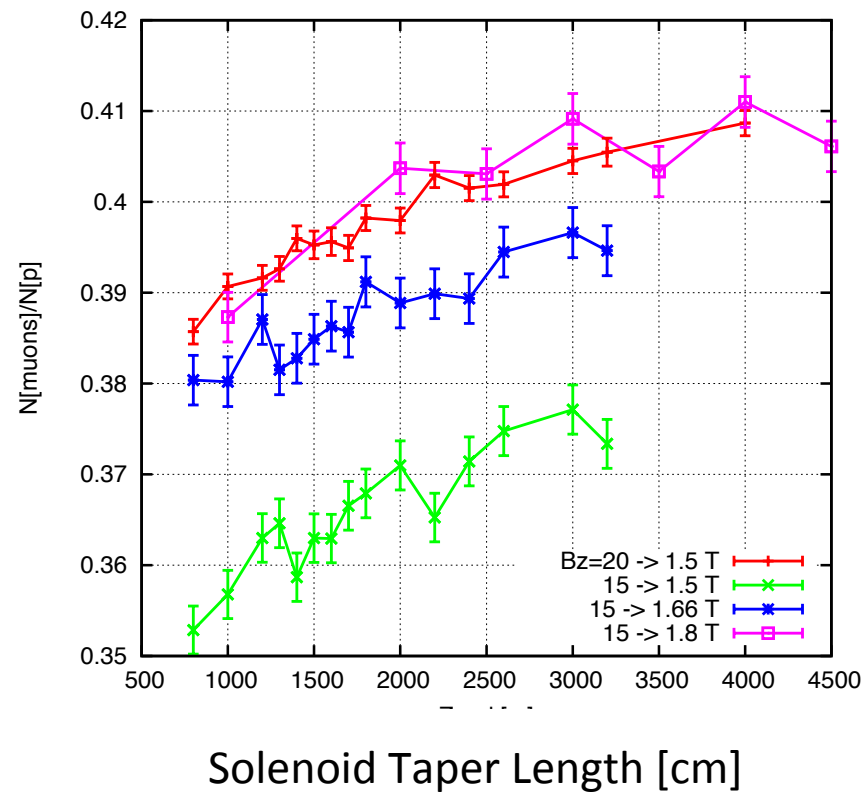


MARS simulation was performed with a “pancake” shaped proton beam, lunched at  $t=0$  from a specified  $z<0$ .

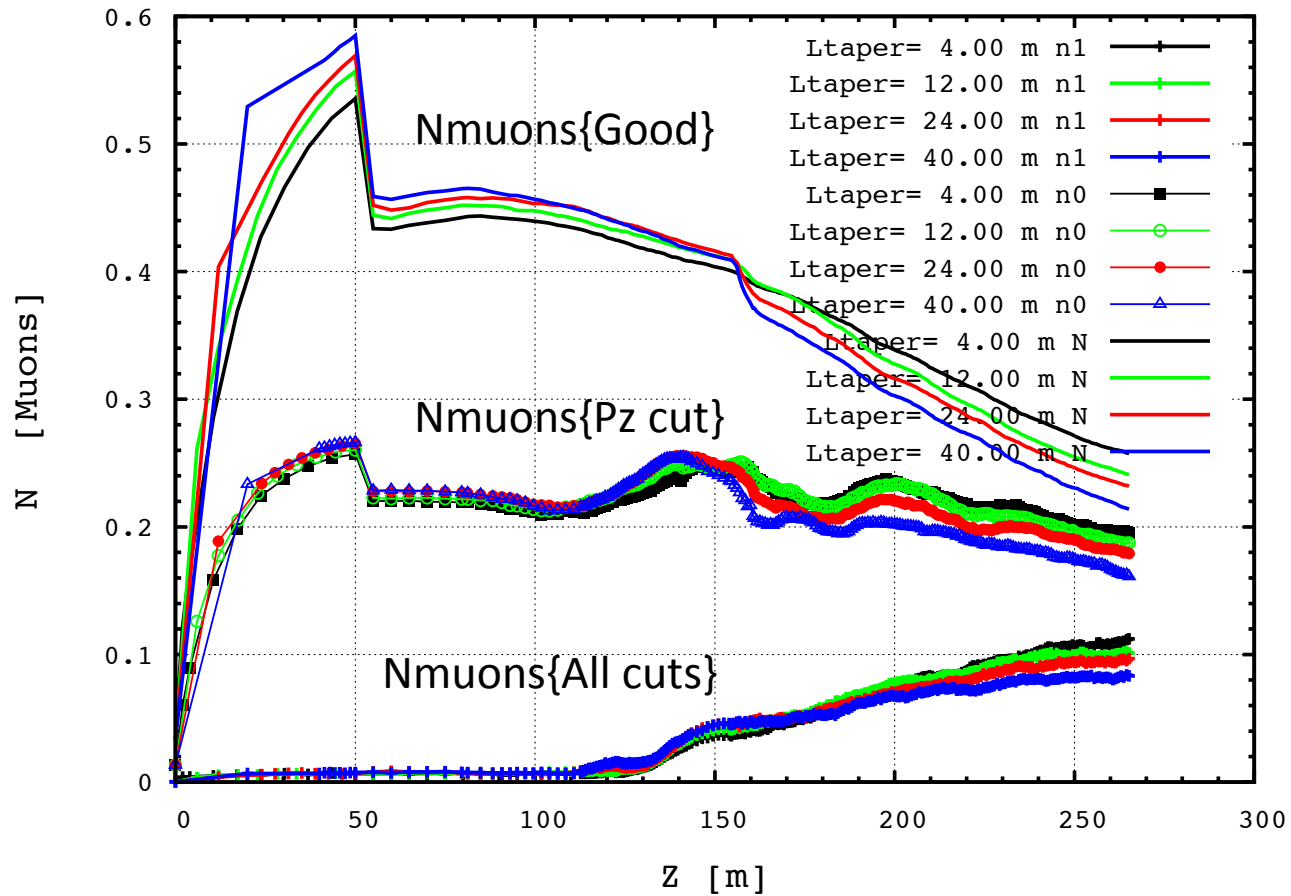
The Gaussian time distribution is “usually” produced by using a random Gaussian generator on the meson distribution at  $z=0$ .

## TRANSMISSION

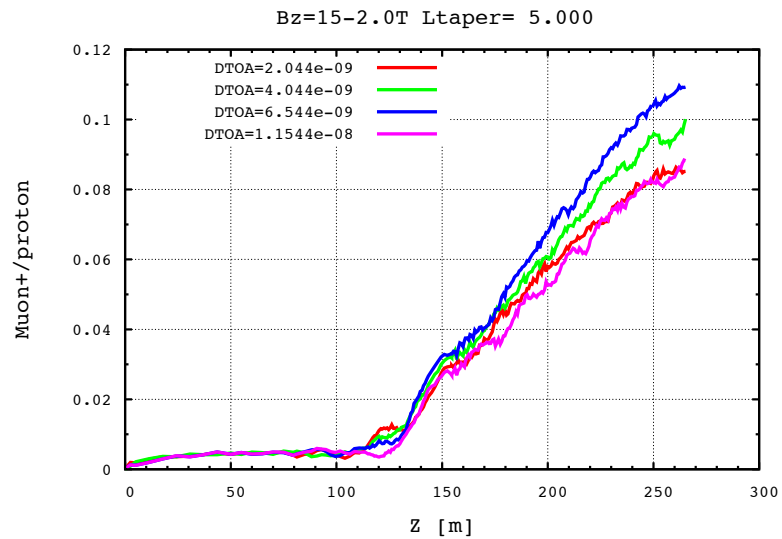
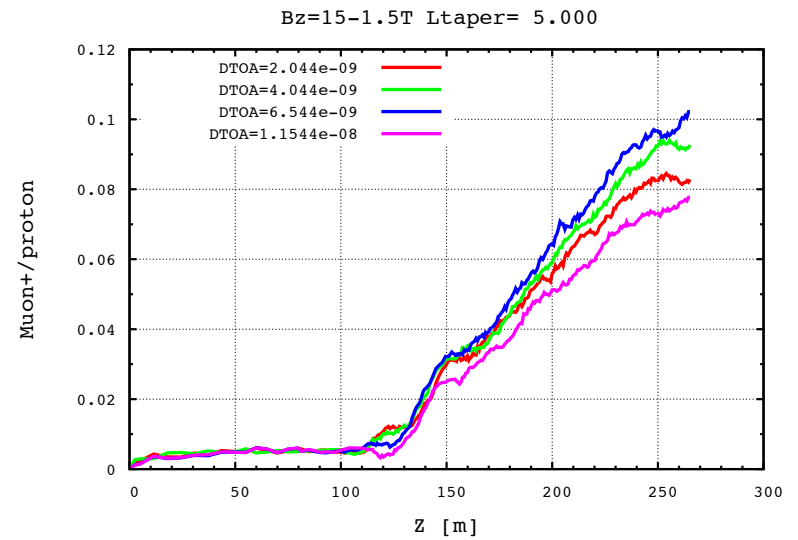
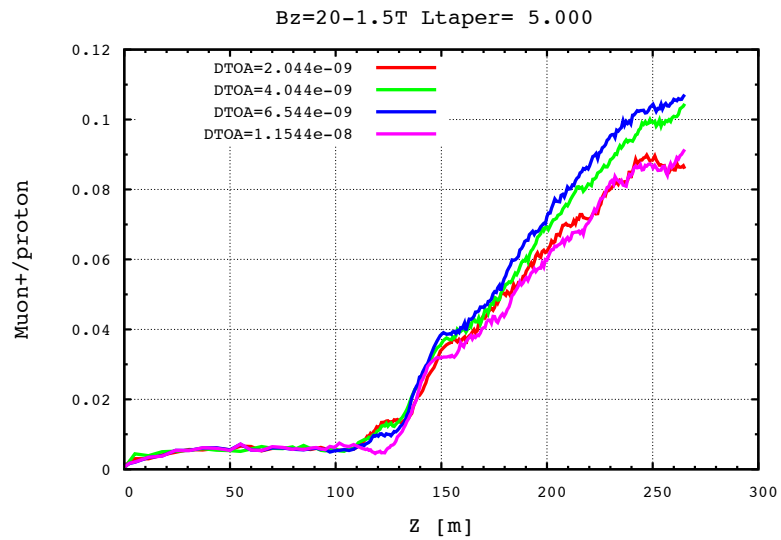
MARS simulation results:  
Counting muons at 50 m with K.E. 80-140 MeV



## TRANSMISSION

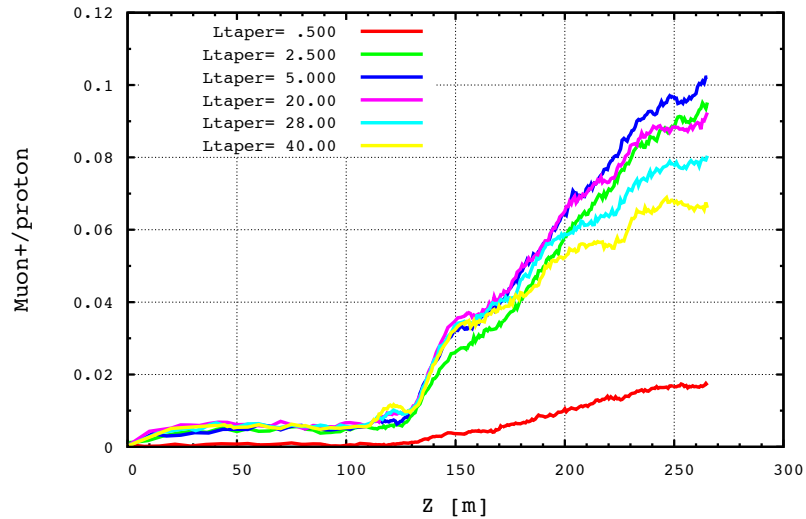


# TIME OF ARRIVAL SCAN

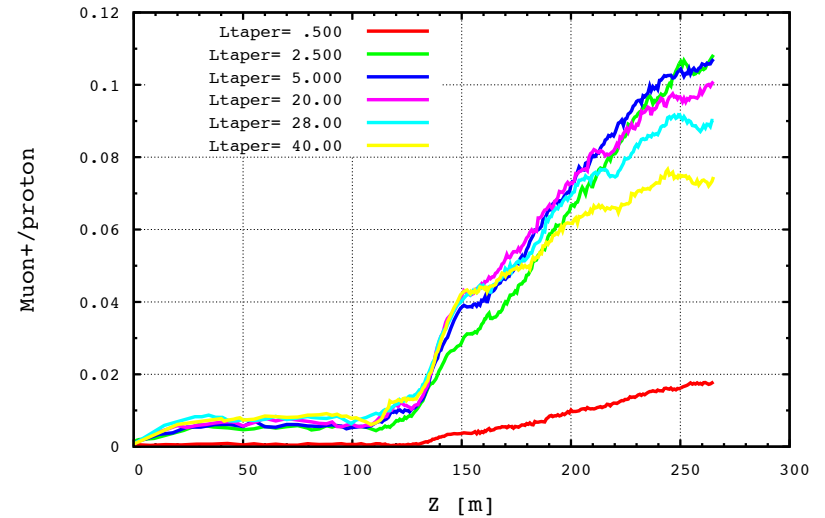


# TAPER SCAN

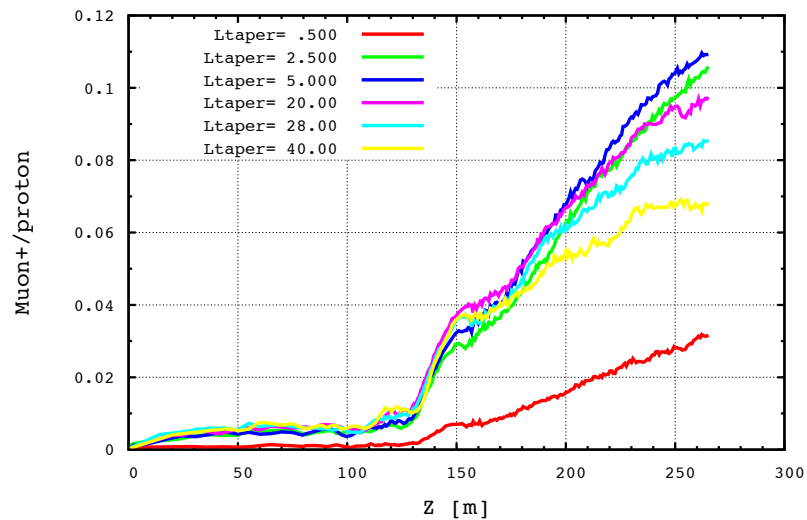
Bz=15-1.5T TOA=6.544e-09



Bz=20-1.5T TOA=6.544e-09

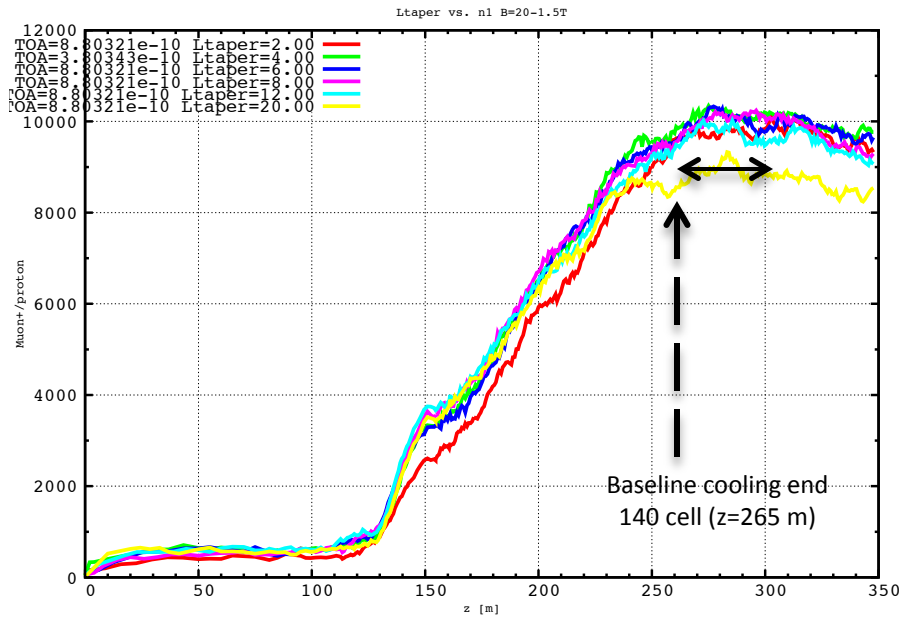


Bz=15-2.0T TOA=6.544e-09

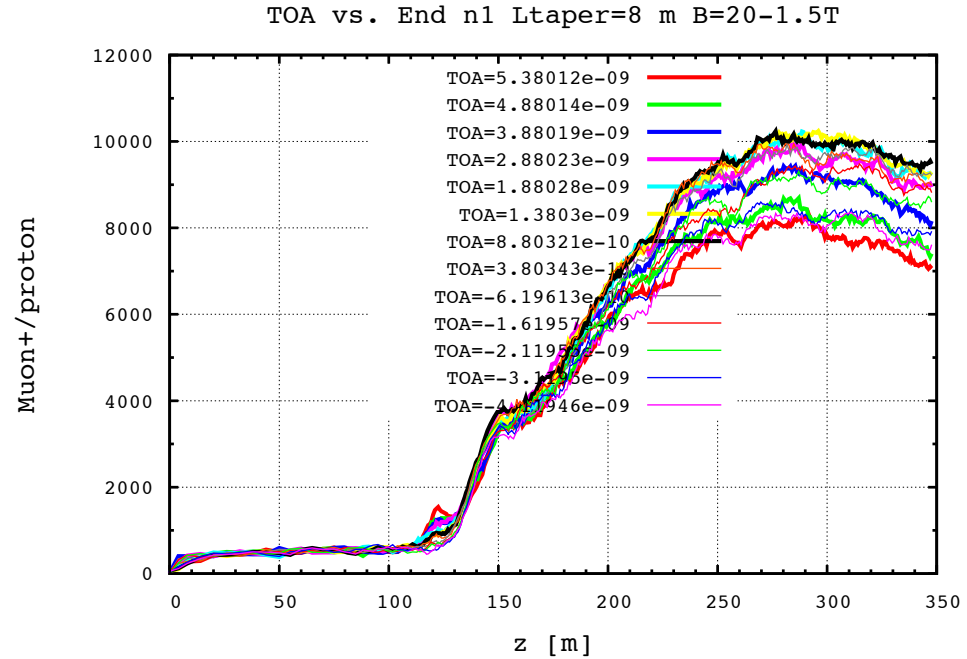


# MORE COOLING

For every taper length optimized TOA

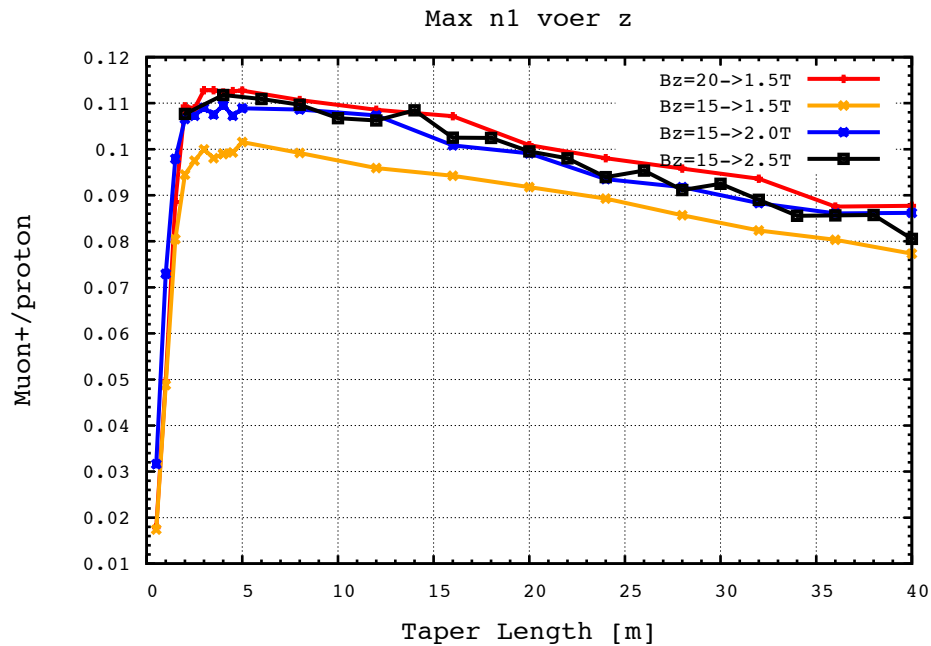


For 8 m taper length TOA scan

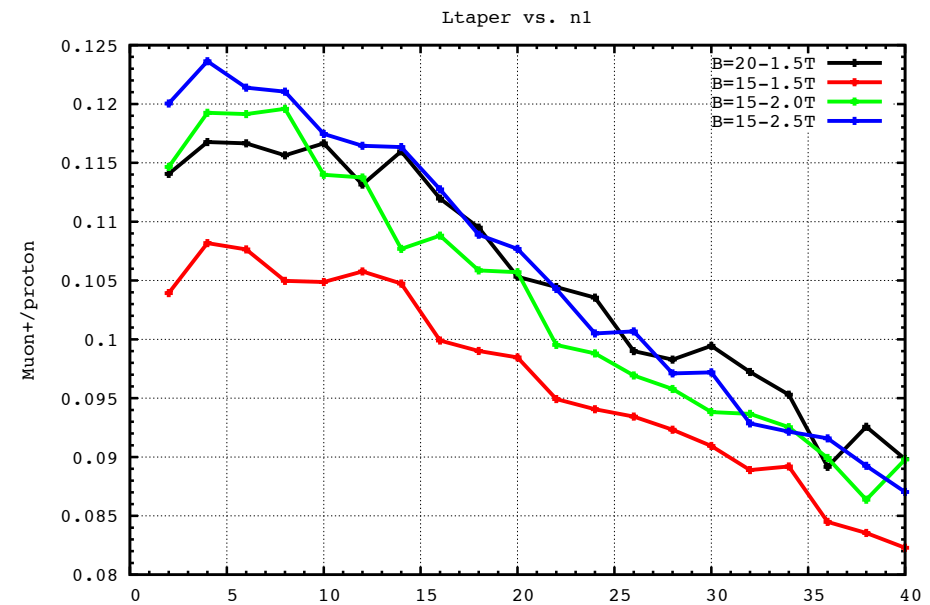


# TIME & TAPER LENGTH SCAN

Using baseline cooling section  
(140 cooling cell)

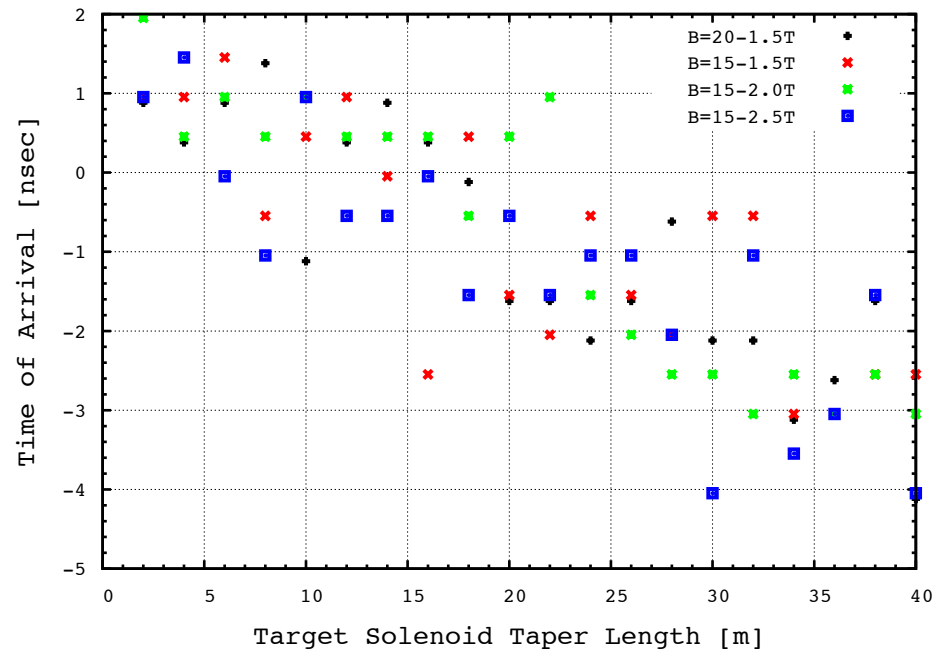


Using longer cooling section  
(200 Cooling cell)



# TIME & TAPER LENGTH SCAN

TOA for optimum throughput at end of cooling for each capture solenoid case





## CONCLUSION & SUMMARY

- Varying the capture solenoid settings requires optimizing the time of arrival (re-phasing) .
- Longer tapers have more meson yield at the decay channel ( $z=50$ ).
- Shorter tapers produce “more good” muons which could be bunched & cooled.
- The maximum yield requires tapers with  $z=4-6$  m.
- Particle loss at  $z=150$  m needs more detailed study.
- Adding longer cooling channel is required to reach maximum cooling.