

Preliminary Analysis of the Target System Magnets

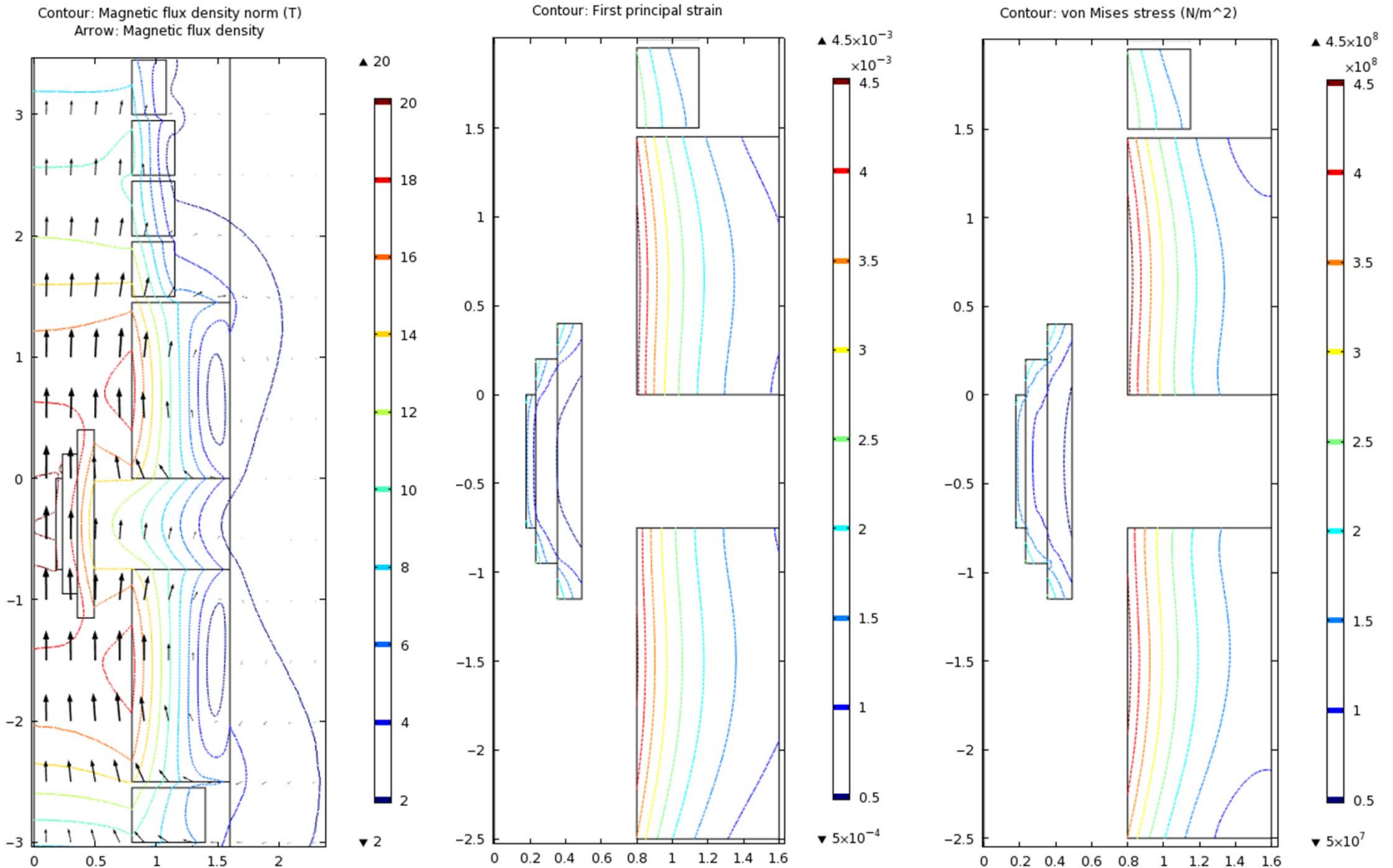
1. Version with a 6-T copper magnet insert
2. Version with a 6-T high-temperature superconductor insert
3. Deformations of the WC shield due to gravity.

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The IDS80d magnet configuration suffered from too high peak field in the superconducting magnets near the target, and from too high fields in these magnets if the 6-T copper magnet insert were to trip off.

A revised configuration, IDS80e, mitigates these issues.

IDS80d Beam is upwards



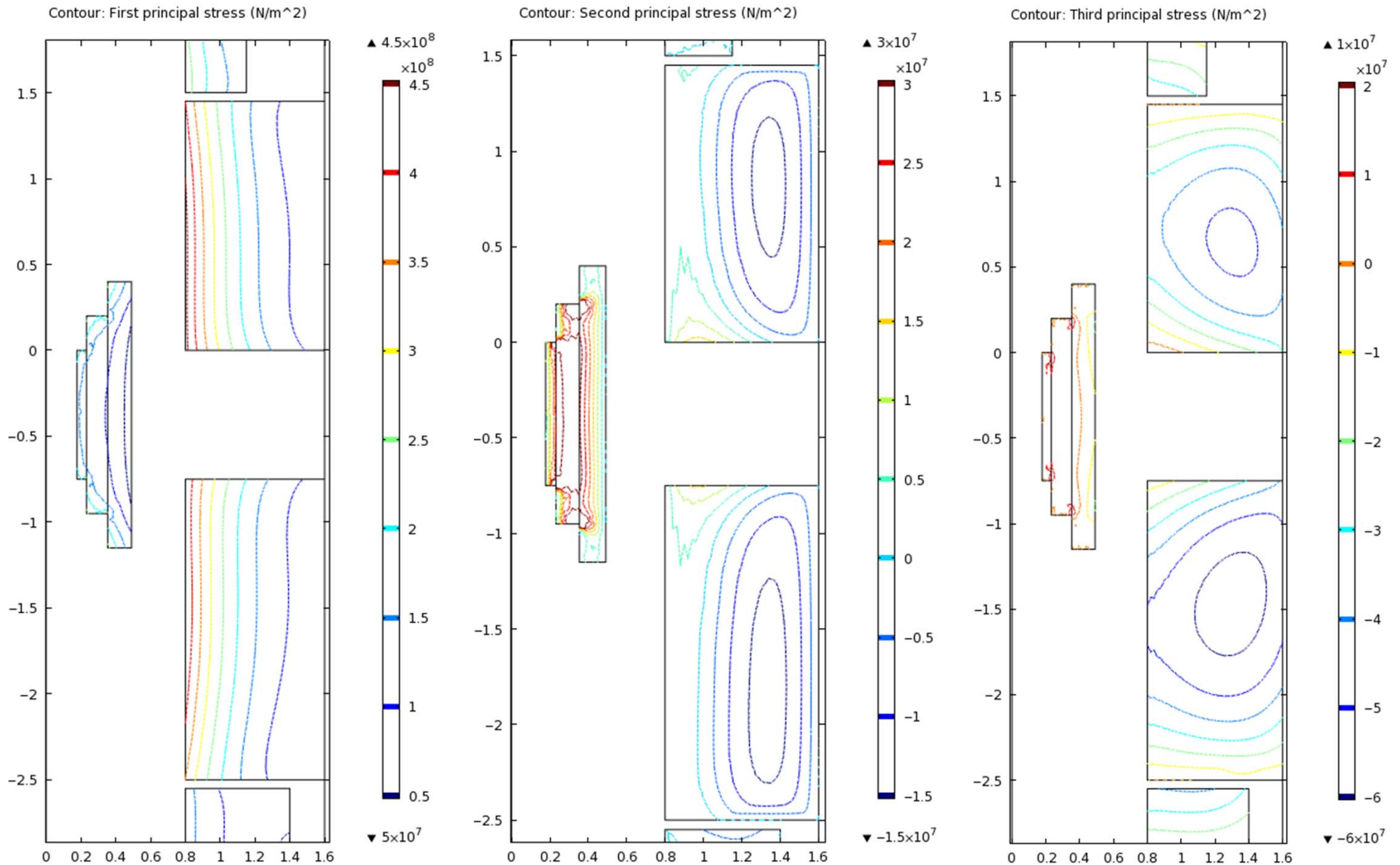
Upstream solenoids of 20 T, 2.3 GJ target magnet "ids80d".

Left: Windings cross section and field magnitude (contours) & direction (arrows). Innermost three solenoids are copper hollow conductor ($B = 6$ T; $P = 8.8$ MW); others shown are Nb_3Sn . $B_{\text{max}} = 20.08$ T; $B = 20$ T at $z = 0, -34$ cm, -43 cm & -74 cm.

Center: Hoop strain; $\epsilon_{\text{max}} = 0.463\%$ if orthotropic Young's modulus components $\{E_\phi, E_r, E_z\} = \{100, 20, 20\}$ GPa.

Right: von Mises stress, σ_{VM} ; max. $\sigma_{\text{VM}} = 473$ MPa.

IDS80d Beam is upwards



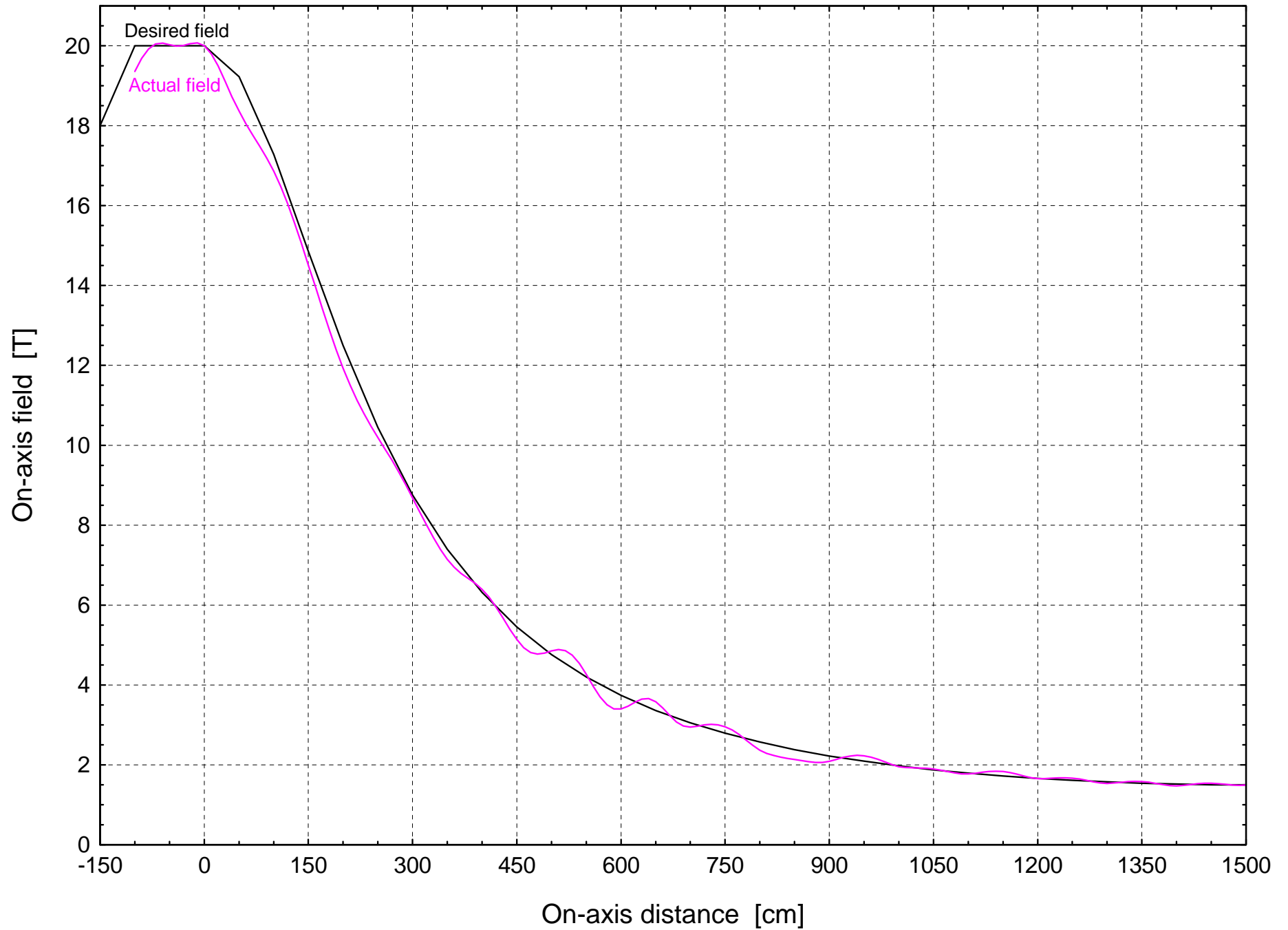
Principal stresses. Left: circumferential (hoop) stress, σ_ϕ ; maximim $\sigma_\phi = 469$ MPa.

Center: radial stress, σ_r .

Right: Axial stress, σ_z ; max. compression = 62 MPa. Axial load on most-upstream Nb₃Sn solenoid is 162 MN (downstream direction); loads, in MN, on successive solenoids = {142, -66, -71, -22, -35, -36}.

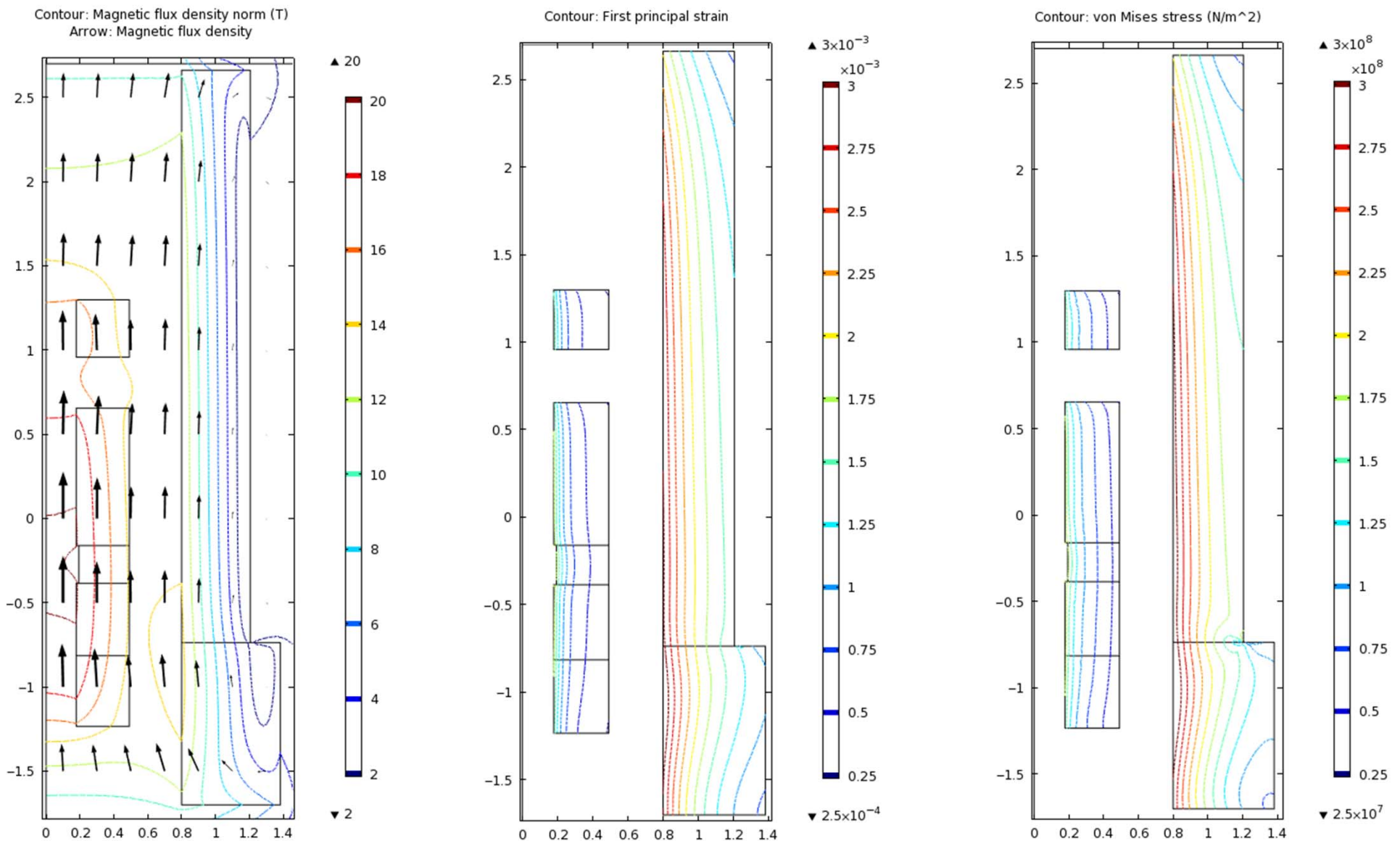
IDS80d

On-Axis Field Profile of Fernow 20 T Target Magnet



IDS80e with lower peak field in SC magnets

Beam is upwards



Upstream solenoids of HC&SC20T# target magnet with 6 T, 10.0 MW magnet of copper hollow conductor in 14 T SC magnet; magnetic energy = 1.18 GJ.

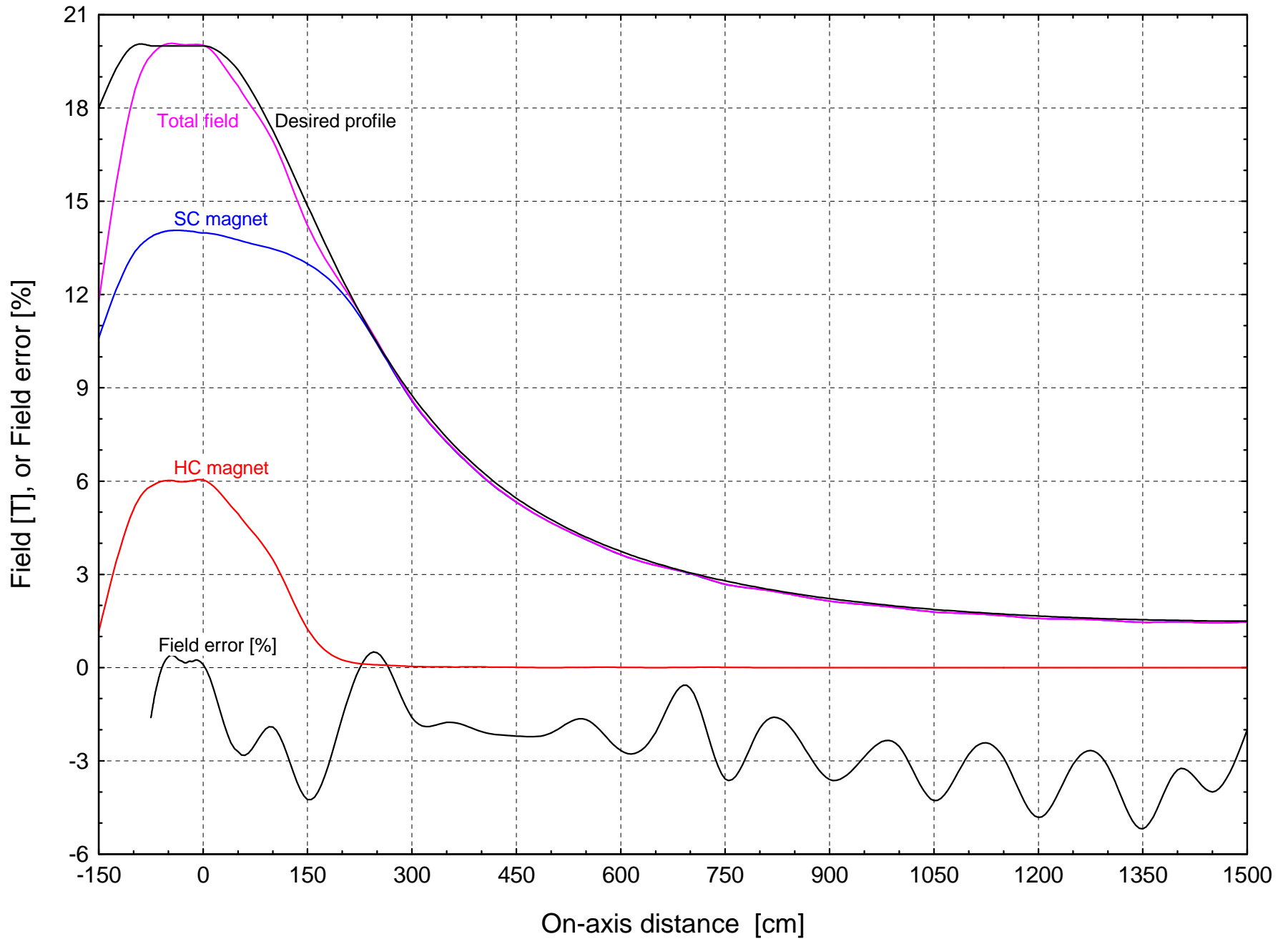
Left: Windings cross section and field magnitude (contours) & direction (arrows); maximum $B_{SC} = 14.6$ T.

Center: Hoop strain with orthotropic Young's modulus components $\{E_\phi, E_r, E_z\} = \{100, 20, 20\}$ GPa; $\epsilon_{max} = 0.326\%$.

Right: von Mises stress, σ_{VM} ; max. $\sigma_{VM} = 340$ MPa.

IDS80e with lower peak field in SC magnets

On-Axis Field Profile of Superconducting and Hollow-Conductor Magnets of "HC&SC20T#"



Replacement of the 6-T copper magnet insert by a 6-T high temperature superconducting magnet could be attractive.

However, the peak stresses in the HTS coil would exceed the capability of any present conductor, \Rightarrow need significant conductor R&D before this option is viable.

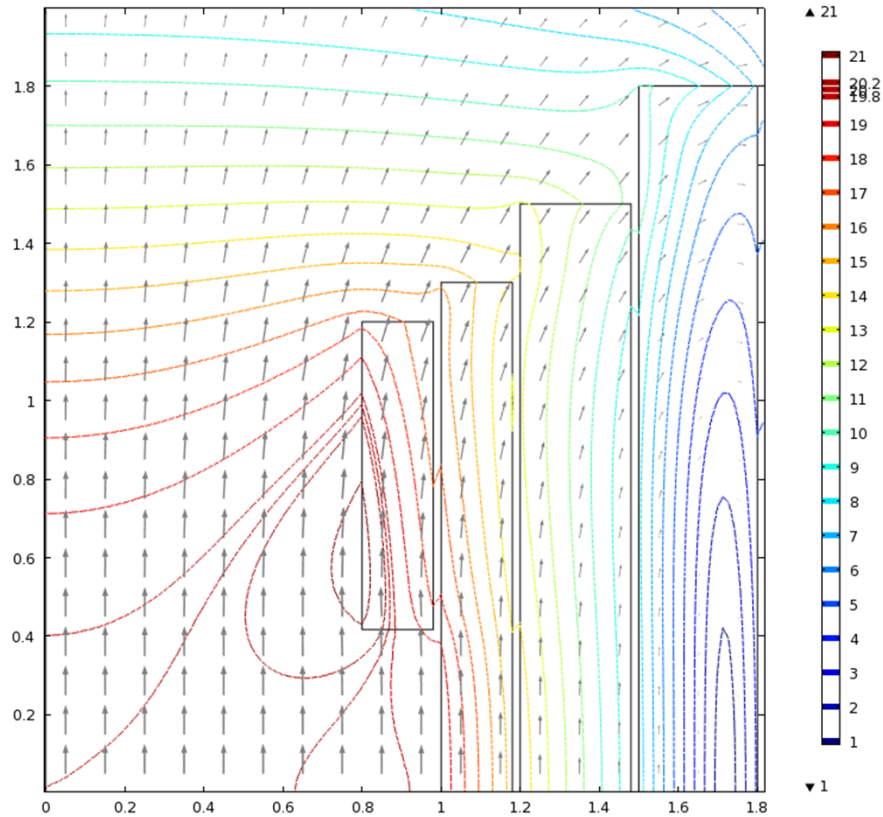
Four-Coil Magnet System near the Target

Inner 2 coils are HTS, 3rd is Nb₃Sn, 4th is NbTi

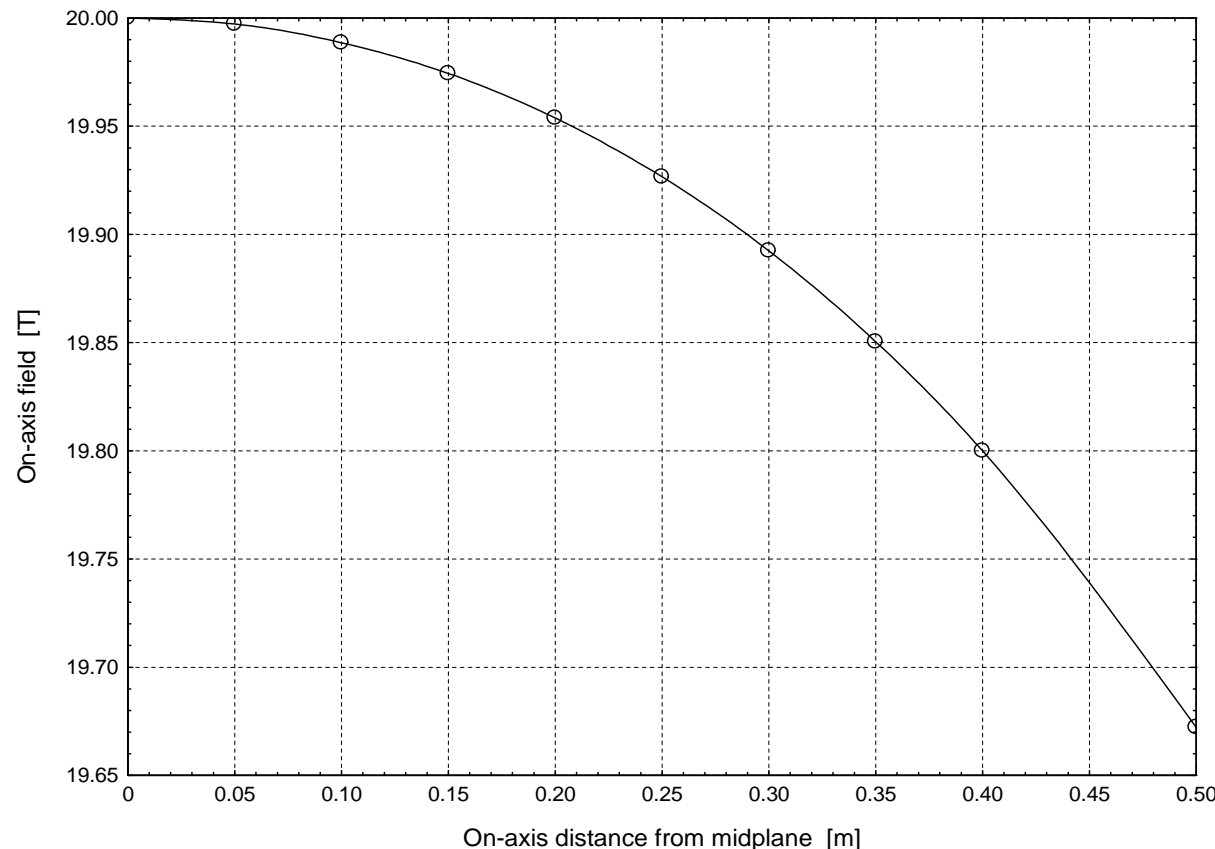
Beam is upwards.

The coils are symmetric about $z = 0$.

Contour: Magnetic flux density norm (T) Arrow: Magnetic flux density



On-Axis Field Profile of Four-Coil 20-Tesla Muon-Collider Target Magnet



Four-coil 20-T pion-capture magnet. Annular spacing = 2 cm.

Inner HTS magnet: I.R. $\equiv a_{11} = 80$ cm; O.R. $\equiv a_{21} = 98$ cm; half length $\equiv b_1 = 120$ cm; half gap $\equiv g_1 = 41.7$ cm; coil current density $\equiv j_1 = 23.4$ A/mm²; central field contribution $\Delta B_1 = 2$ T; maximum ambient field $B_1 = 21.5$ T.

Outer HTS coil: $a_{22} = 118$ cm; $b_2 = 130$ cm; $j_2 = 23.1$ A/mm²; $\Delta B_2 = 4$ T; $B_2 = 19.8$ T.

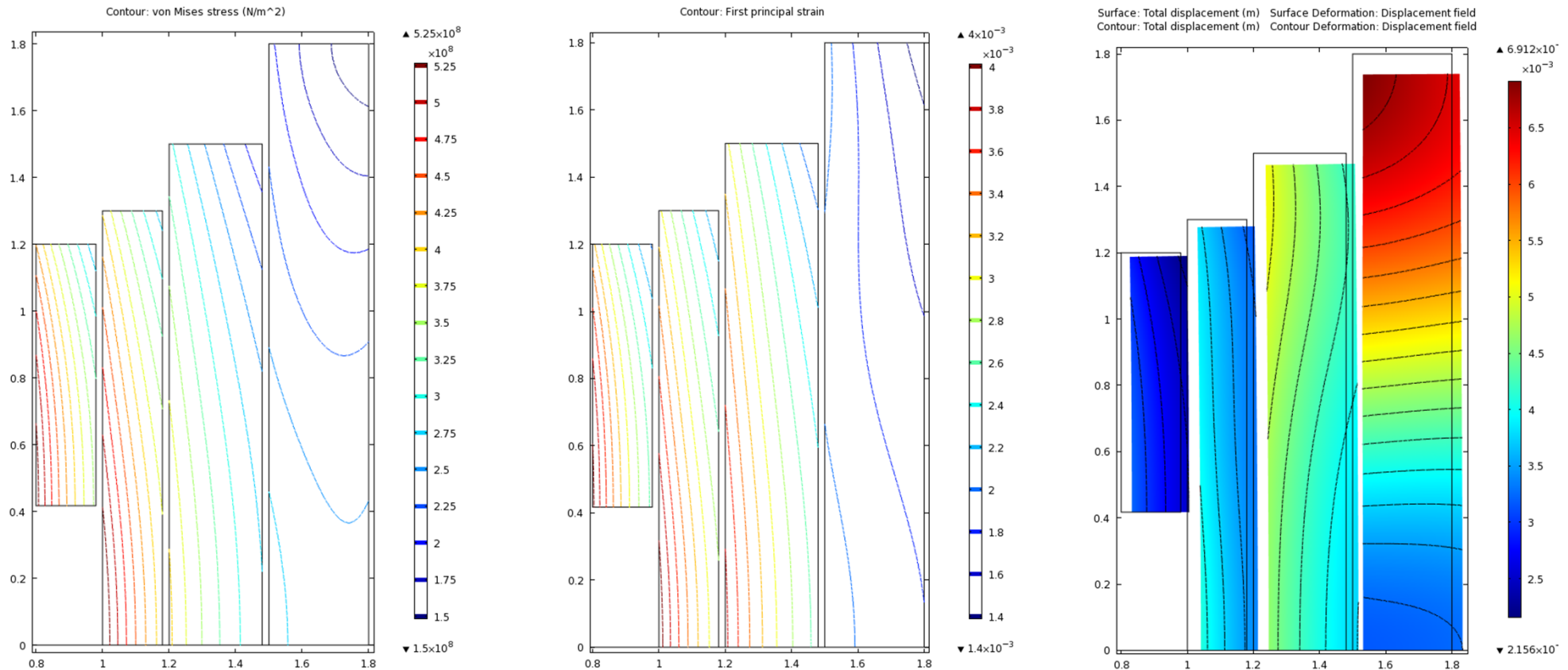
Nb₃Sn coil: $a_{23} = 148$ cm; $b_3 = 150$ cm; $j_3 = 19.0$ A/mm²; $\Delta B_3 = 5$ T; $B_3 = 14.6$ T.

NbTi coil: $a_{24} = b_4 = 180$ cm; $j_4 = 32.4$ A/mm²; $\Delta B_4 = 9$ T; $B_4 = 10.8$ T.

Left: First-quadrant cross section, field magnitude (contours) & direction (arrows).

Right: Field homogeneity is 1% over $z = \pm 40$ cm.

Stress, Strain and Deformation in Magnets of Slide 9



Stress, strain and deformation in magnets of slide 9 with orthotropic windings.

Young's moduli $\{E_r, E_\phi, E_z\} = \{26, 130, 65\}$ GPa in HTS coils and $\{20, 100, 40\}$ GPa in LTS coils.

130 GPa derived from 50% Hastelloy of 220 GPa^[13] + 25% copper of 80 GPa (320 MPa stress @ 0.4% strain) + 25% coolant & insulation (negligible stiffness).

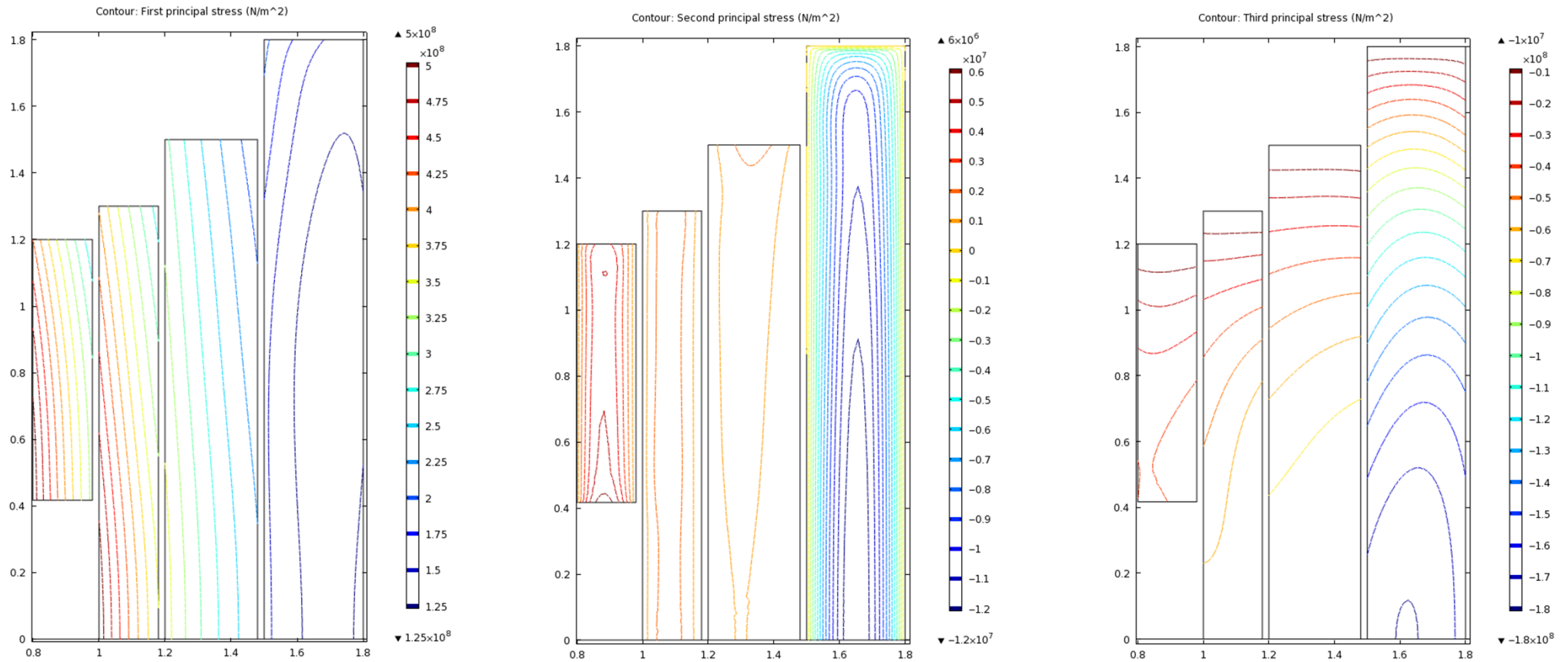
100 GPa derived from 35% steel of ~ 230 GPa^[14] + 25% Cu + 40% residual for Nb₃Sn coil and, for NbTi coil, 20% steel + 40% Cu of ~ 135 GPa^[15] + 40% residual.

Left: Von Mises stress, averaged locally over winding; maximum stress in consecutive coils = $\{535, 549, 406, 288\}$ MPa.

Center: Hoop strain, ϵ_ϕ ; max. percent = $\{0.40, 0.41, 0.38, 0.21\}$.

Right: Deformation (magnified tenfold) ranges from 2.2 mm to 6.9 mm; contour interval = 0.25 mm.

Principal Stresses in Magnets of Slide 9



Principal stresses in magnets of slide 9.

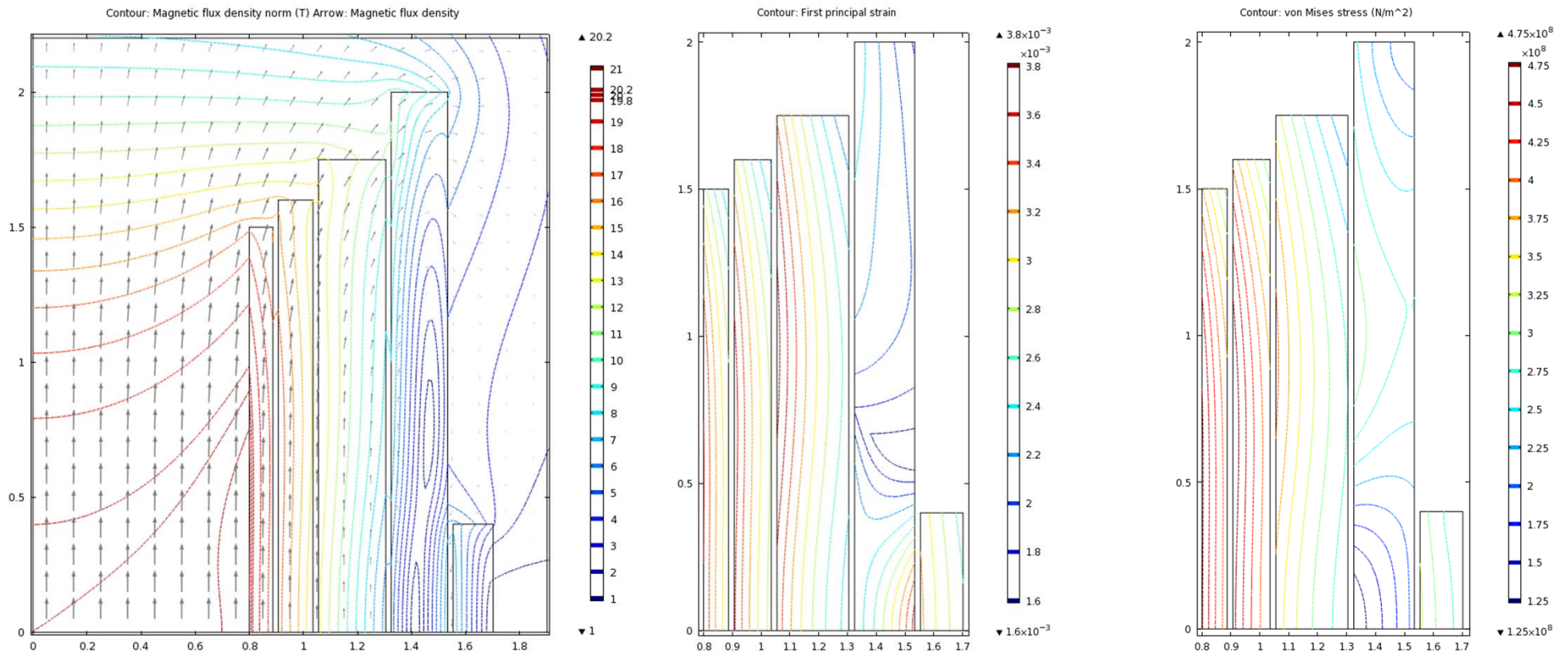
Left: Hoop stress σ_ϕ ; max. MPa = {515, 516, 362, 159}.

Center: Radial stress σ_r ; max. MPa = {6.5, 2.6, 1.6, -12.4}.

Right: Axial stress σ_z ; max. MPa = {-49, -65, -78, -180}.

5-Coil Design with No Midplane Gap

Reversed Current in the 5th, Outer Coil



5-Coil design that eliminates midplane gap by use of reverse-current field-homogenization coil.

Inner HTS coil: $a_{11} = 80$ cm; $a_{21} = 88.7$ cm; $b_1 = 150$ cm; $j_1 = 25.2$ A/mm²; $\Delta B_1 = 2.4$ T; $B_1 = 20.3$ T.

Outer HTS coil: $a_{12} = 90.7$ cm; $a_{22} = 103.5$ cm; $b_2 = 160$ cm; $j_2 = 26.1$ A/mm²; $\Delta B_2 = 3.6$ T; $B_2 = 17.7$ T.

Nb₃Sn coil: $a_{23} = 130.5$ cm; $b_3 = 175$ cm; $j_3 = 23.1$ A/mm²; $\Delta B_3 = 5$ T; $B_3 = 14.1$ T.

NbTi coil: $a_{24} = 153.4$ cm; $b_4 = 200$ cm; $j_4 = 47.2$ A/mm²; $\Delta B_4 = 10.1$ T; $B_4 = 11.0$ T.

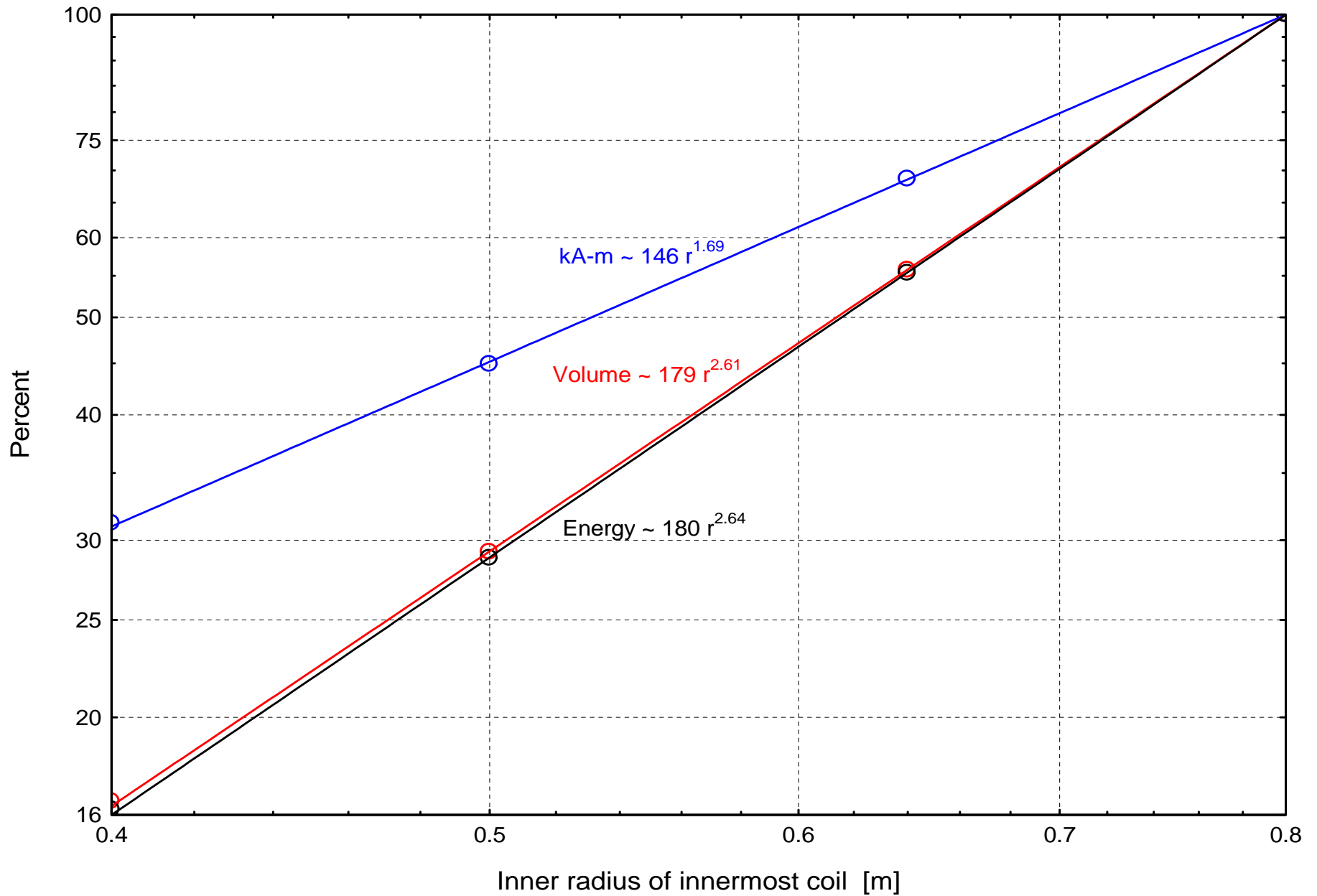
Field-homogenizing coil: $a_{25} = 170.2$ cm; $b_5 = 40$ cm; $j_5 = -j_4$; $\Delta B_5 = -2.09$ T; $B_5 = 7.7$ T.

Left: First-quadrant cross section and field magnitude (contours) & direction (arrows).

Center: Hoop strain ϵ_ϕ ; max. percent $\epsilon_\phi = \{0.36, 0.37, 0.39, 0.37, 0.32\}$.

Right: von Mises stress; max. MPa = $\{480, 496, 406, 315, 328\}$.

Volume, kA-m and Magnetic Energy, Normalized to Magnet of 0.8 m I.R.



Magnet volume, kiloampere-meters & magnetic energy vs. bore diameter.

Reducing the magnet bore by a factor of two would decrease its kA-m by a factor of three, and its volume and energy by a factor of six.

The WC shield weighs ~ 100 tons, and must be supported off the superconducting magnet cryostat.

The following models are "2-D" \Rightarrow no stiffening due to end disks or internal ribs.

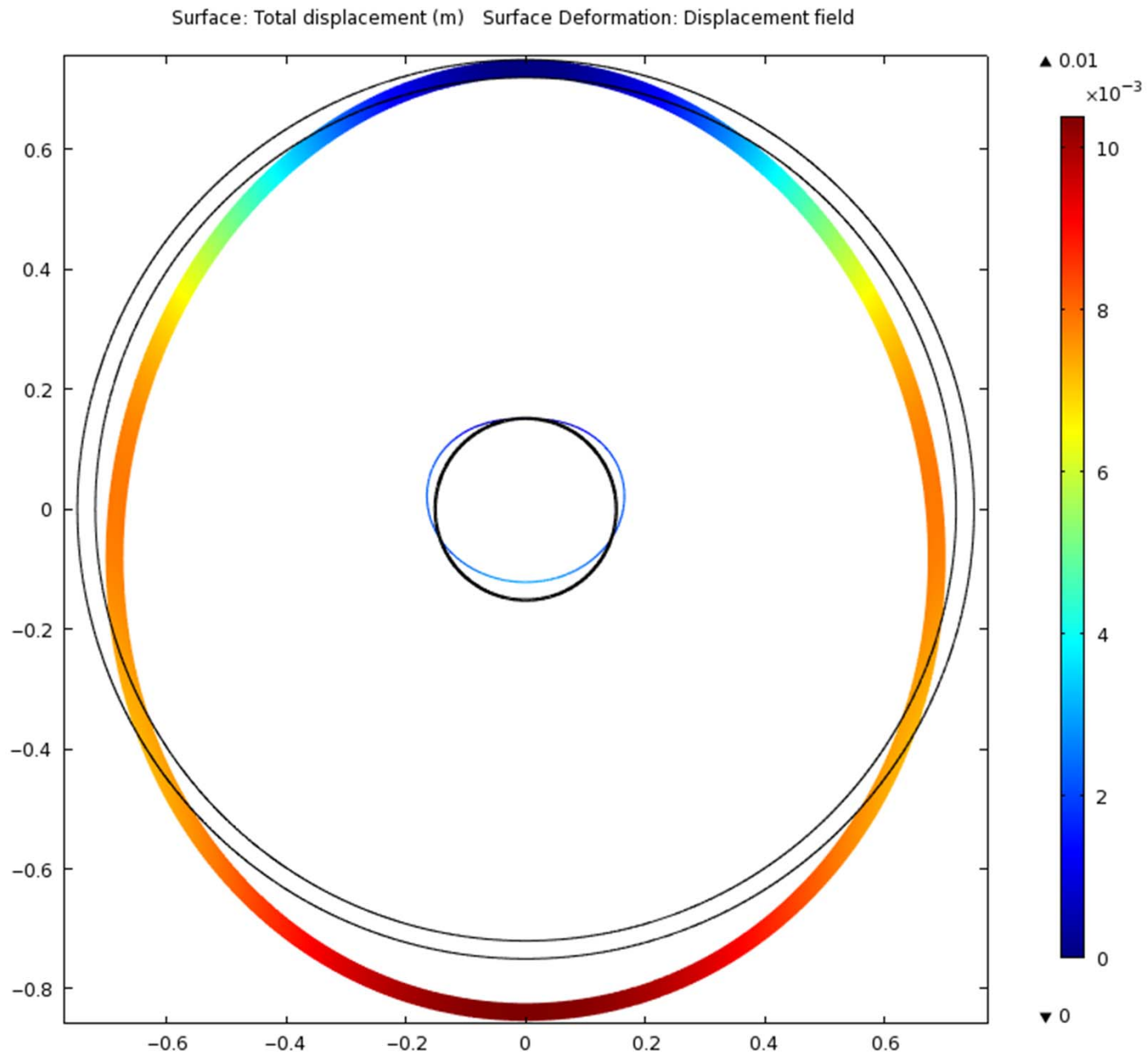
The tungsten-carbide beads + water is modeled as a liquid.

Even with 3-cm-thick walls, the deformations are of order 1 cm.

WC Shield, supported from Top

3-cm-thick walls

Approximate the WC as a liquid, so center tube "floats" upwards

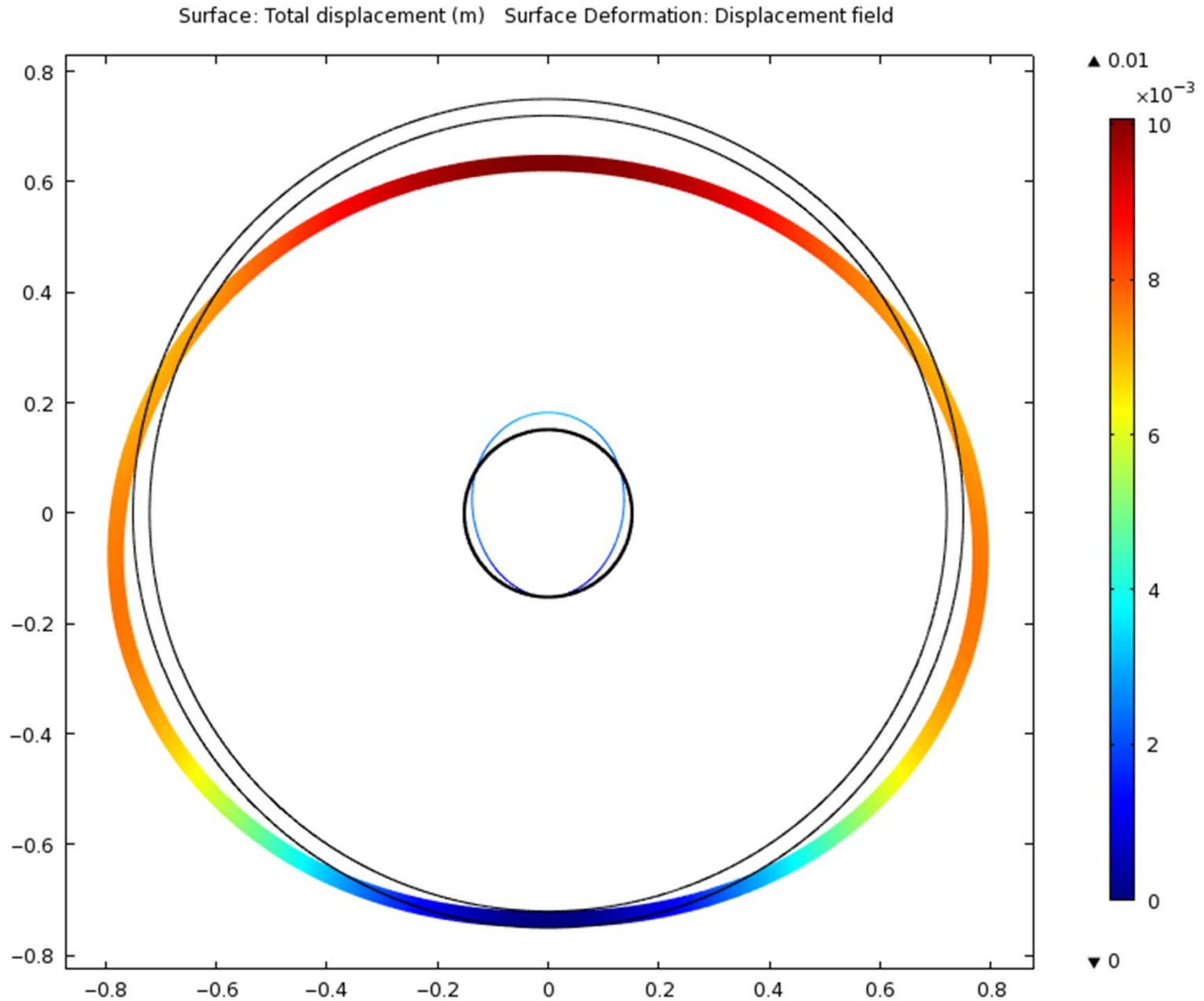


Deformation, magnified tenfold, of horizontal steel cylinders, fixed at 12 o'clock, with annulus of 10 g/cm³ fluid;
 $r_1 = 15$ cm; $dr_1 = 3$ mm; $r_2 = 72$ cm; $dr_2 = 3$ cm.

WC Shield, supported from Bottom

3-cm-thick walls

Approximate the WC as a liquid, so center tube "floats" upwards



Deformation, magnified tenfold, of horizontal steel cylinders, fixed at 6 o'clock, with annulus of 10 g/cm³ fluid;
 $r_1 = 15$ cm; $dr_1 = 3$ mm; $r_2 = 72$ cm; $dr_2 = 3$ cm.