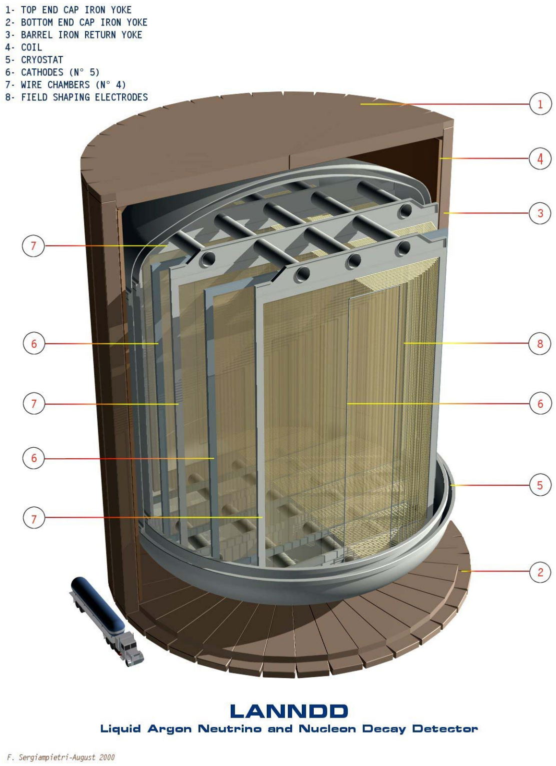
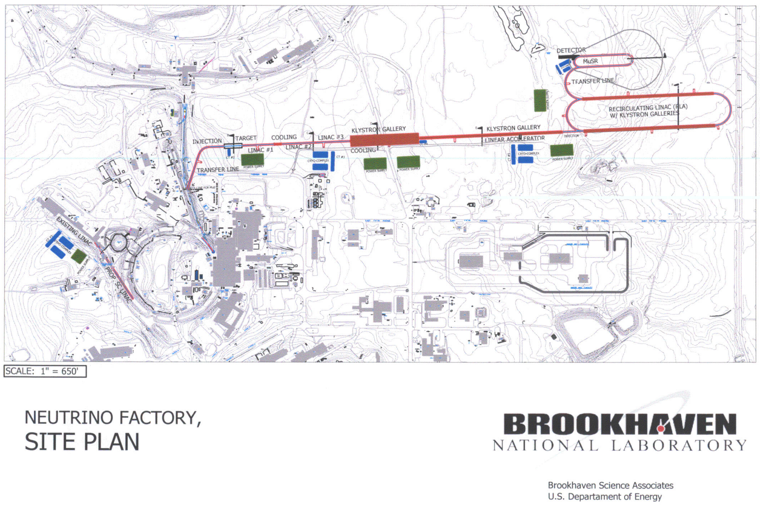
Physics with a Neutrino Superbeam





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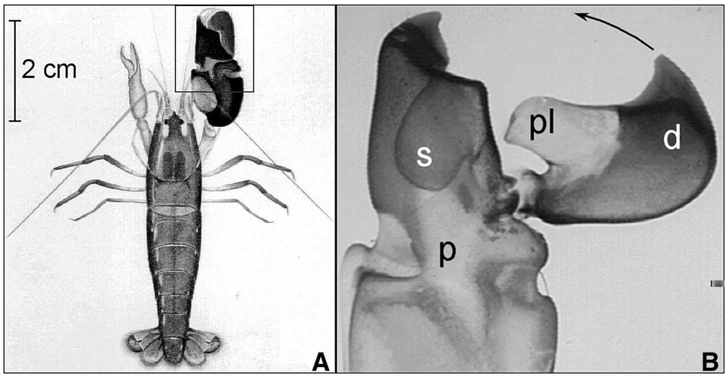
Physics Colloquium at Brookhaven National Laboratory

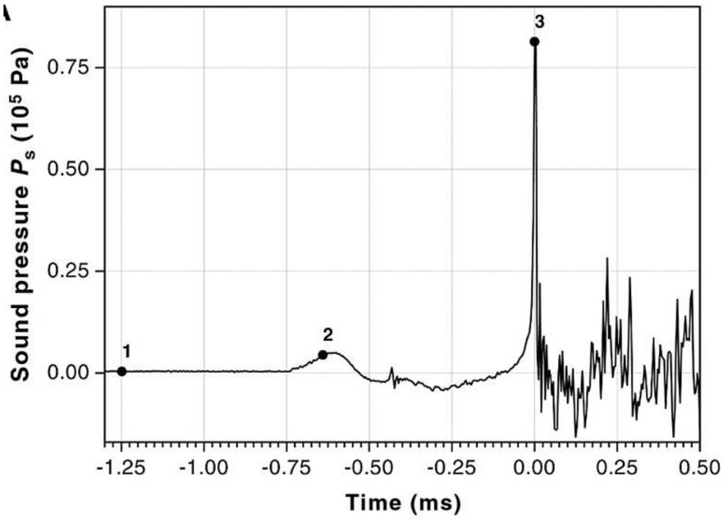
November 27, 2001

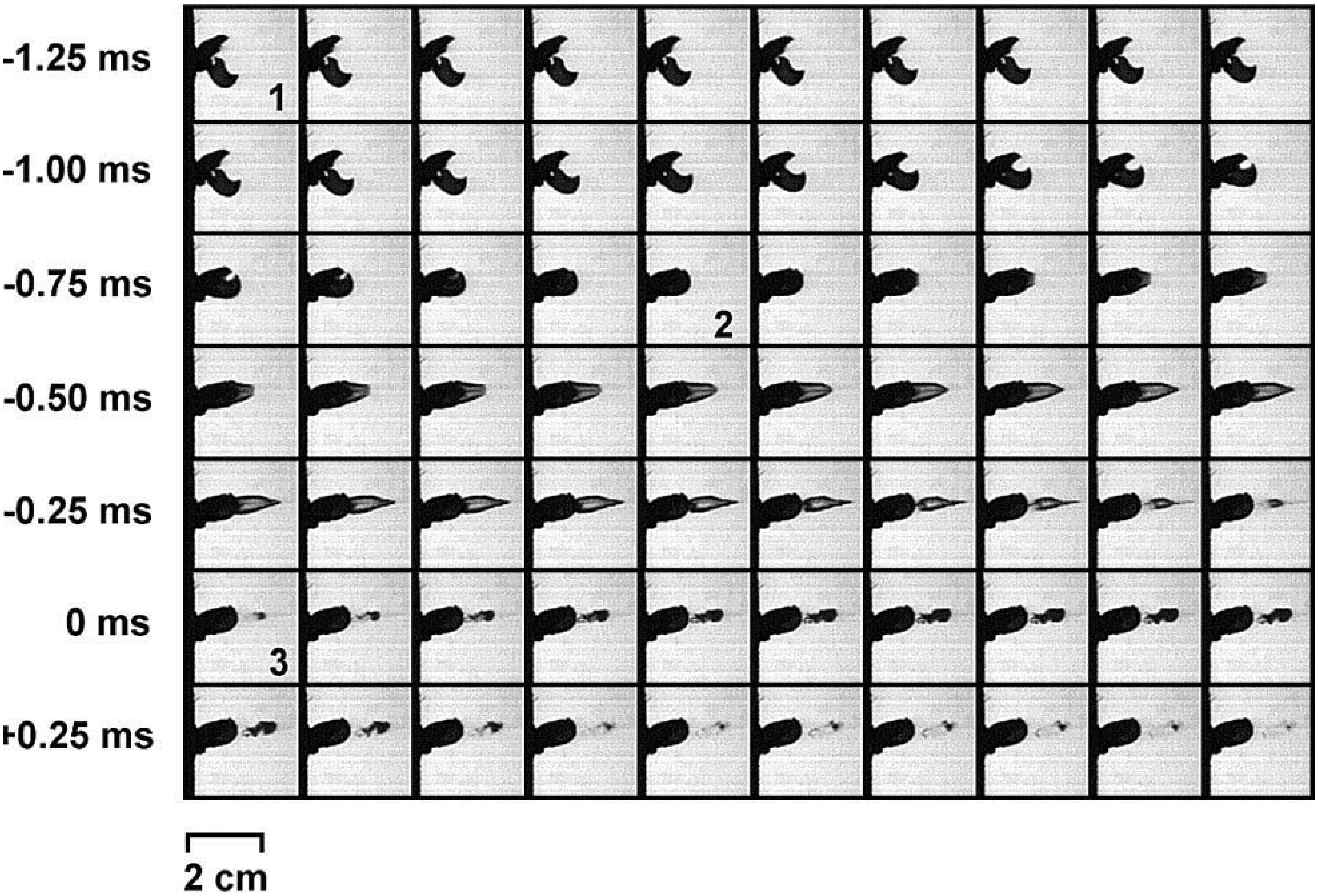
http://puhep1.princeton.edu/~mcdonald/nufact/

Snapping Shrimp Stun Their Prey with Pressure Waves from Collapsing Bubbles

M. Versluis, Science **289**, 2114 (2000).







Starting the Second Century of Neutrinos

1896 – Bequerel discovers radioactivity of uranium salts.

1899 – Rutherford identifies α and β radioactivity.

1914-1927 – Chadwick: the β energy spectrum is continuous.

1933 – Pauli: β decay involves a neutrino, $n \to p + e + \overline{\nu}_e$.

1934 – Fermi: theory of β decay with very light neutrinos.

1956 – Cowan and Reines detect the $\overline{\nu}_e$ via $\overline{\nu}_e + p \to e^+ + n$.

1957 – Pontecorvo: ν_e could oscillate into ν_μ.

1962 – Lederman, Schwartz and Steinberger detect the ν_μ.

1968 – Davis reports the first solar neutrino (ν_e) "deficit".

1976 – Perl *et al.* discover the τ lepton; ν_τ is presumed to exist.

1990 – Γ_{Z^0} measured at LEP, $\Rightarrow$ only 3 light, SM neutrinos.

1998 – Superkamiokande: ν_μ's disappear over Earth distances.

2001 – SNO: Solar neutrino deficit due to neutrino oscillations.

There are 3 known types of neutrinos, ν_e, ν_μ, and ν_τ, which are partners to the three charged leptons e, μ, and τ.

Oscillations of Massive Neutrinos

Neutrinos could have a small mass (Pauli, Fermi, Majorana, 1930's).

Massive neutrinos can mix (Pontecorvo, 1957).

In the example of only two massive neutrinos (that don't decay), with mass eigenstates ν_1 and ν_2 with mass difference Δm and mixing angle θ, the flavor eigenstates ν_a and ν_b are related by

$$\begin{pmatrix} \nu_a \\ \nu_b \end{pmatrix} = \begin{pmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \end{pmatrix}.$$

The probability that a neutrino of flavor ν_a and energy E appears as flavor ν_b after traversing distance L in vacuum is

$$P(\nu_a \to \nu_b) = \sin^2 2\theta \sin^2 \left(\frac{1.27 \Delta m^2[\mathrm{eV}^2]\ L[\mathrm{km}]}{E[\mathrm{GeV}]} \right).$$

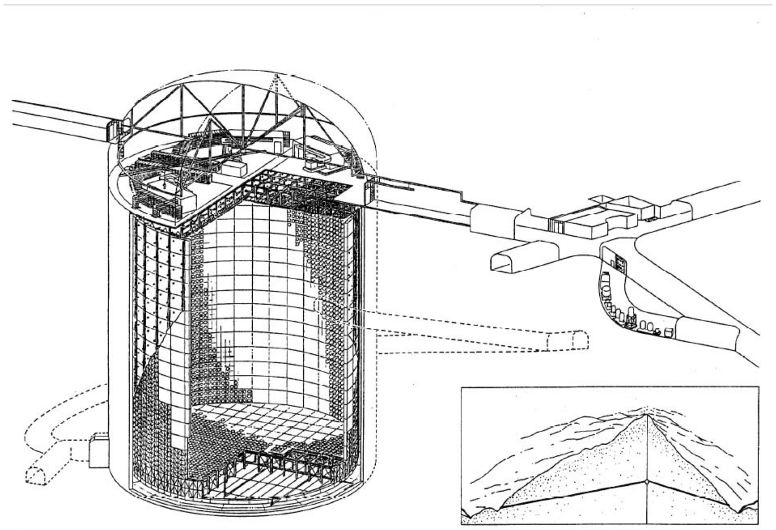
The probability that ν_a does not disappear is

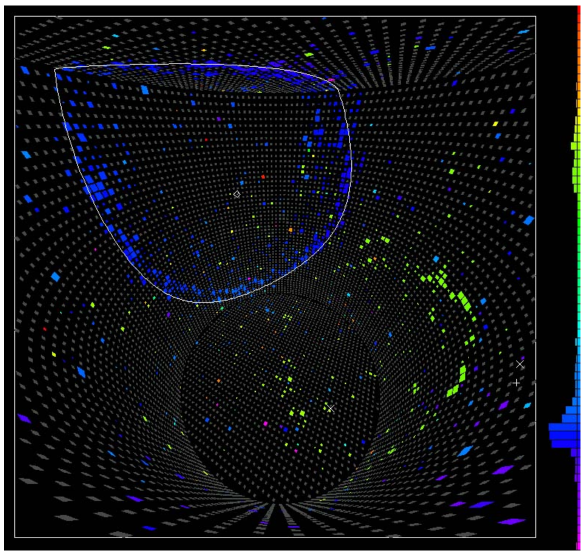
$$P(\nu_a \to \nu_a) = 1 - P(\nu_a \to \nu_b),$$

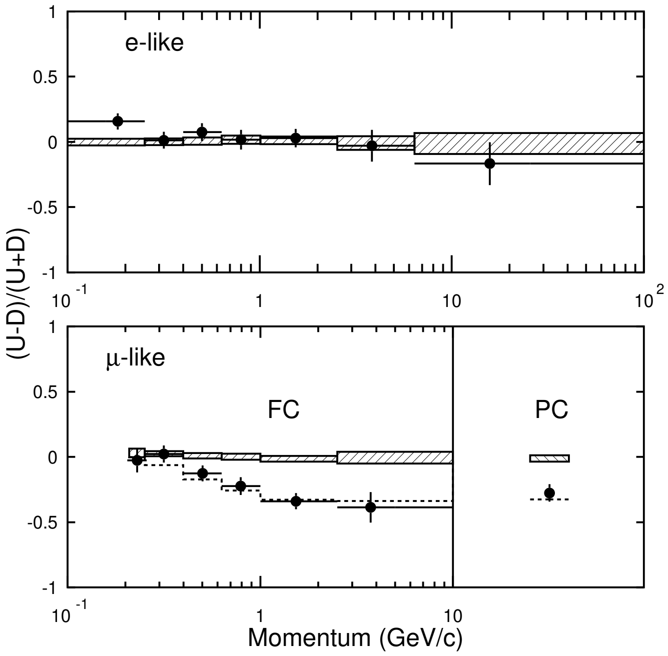
since we presume that neutrinos do not decay.

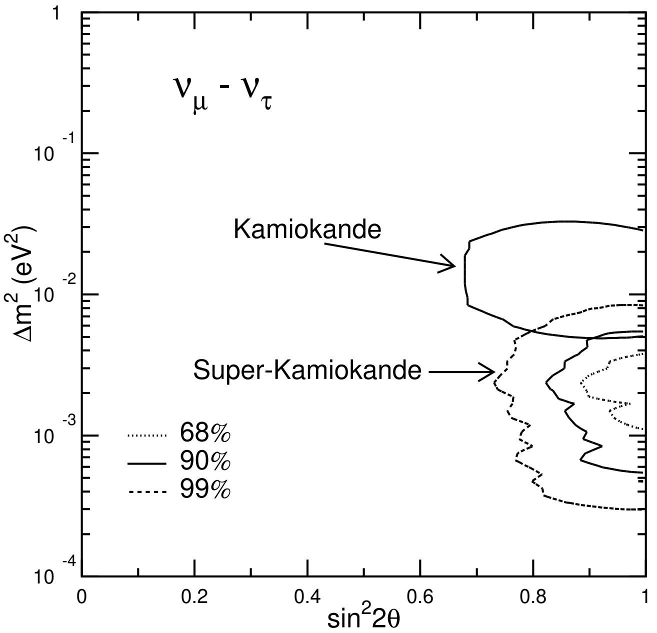
A Sketch of Current Data

- The **Atmospheric Neutrino "Anomaly"** suggests that GeV ν_μ's (from $p+N_2 \to \pi \to \mu\nu_\mu$) disappear while traversing the Earth's diameter, $\Rightarrow \Delta m^2 \approx 10^{-3}$ $(\mathrm{eV})^2$ for $\sin^2 2\theta \approx 1$. (Kamiokande, IMB, Soudan-2, MACRO, Super-Kamiokande)

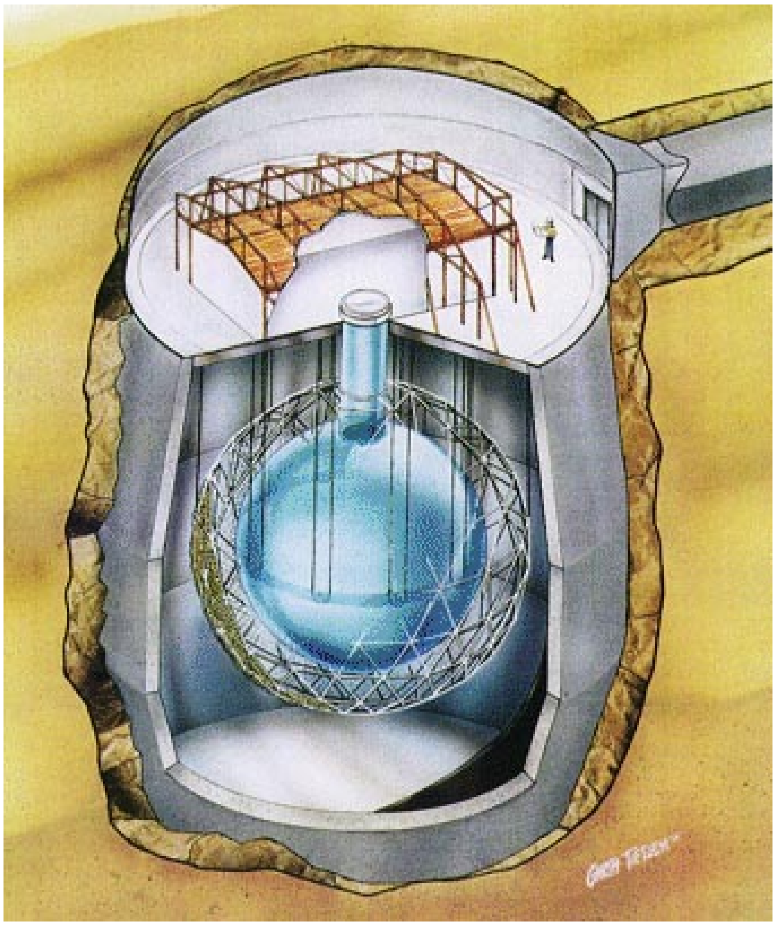


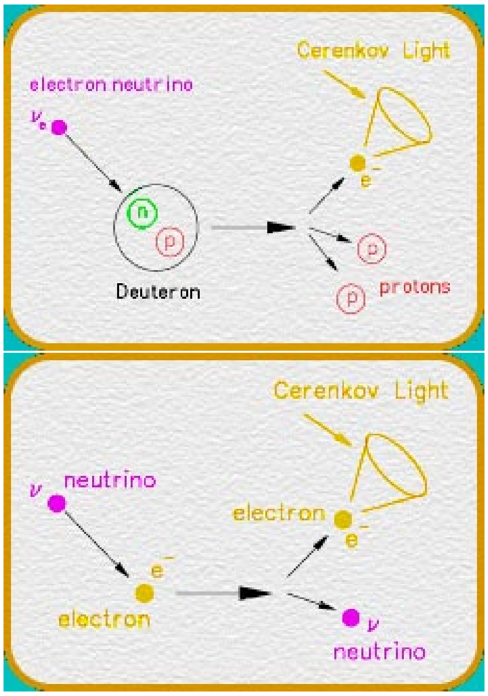






- **SNO** uses deuterium to study **Solar Neutrinos**.





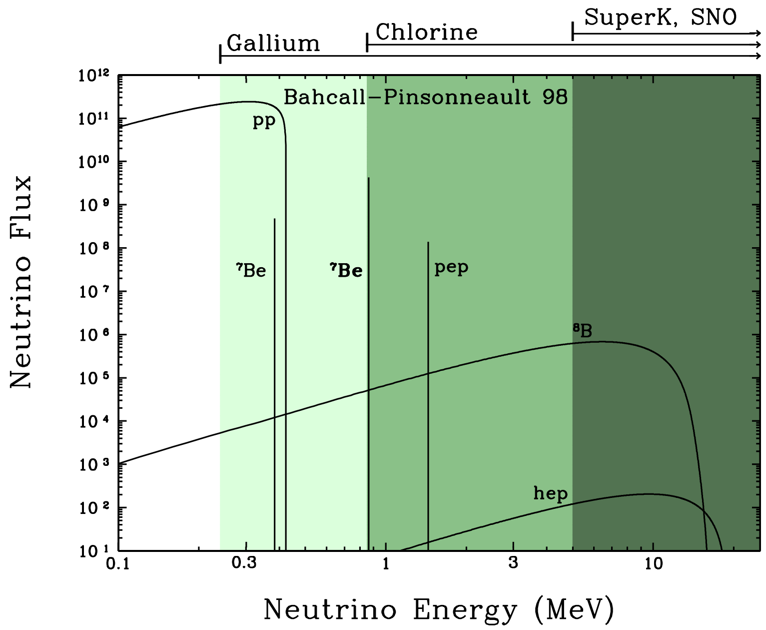
Only electron neutrinos can cause $\nu + d \to p + p + e$.

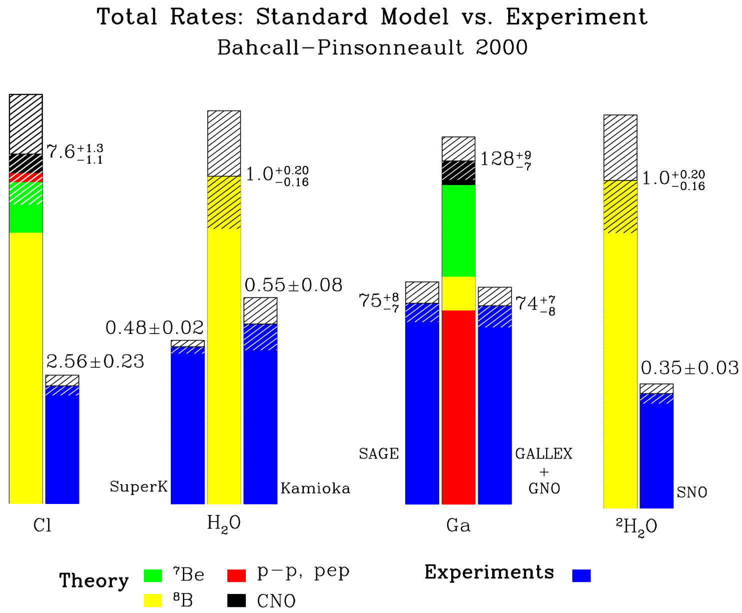
But any neutrino can cause $\nu + e \to \nu + e$.

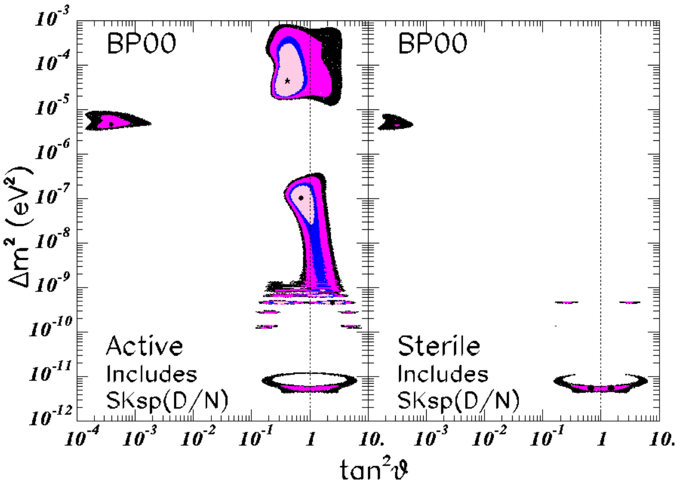
SNO observes Rate$(\nu + d \to p + p + e) \approx 0.75 \pm 0.05$ of Rate$(\nu + e \to \nu + e)$ seen by SuperK.

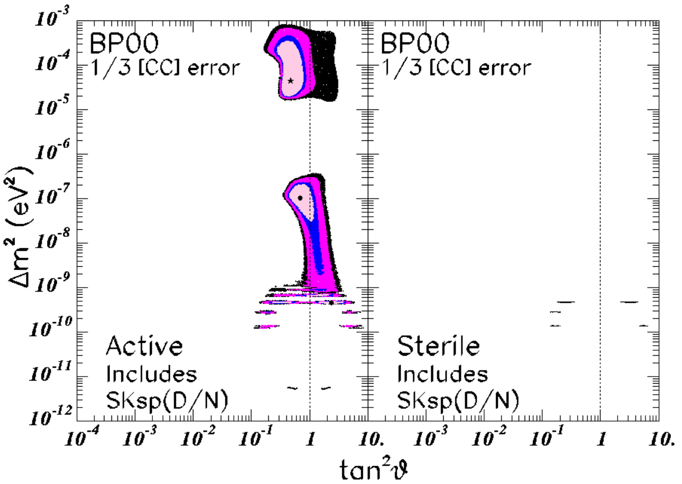
$\Rightarrow$ 25% of electron neutrinos change into another type of neutrino between the Sun and the Earth.

- The **Solar Neutrino "Deficit"** suggests that MeV ν_e's disappear between the center of the Sun and the Earth.
  $\Rightarrow \Delta m^2 \approx 10^{-10}\ (\mathrm{eV})^2$ for $\sin^2 2\theta \approx 1$, if vacuum oscillations.
  (Homestake, Super-Kamiokande, GALLEX, SAGE, SNO)





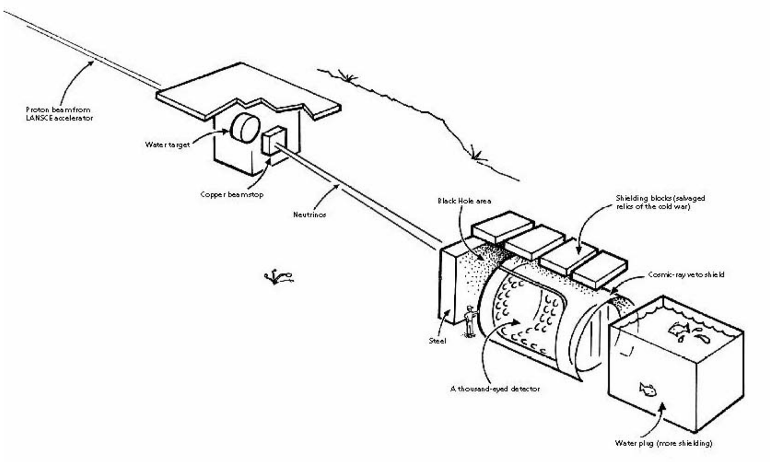


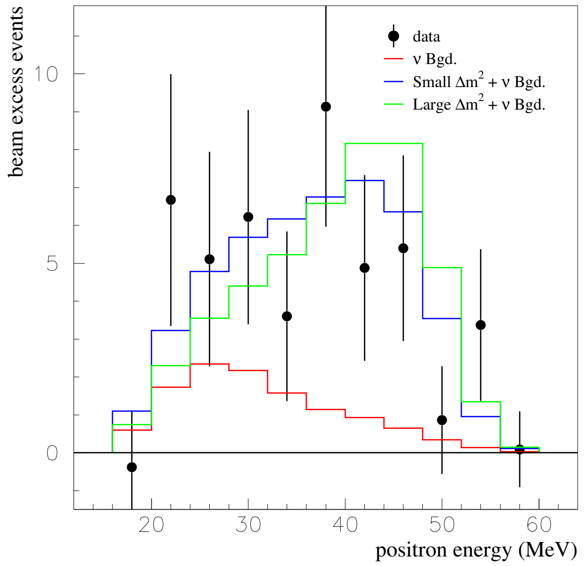


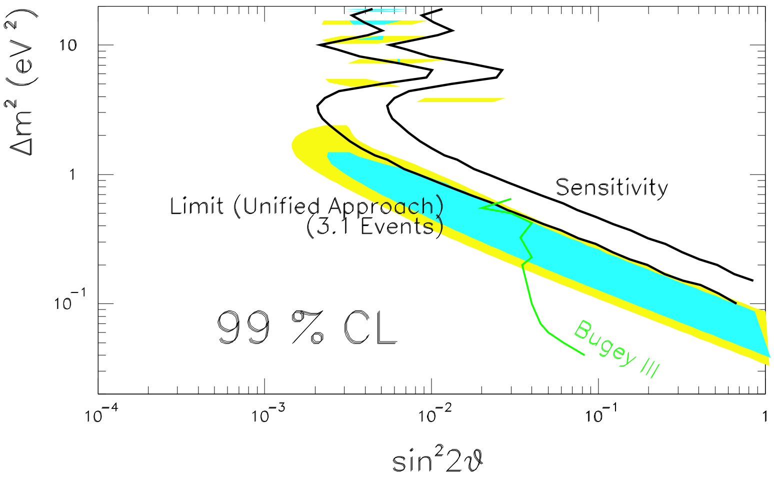
– Bahcall *et al.*, hep-ex/0106258.

Still four solutions to the solar neutrino problem
– Though sterile neutrinos seem increasingly unlikely.

- The **LSND Experiment** suggests that 30-MeV $\overline{\nu}_\mu$'s (from $p + \mathrm{H_2O} \to \pi^- \to \mu^- \overline{\nu}_\mu$) appear as $\overline{\nu}_e$'s after 30 m. $\Rightarrow \Delta m^2 \approx 1\ (\mathrm{eV})^2$, but reactor data requires $\sin^2 2\theta \lesssim 0.03$.







The atmospheric neutrino anomaly + the solar neutrino deficit (if both correct) require at least 3 massive neutrinos.

If LSND is correct as well, need at least 4 massive neutrinos.

The measured width of the Z^0 boson (LEP) $\Rightarrow$ only 3 Standard Model neutrinos. A 4th massive neutrino must be "sterile".

The Supersymmetric Seesaw

A provocative conjecture is that neutrino mass m_ν is coupled to two other mass scales, m_I (intermediate) and m_H (heavy), according to

$$m_\nu = \frac{M_I^2}{M_H}.$$

(Gell-Mann, Ramond, Slansky, 1979)

A particularly suggestive variant takes $m_I = \langle \phi_{\text{Higgs}} \rangle = 250$ GeV; Then

$m_\nu \approx \sqrt{\Delta m^2(\text{atmospheric})} \approx 0.06 \text{ eV} \Rightarrow m_H \approx 5 \times 10^{15}$ GeV.

This is perhaps the best experimental evidence for a grand unification scale, such as that underlying supersymmetric SO(10) models.

[Others interpret the need for a mass scale beyond the electroweak scale (≈ 1 TeV) as suggesting there exist large extra dimensions.]

Mixing of Three Neutrinos

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{13}s_{23}e^{i\delta} & c_{12}c_{23} - s_{12}s_{13}s_{23}e^{i\delta} & c_{13}s_{23} \\ s_{12}s_{23} - c_{12}s_{13}c_{23}e^{i\delta} & -c_{12}s_{23} - s_{12}s_{13}c_{23}e^{i\delta} & c_{13}c_{23} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

where $c_{12} = \cos\theta_{12}$, *etc.* [Maki, Nakagawa, Sakata, 2×2 form, 1962; Lee & Shrock, 3×3 form, 1977].

Three massive neutrinos $\Rightarrow$ six independent parameters:

- Two differences of the squares of the neutrino masses. Ex: $\Delta m^2_{12} = \Delta m^2(\text{solar})$ and $\Delta m^2_{23} = \Delta m^2(\text{atmospheric})$.
- Three mixing angles: $\theta_{12} \overset{?}{\approx} 45°$, θ_{13}, $\theta_{23} \approx 45°$,
- A phase δ related to CP violation,
- [$J_{CP} = s_{12}s_{23}s_{31}c_{12}c_{23}c^2_{31}s_\delta$ = Jarlskog invariant.]

The MNS neutrino mixing matrix is more provocative than the CKM quark matrix; if 2 of 3 mixing angles are near 45° ($\Rightarrow$ "bimaximal" mixing), there is likely an associated symmetry.

If four massive neutrinos, then 6 mixing angles, 3 phases, 3 independent squares of mass differences.

Matter Effects

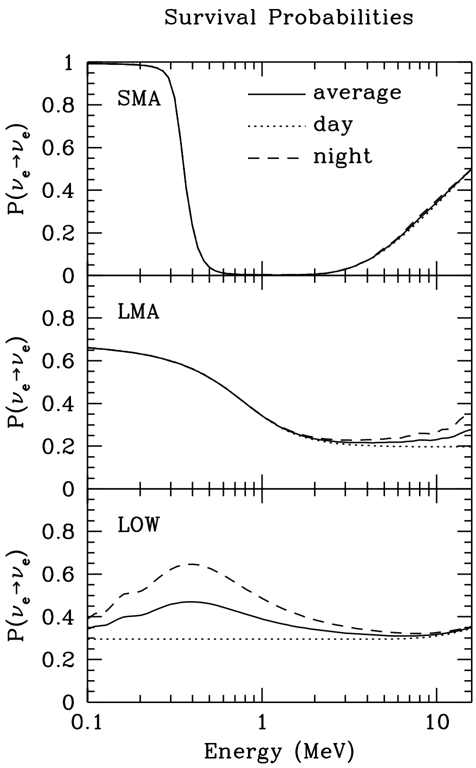
ν_e's can interact with electrons via both W and Z^0 exchanges, but other neutrinos can only interact with e's via Z^0 exchange.

$$\Rightarrow \sin^2 2\theta_{\rm matter} = \frac{\sin^2 2\theta_{\rm vac}}{\sin^2 2\theta_{\rm vac} + (\cos 2\theta_{\rm vac} - A)^2},$$

where $A = 2\sqrt{2} G_F N_e E/\Delta m^2$ depends on sign of Δm^2.

At the "resonance", $\cos 2\theta_{\rm vac} = A$, $\sin^2 2\theta_{\rm matter} = 1$ even if $\sin^2 2\theta_{\rm vac}$ is small (Wolfenstein, 1978, Mikheyev, Smirnov, 1986).

$\Rightarrow$ 3 MSW solutions to the solar neutrino problem:



In any of these MSW solutions, $\Delta m^2_{\rm solar} > 0$.

Too Many Solutions

There are 8 scenarios suggested by present data:

- Either 3 or 4 massive neutrinos.
- Four solutions to the solar neutrino problem:
  1. Vacuum oscillation (VO, or "Just So") solution;
     $\Delta m_{12}^2 \approx (0.5 - 5.0) \times 10^{-10}$ eV^2, $\sin^2 2\theta_{12} \approx (0.7 - 1.0)$.
  2. Low MSW solution;
     $\Delta m_{12}^2 \approx (0.5 - 2.0) \times 10^{-7}$ eV^2, $\sin^2 2\theta_{12} \approx (0.9 - 1.0)$.
  3. Small mixing angle (SMA) MSW solution;
     $\Delta m_{12}^2 \approx (4.0 - 9.0) \times 10^{-6}$ eV^2, $\sin^2 2\theta_{12} \approx (0.001 - 0.01)$.
  4. **Large mixing angle (LMA) MSW solution**;
     $\Delta m_{12}^2 \approx (0.2 - 2.0) \times 10^{-4}$ eV^2, $\sin^2 \theta_{12} \approx (0.65 - 0.96)$.
- Atmospheric neutrino data $\Rightarrow \Delta m_{23}^2 \approx (3 - 5) \times 10^{-3}$ eV^2, $\sin^2 \theta_{12} > 0.8$.
- θ_{13} very poorly known; δ completely unknown.

SO(10) Fit to CKM and MNS Matrices

[Albright and Barr, P.R. D **64**, 073010 (2001), hep-ph/0110259, Albright and Geer, hep-ph/0108070.]

12 Input parameters:

$$M_U \simeq 113 \text{ GeV}, \quad M_D \simeq 1 \text{ GeV}, \quad \Lambda_R = 2.4 \times 10^{14} \text{ GeV},$$
$$\sigma = 1.78, \qquad \epsilon = 0.145, \qquad \delta = 0.0086,$$
$$\delta' = 0.0079, \qquad \phi = 126^\circ, \qquad \eta = 8 \times 10^{-6},$$
$$1 < a' < 2.4, \qquad |\phi'| < 75^\circ, \qquad 1.8 < b = c < 5.2,$$

28 Fitted Parameters (LMA Solution):

$$m_t = 165 \text{ GeV}, \qquad m_c = 1.23 \text{ GeV}, \qquad m_u = 4.5 \text{ MeV},$$
$$m_b = 4.25 \text{ GeV}, \qquad m_s = 148 \text{ MeV}, \qquad m_d = 7.9 \text{ MeV},$$
$$V_{us} = 0.220, \qquad V_{cb} = 0.0395, \qquad |V_{ub}/V_{cb}| = 0.080,$$
$$\delta_{CP,CKM} = 64^\circ, \qquad \sin 2\beta = 0.64,$$
$$m_\tau = 1.777 \text{ GeV}, \qquad m_\mu = 105.7 \text{ MeV}, \qquad m_e = 0.511 \text{ MeV},$$
$$M_{R,1} = 2.8 \times 10^8 \text{ GeV}, \qquad M_{R,2} = 2.8 \times 10^8 \text{ GeV}, \qquad M_{R,3} = 2.5 \times 10^{14} \text{ GeV},$$
$$m_1 = 5.6 \times 10^{-3} \text{ eV}, \qquad m_2 = 9.8 \times 10^{-3} \text{ eV}, \qquad m_3 = 57 \times 10^{-3} \text{ eV},$$
$$\Delta m^2_{32} = 3.2 \times 10^{-3} \text{ eV}^2, \quad \Delta m^2_{21} = 0.2\text{--}2 \times 10^{-4} \text{ eV}^2, \quad |\delta_{CP,MNS}| < 50^\circ,$$
$$\sin^2 2\theta_{32} = 0.994, \qquad \sin^2 2\theta_{21} = 0.6\text{--}0.9, \qquad \sin^2 2\theta_{13} < 0.006.$$

Central values: $\sin^2 2\theta_{13} = 0.003$, $\delta_{CP,MNS} \approx 0$.

Proton Decay in SO(10) Models

[Pati, hep-ph/0106082.]

In (nonSUSY) SU(5) models, $p \to \pi^0 e^+$ is favored – but ruled out by experiment.

SUSY SU(5) has difficulty accommodating the observed data on neutrino mixing, as well as the proton decay limits.

In SUSY SO(10) models, $p \to \bar{\nu} K^+$ is favored relative to $p \to \pi^0 e^+$, with $\tau_p \approx 10^{31}$ years in MSSM, and $\tau_p \approx 10^{33-34}$ years in ESSM.

Implications for Experiment

Future studies of neutrino mixing should include good capability to study $p \to \bar{\nu} K^+$.

Studies of CP violation in neutrino mixing require lepton charge identification: both $\mu^\pm$ and $e^\pm$ desirable.

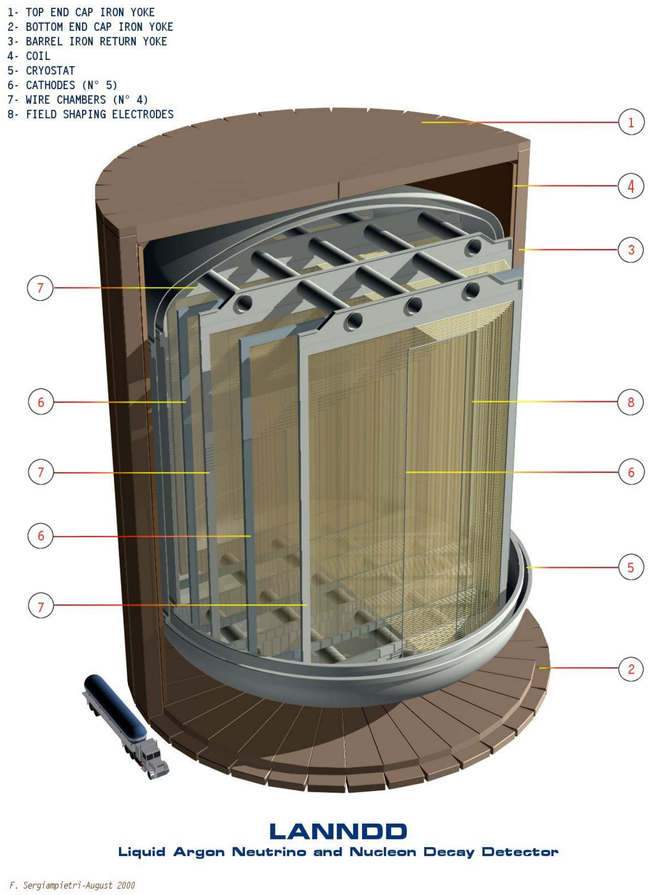
$\Rightarrow$ Water Čerenkov, Iron-Scintillator, and Liquid Scintillator detectors disfavored.

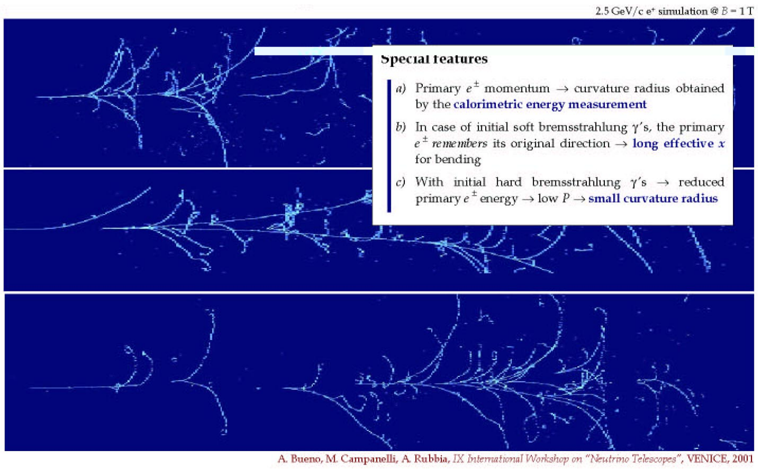
$\Rightarrow$ **Magnetized Liquid Argon** is the most flexible option.

LANNDD – A Magnetized Liquid Argon Detector

Use a magnetized detector to distinguish ν_μ from $\bar{\nu}_\mu$ via sign of $\mu^\pm$ produced.

Use a magnetized liquid argon detector to distinguish ν_e from $\bar{\nu}_e$ via sign of $e^\pm$ produced.

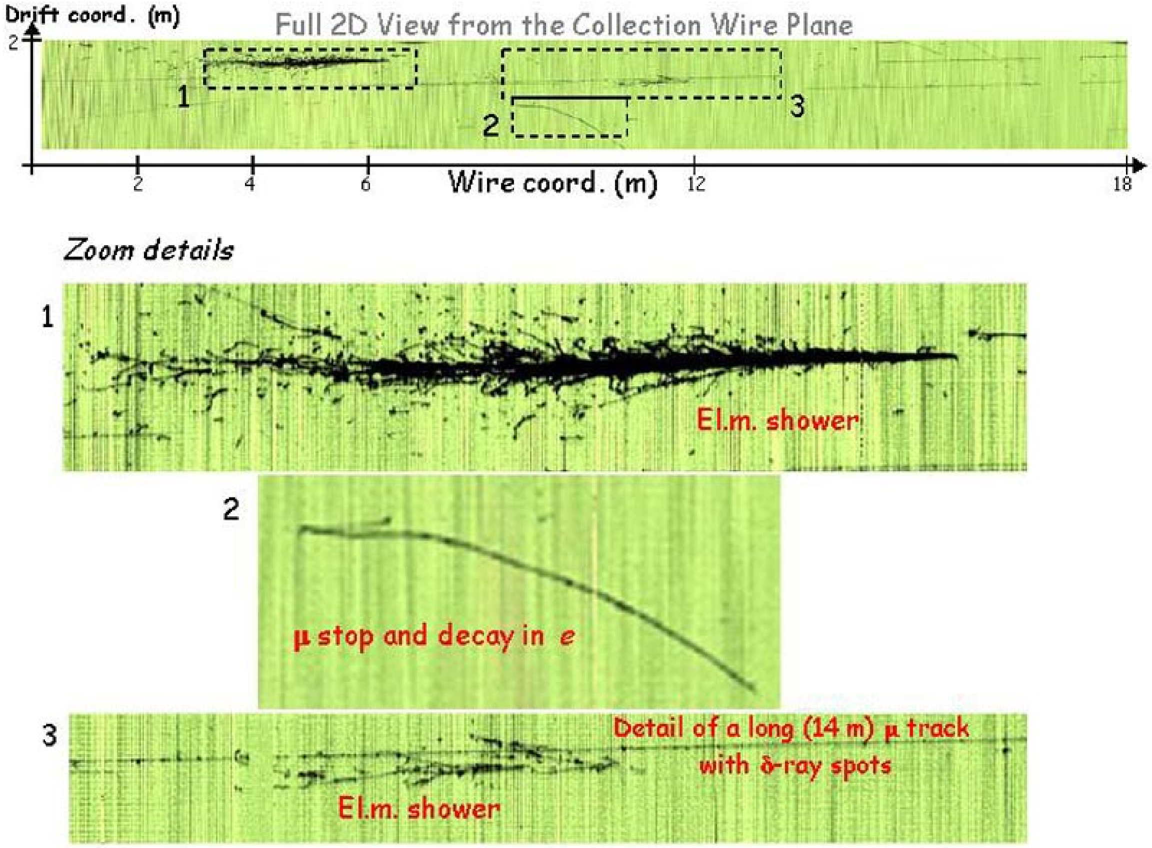


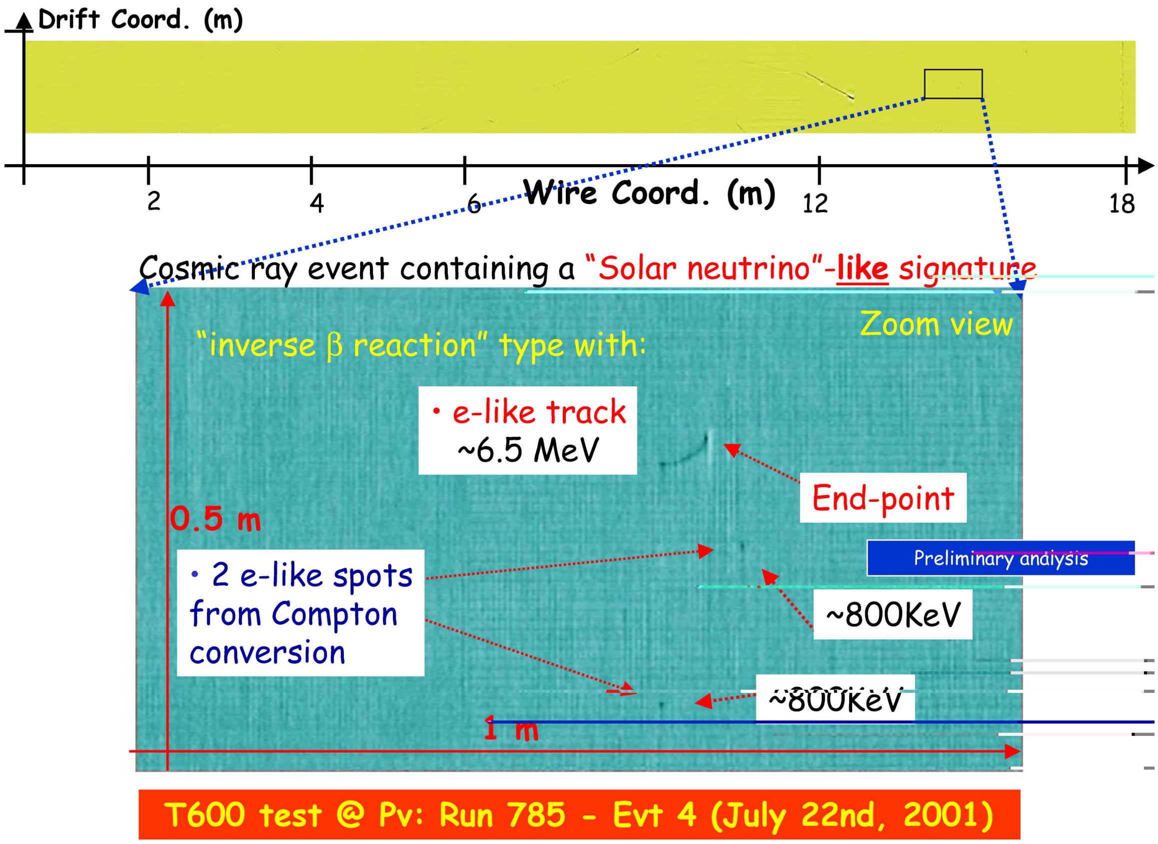


Need detector mass of ≈ 100 kton for competitive neutrino physics.

A liquid argon detector has good sensitivity to $p \to \nu K^+$ $\Rightarrow$ 100 kton of LAr is competitive with 1 Mton of water for proton decay.

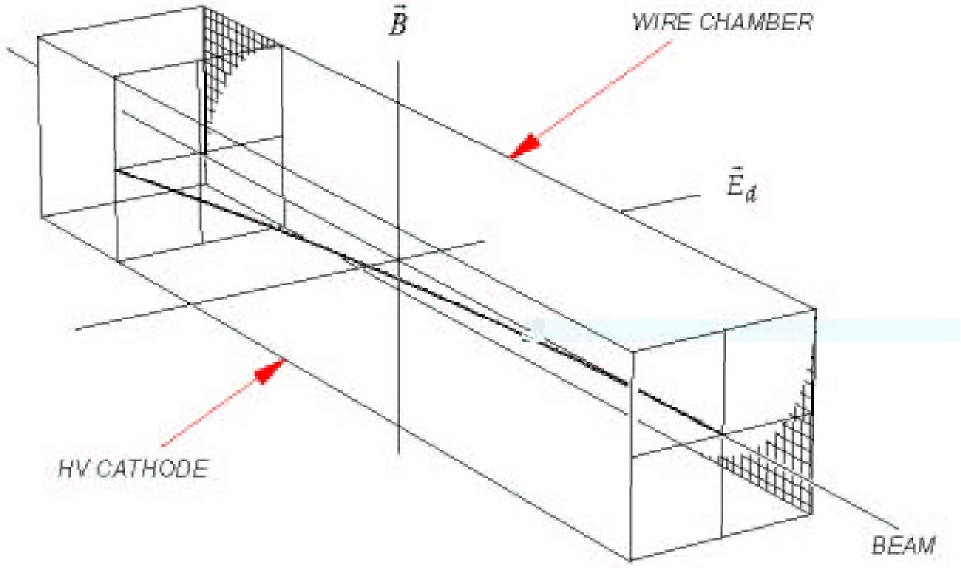
ICARUS – 300 Ton Liquid Argon Module

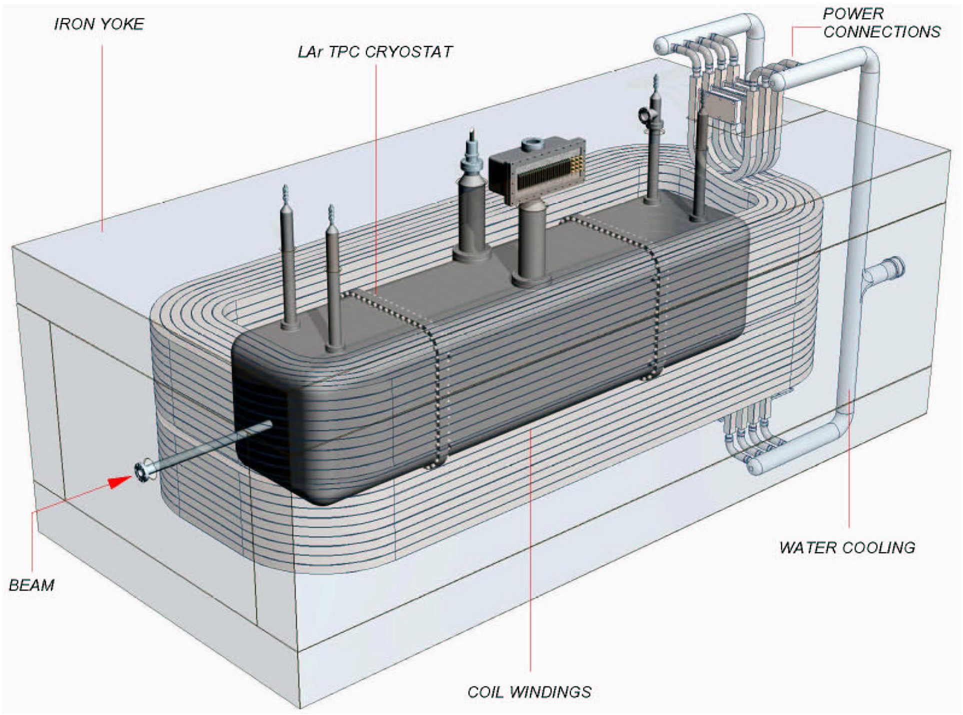




Demonstration of Electron Sign Determination

Study electromagnetic showers or 0.5-10 GeV in a liquid argon TPC 6 rad. lengths deep, ±1 rad. length wide, in magnetic field up to 1 T.





The BNL A3 line (Neutrino Factory Test Beam) is well suited to such a study.

The Next Generation of Neutrino Experiments

- Short baseline accelerator experiments (miniBoone, CERN) will likely clarify the LSND result.

- Super-Kamiokande + new long baseline accelerator experiments (K2K, Minos, NGS) will firm up measurements of θ_{23} and Δm^2_{23}, but will provide little information on θ_{13} and δ.

- New solar neutrino experiments (BOREXino, HELLAZ, HERON) will explore different portions of the energy spectrum, and clarify possible pathlength-dependent effects.

  SNO should also provide independent confirmation of neutrino oscillations via comparison of reactions
  $\nu + {}^2\mathrm{H} \to p + p + e$ and $\nu + {}^2\mathrm{H} \to p + n + \nu$.

- Reactor experiments such as KamLAND can help clarify whether the LMA solar neutrino solution is correct.

- Each of these experiments studies oscillations of only a single pair of neutrinos.

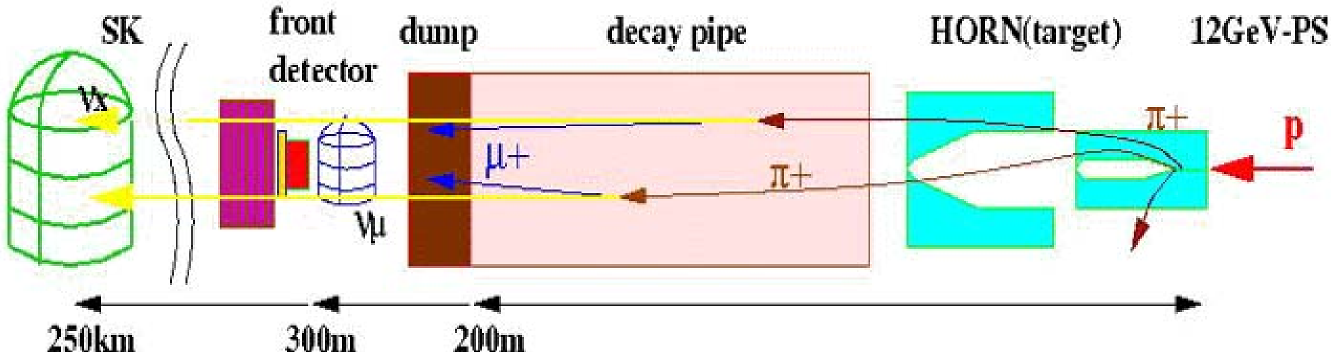
- The continued search for the neutrinoless double-beta decay ${}^{78}\mathrm{Ge} \to {}^{78}\mathrm{Se} + 2e^-$ will improve the mass limits on Majorana neutrinos to perhaps as low as 0.01 eV (hep-ex/9907040).

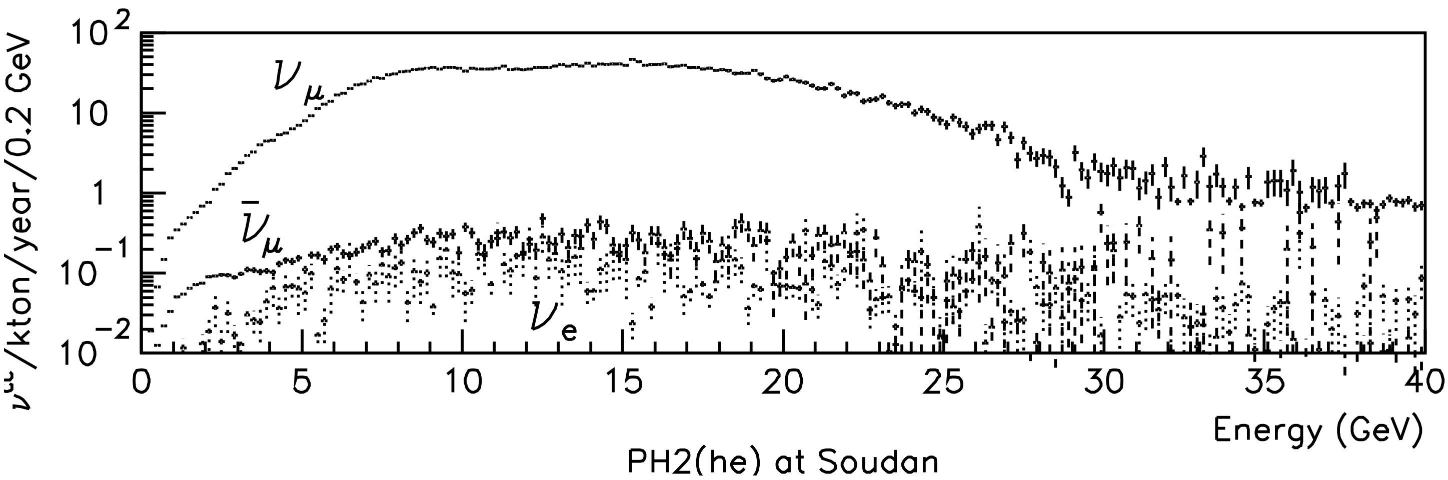
The Opportunity for a Neutrino Factory

- Many of the neutrino oscillation solutions permit study of the couplings between 2, 3, and 4 neutrinos in accelerator based experiments.

- More neutrinos are needed!

- Present neutrino beams come from $\pi, K \to \mu\nu_\mu$ with small admixtures of $\overline{\nu}_\mu$ and ν_e from μ and $K \to 3\pi$ decays.

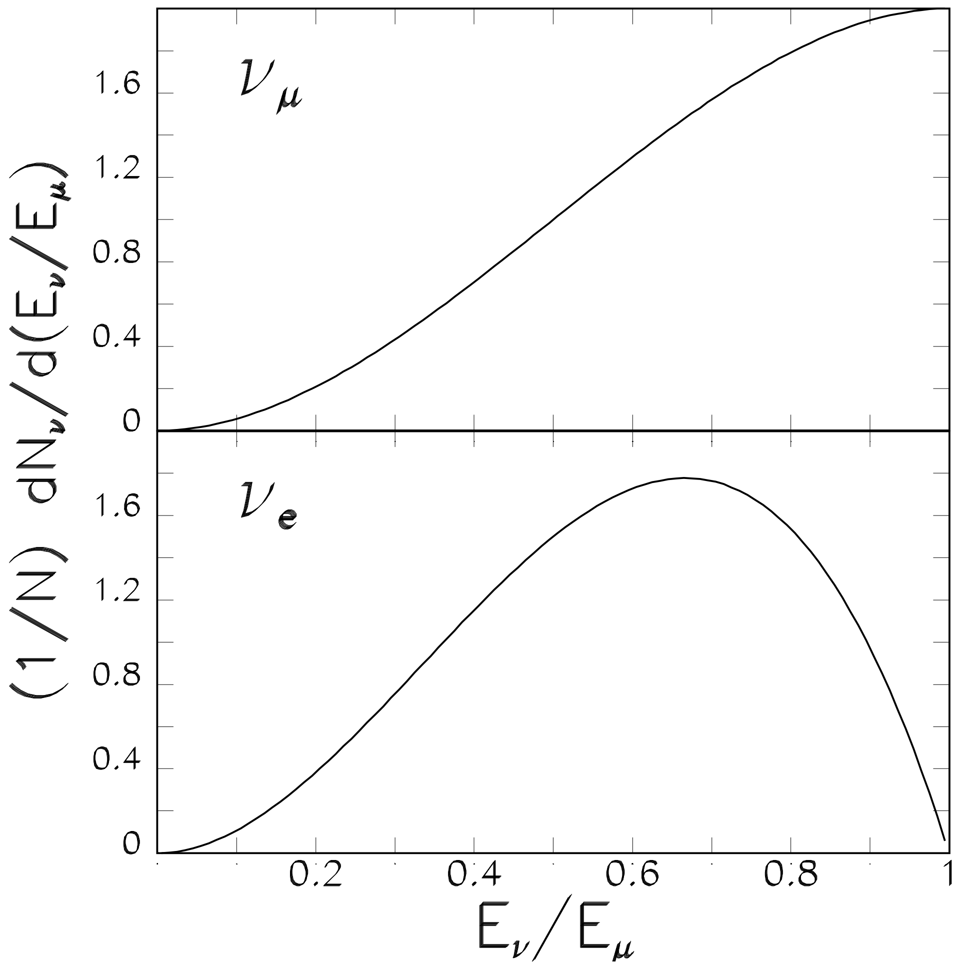




- Cleaner spectra and comparable fluxes of ν_e and ν_μ desirable.

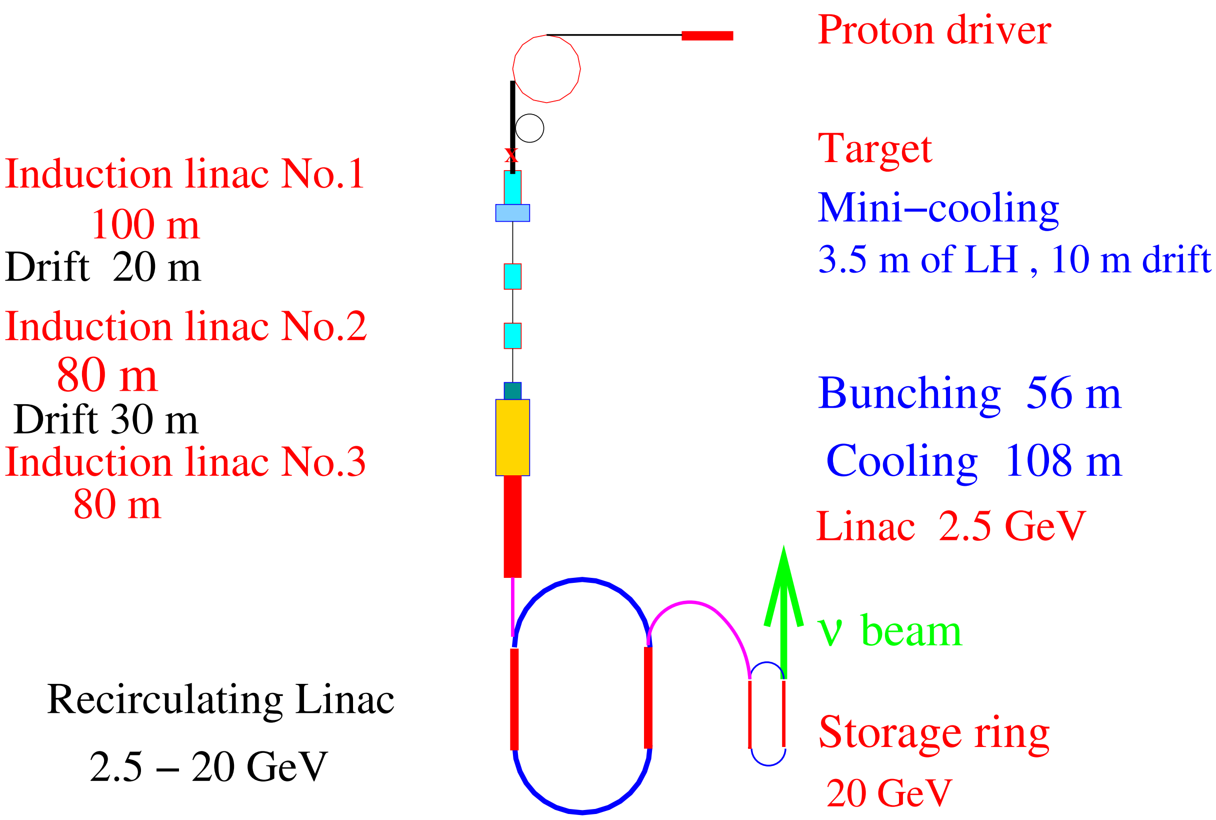
A Neutrino Factory based on a Muon Storage Ring

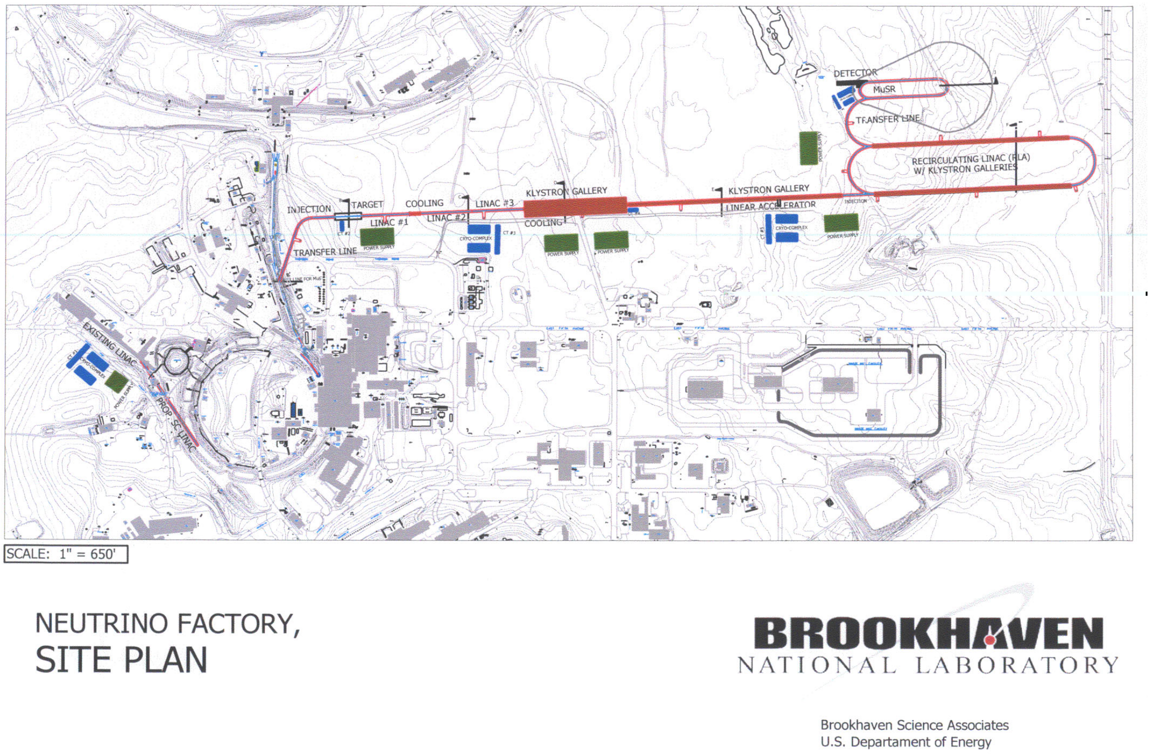
- Higher (per proton beam power) and better characterized, neutrino fluxes are obtained from μ decay.
- Collect low-energy μ's from π decay,
  Cool the muon bunch,
  Accelerate the μ's to the desired energy,
  Store them in a ring while they decay via $\mu^- \to e^- \nu_\mu \overline{\nu}_e$.
  [Of course, can use μ^+ also.]



Sketch of a Neutrino Factory

[S. Ozaki *et al.*, Neutrino Factory Feasibility Study-2 (4/01)]





6 Classes of Experiments at a Neutrino Factory

$$\nu_\mu \to \nu_e \to e^- \qquad \text{(appearance)}, \tag{1}$$

$$\nu_\mu \to \nu_\mu \to \mu^- \qquad \text{(disappearance)}, \tag{2}$$

$$\nu_\mu \to \nu_\tau \to \tau^- \qquad \text{(appearance)}, \tag{3}$$

$$\overline{\nu}_e \to \overline{\nu}_e \to e^+ \qquad \text{(disappearance)}, \tag{4}$$

$$\overline{\nu}_e \to \overline{\nu}_\mu \to \mu^+ \qquad \text{(appearance)}, \tag{5}$$

$$\overline{\nu}_e \to \overline{\nu}_\tau \to \tau^+ \qquad \text{(appearance)}. \tag{6}$$

[Plus 6 corresponding processes for $\overline{\nu}_\mu$ from μ^+ decay.]

Processes (2) and (5) are easiest to detect, via the final state μ.

Process (5) is noteworthy for having a "wrong-sign" μ.

Processes (3) and (6) with a final state τ require μ's of 10's of GeV.

Processes (1) and (4) with a final state electron are difficult to distinguish – unless use magnetized liquid argon.

Magnetic detectors of 10's of kilotons will be required, with fine segmentation if τ's are to be measured.

The Rates are High at a Neutrino Factory

Charged current event rates per kton-yr.

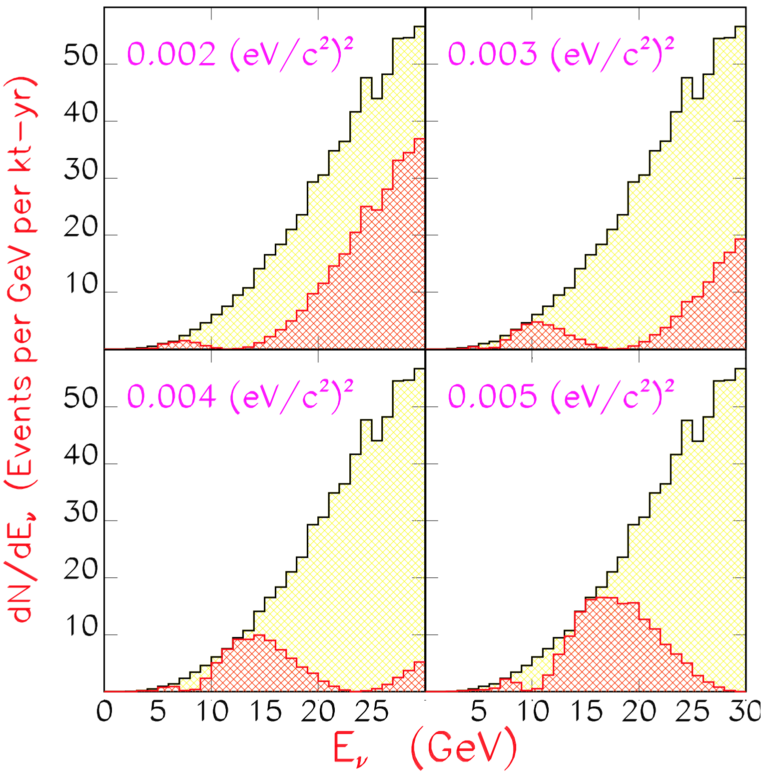
$(L = 732$ km$)$	ν_μ	$\overline{\nu}_e$
Neutrino Factory	$(2 \times 10^{20}$ $\nu_\mu/$yr$)$	
10 GeV	2200	1300
20 GeV	18,000	11,000
50 GeV	2.9×10^5	1.8×10^5
250 GeV	3.6×10^7	2.3×10^7
MINOS (WBB)		
Low energy	460	1.3
Medium energy	1440	0.9
High energy	3200	0.9

Even a low-energy neutrino factory has high rates of electron neutrino interactions.

A neutrino factory with $E_\mu \gtrsim 20$ GeV is competitive for muon neutrino interactions.

$\nu_\mu \to \ \nu_\mu \to \mu^-$ **Disappearance**

$$P(\overline{\nu}_e \to \overline{\nu}_\mu) = (\sin^2 2\theta_{23} \cos^2 \theta_{13} + \sin^2 2\theta_{13} \sin^4 \theta_{23}) \sin^2 \frac{1.27\Delta m^2_{23} L}{E_\nu}$$



(hep-ph/9906487)

$E_\mu = 30$ GeV,
2×10^{20} μ decays,
$L = 7000$ km,
$\sin^2 2\theta_{23} \approx 1 \approx \cos^2 \theta_{13}$.

Δm^2_{23} (eV^2)	Events (per 10 kton-yr)
0.002	2800
0.003	1200
0.004	900
0.005	1700
No Osc.	6200

$\nu_\mu \to \ \nu_\tau \to \tau^-$ **Appearance**

Δm^2_{23} (eV^2)	Events (per 10 kton-yr)
0.002	1200
0.003	1900
0.004	2000
0.005	1800

For conditions as above.

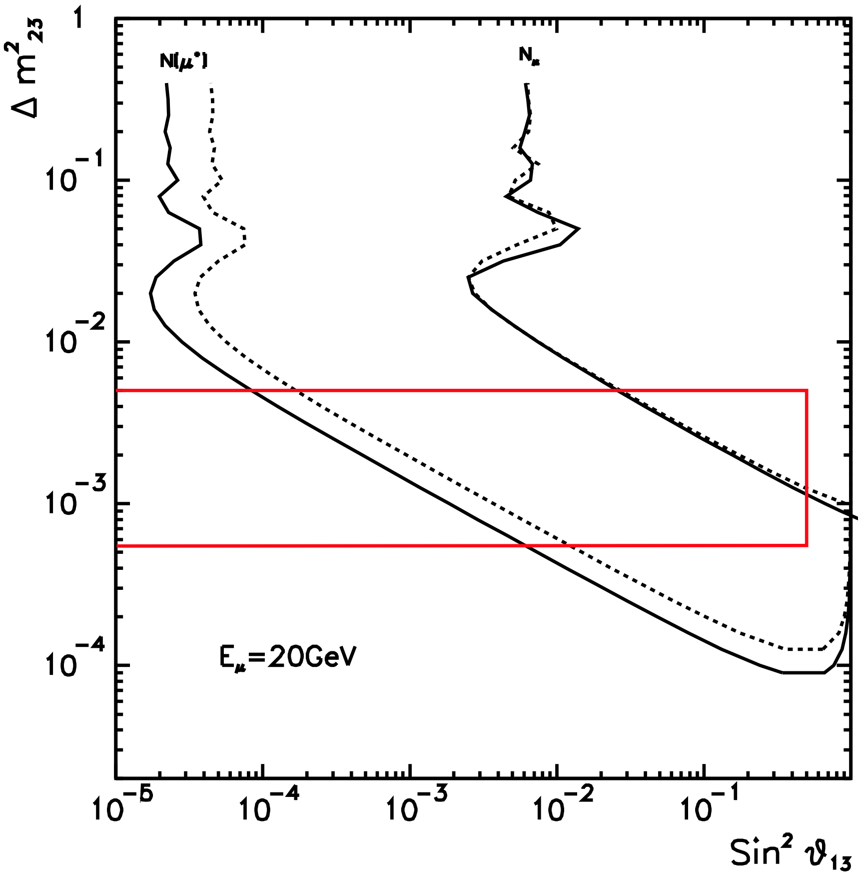
Measuring θ_{13}

Many ways:

$$P(\overline{\nu}_e \to \overline{\nu}_\mu) = \sin^2 2\theta_{13} \sin^2 \theta_{23} \sin^2 \frac{1.27\Delta m_{23}^2 L}{E_\nu},$$

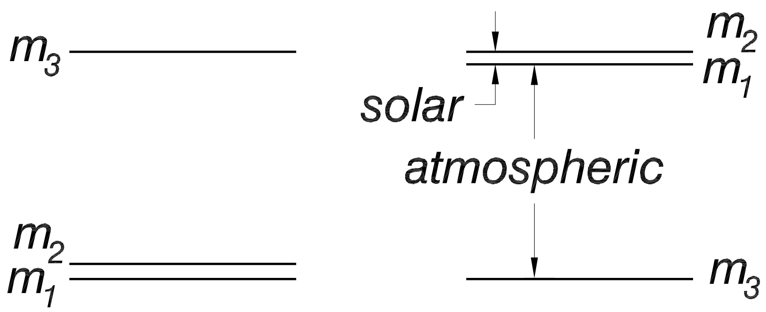
$$P(\overline{\nu}_e \to \overline{\nu}_\tau) = \sin^2 2\theta_{13} \cos^2 \theta_{23} \sin^2 \frac{1.27\Delta m_{23}^2 L}{E_\nu},$$

$$P(\nu_\mu \to \nu_\tau) = \cos^4 \theta_{13} \sin^2 2\theta_{23} \sin^2 \frac{1.27\Delta m_{23}^2 L}{E_\nu}.$$



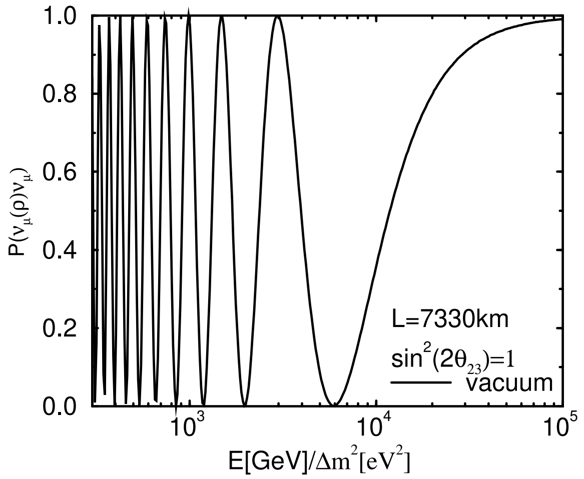
10 kton detector,
$E_\mu = 20$ GeV,
2×10^{20} μ decays,
$L = 732$ km,
$\sin^2 2\theta_{23} = 1$,
Left: $\overline{\nu}_e \to \overline{\nu}_\mu \to \mu^+$,
Right: $\nu_\mu \to \nu_\mu \to \mu^-$,
Box = presently allowed.
(hep-ph/9811390).

Measuring the Sign of Δm^2_{23} via Matter Effects

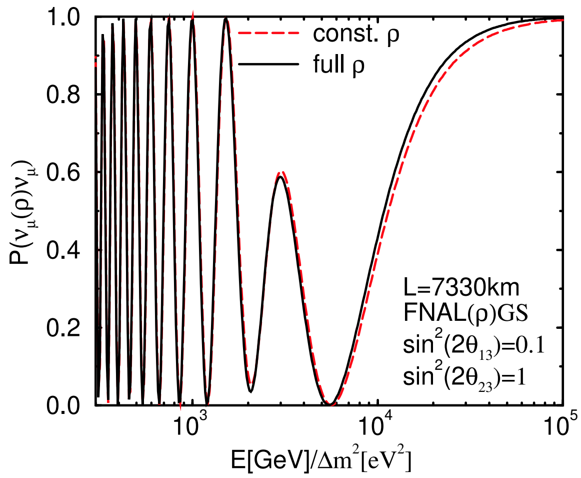


The matter effect resonance depends on the sign of Δm^2 (p. 11).

Large effect of Δm^2_{23} in ν_μ (disappearance) if $\sin^2 2\theta_{13} \approx 0.1$.

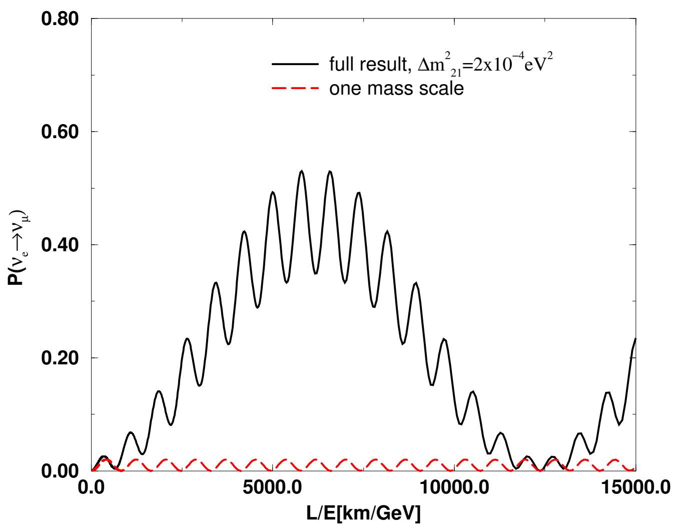


(hep-ph/ 9910554)



For smaller $\sin^2 2\theta_{13}$, may be better to use $\overline{\nu}_e \to \overline{\nu}_\mu$ (appearance).

Effect of Δm^2_{12} can be prominent in some cases. (hep-ph/0106139)



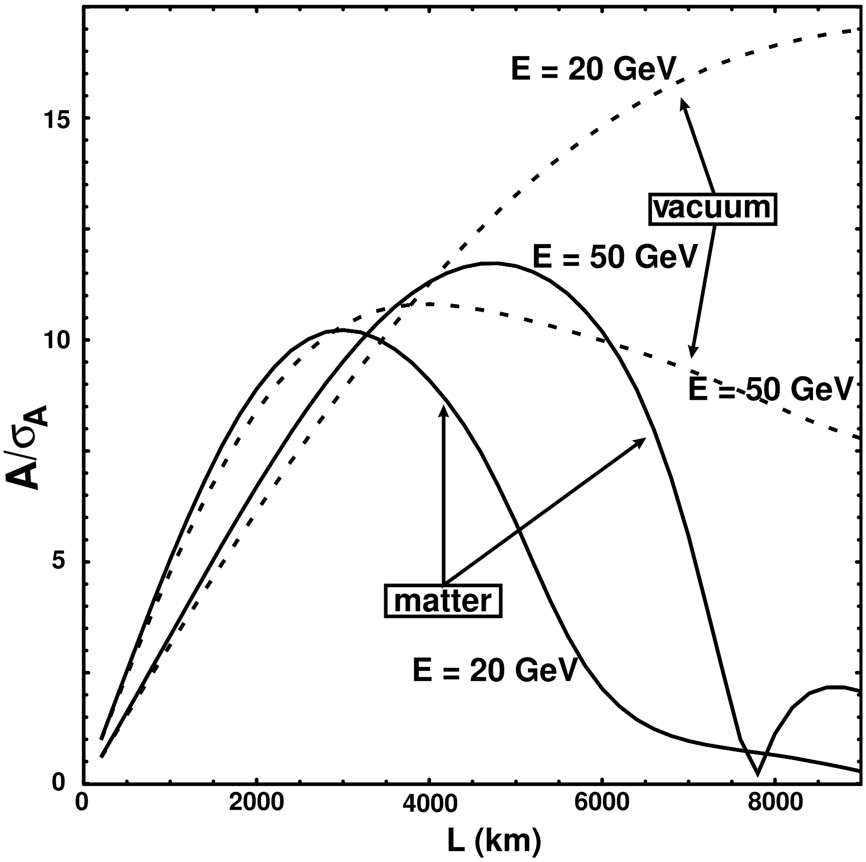
Measuring δ via CP Violation

The phase δ is accessible to terrestrial experiment in the large mixing angle (LMA) solution to the solar neutrino problem (or if there are 4 massive neutrinos).

CP violation:

$$A_{\mathrm{CP}} = \frac{P(\nu_e \to \nu_\mu) - P(\overline{\nu}_e \to \overline{\nu}_\mu)}{P(\nu_e \to \nu_\mu) + P(\overline{\nu}_e \to \overline{\nu}_\mu)} \approx \left| \frac{2 \sin\delta}{\sin 2\theta_{13}} \sin \frac{1.27 \Delta m^2_{12} L}{E} \right| ,$$

assuming $\sin^2 2\theta_{12} \approx \sin^2 2\theta_{23} \approx 1$ (LMA).



10 kton detector,
2×10^{21} muon decays,
Large angle MSW:
$\Delta m^2_{12} = 10^{-4}$ eV^2,
$\Delta m^2_{23} = 2.8 \times 10^{-3}$ eV^2,
$\theta_{12} = 22.5°$,
$\theta_{13} = 13°$,
$\theta_{23} = 45°$,
$\delta = -90°$.
(hep-ph/9909254)

Matter effects dominate the asymmetry for $L > 1000$ km.

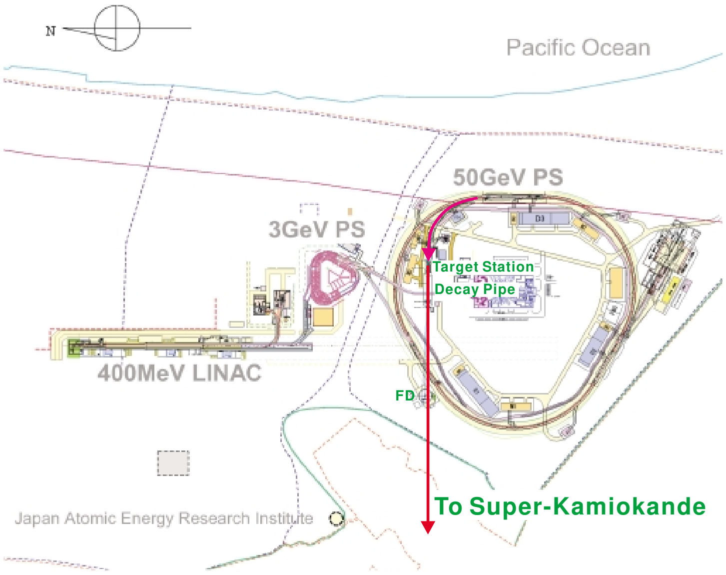
Before a Neutrino Factory – a Neutrino Superbeam

Many technical challenges remain for a neutrino factory
$\Rightarrow$ Costly in both money and time.

Results of neutrino factory R&D strongly encourage use of 1-4 MW target stations to produce future neutrino (and muon) beams.

Success of the SuperK detector encourages construction of neutrino detectors of $\approx$ 100 kton mass.

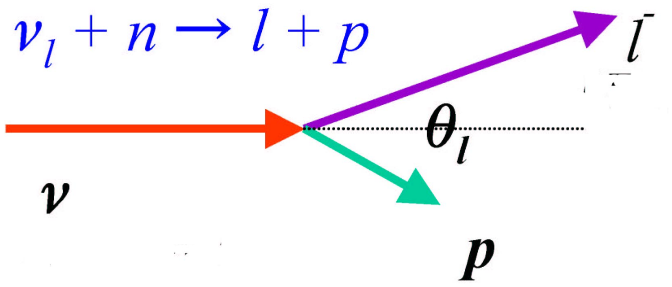
The Japanese are well positioned to follow this path, using SuperK + a neutrino beam from the JHF 0.7-MW, 50-GeV proton source recently approved (hep-ex/0106019).

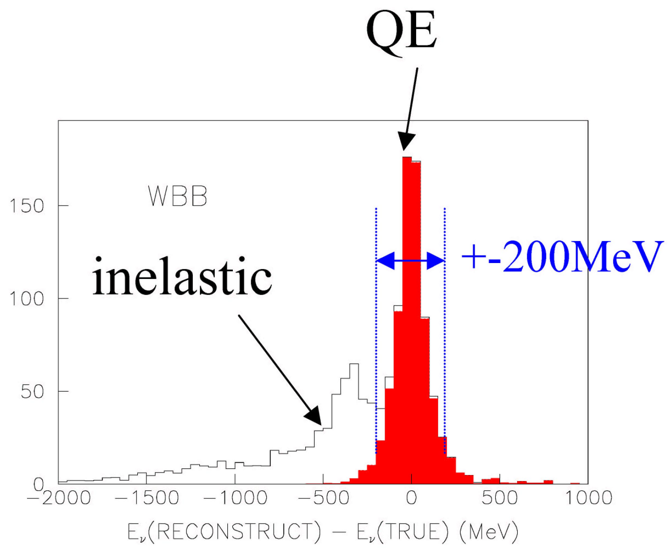


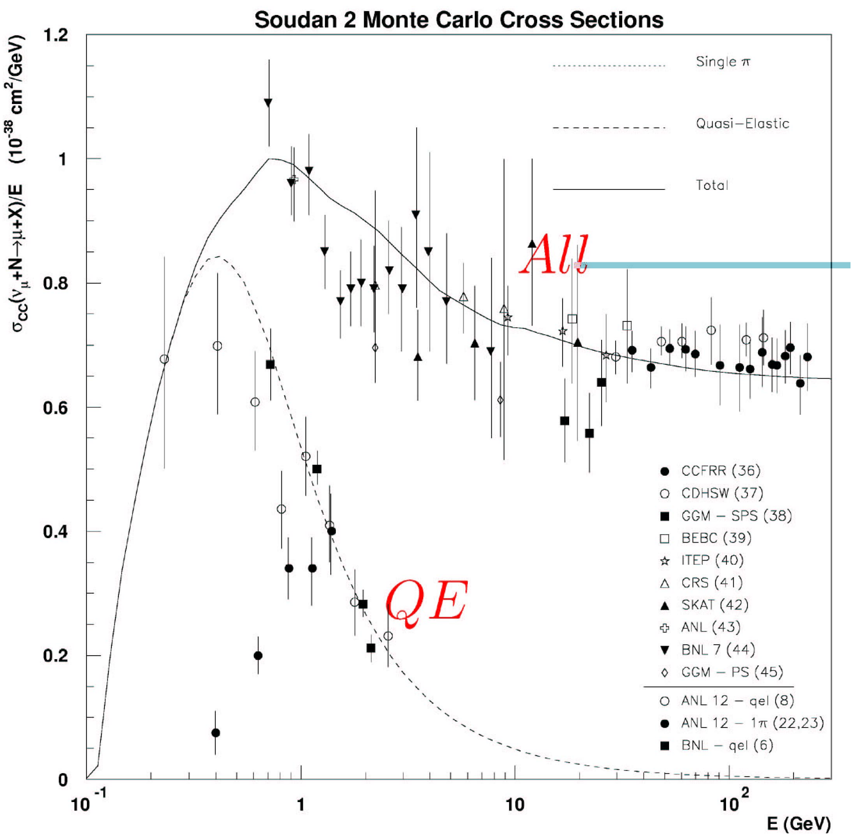
Superbeam Strategy, I

Use $\approx$ 1 GeV neutrinos: Production rate is high;

Interactions are simple $\leftrightarrow$ quasielastic (no pions).



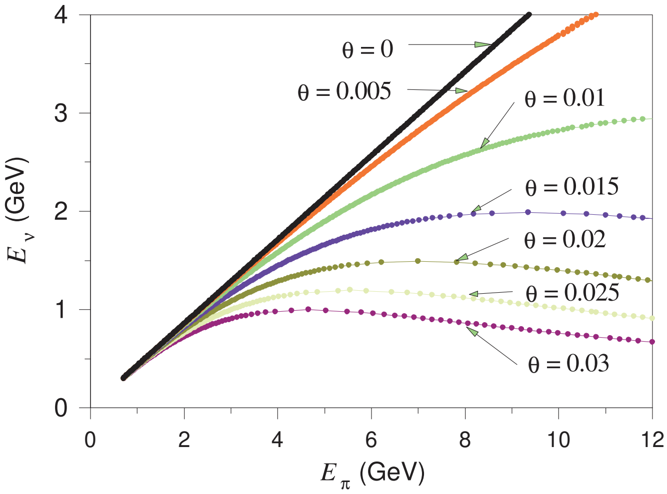


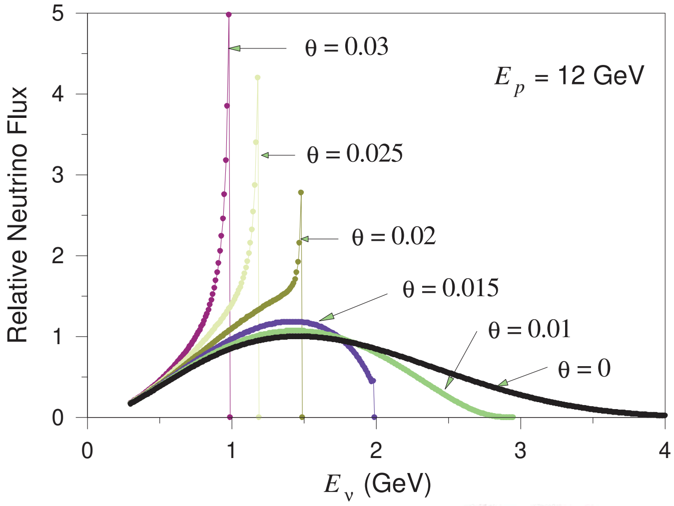


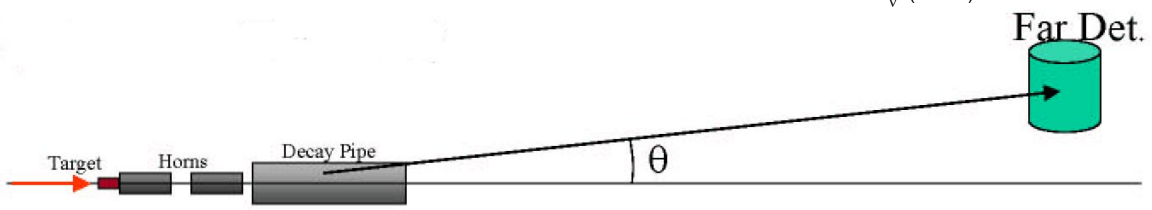
Superbeam Strategy, II

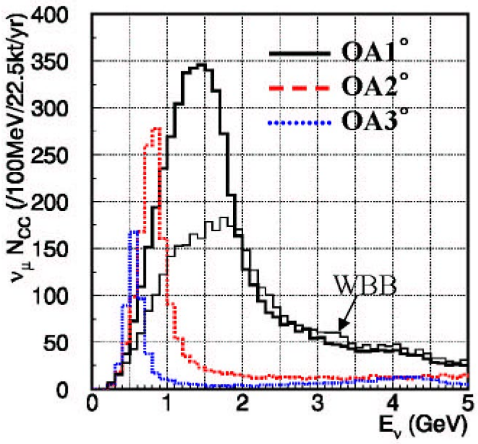
Use an **off-axis** neutrino beam (BNL E-889).

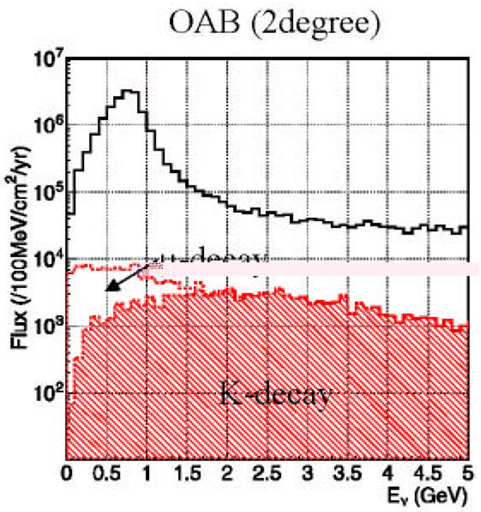
$\pi \to \mu\nu$ decay kinematics has a Jacobian peak.
(Sternheimer, 1955)







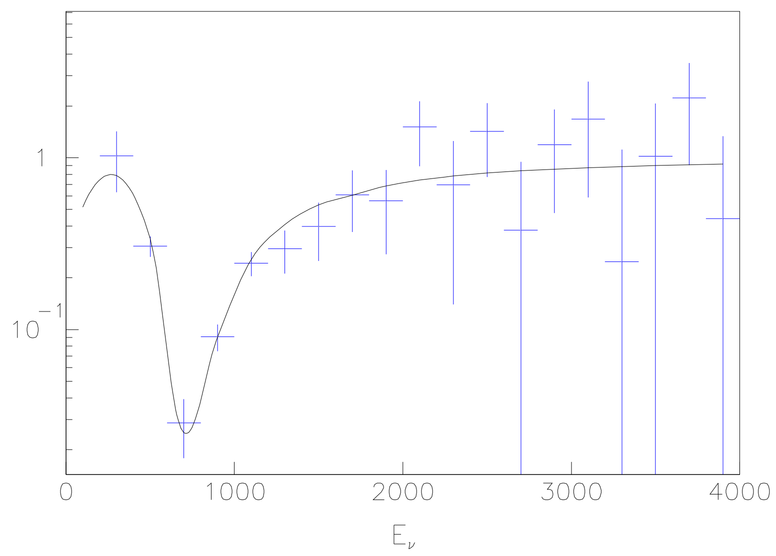




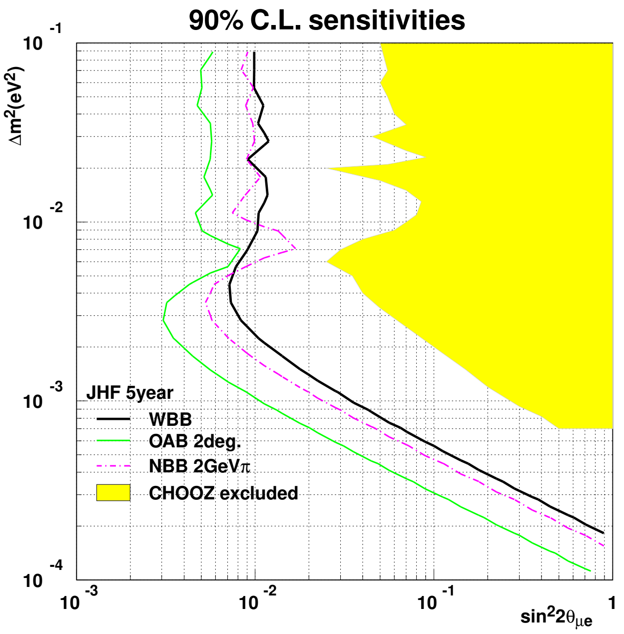
Superbeam Strategy, III

Choose detector distance L to match first maximum of ν_2-ν_3 oscillations: $L/E \approx 400$ km/GeV.

$\Rightarrow$ ν_μ disappearance is dramatic.



$\Rightarrow$ Sensitivity to $\sin^2\theta_{\mu e} \approx \sin^2\theta_{13}$ down to a 10^{-3} with 4 MW beam and 100 kton fiducial volume detector.



Can Study CP Violation at $L/E = (2n+1)400$ km/GeV

[Marciano, hep-ph/0108181]

The nth maximum of ν_2-ν_3 oscillations occurs at $L/E \approx (2n+1)400\ \mathrm{km/GeV}$.

The CP asymmetry grows with distance:

$$A = \frac{P(\nu_\mu \to \nu_e) - P(\bar{\nu}_\mu \to \bar{\nu}_e)}{P(\nu_\mu \to \nu_e) + P(\bar{\nu}_\mu \to \bar{\nu}_e)} \approx \frac{2 s_{13} c_{12} c_{23} \sin\delta}{s_{23} s_{13}} \left(\frac{\Delta m^2_{12}}{\Delta m^2_{23}}\right) \frac{\Delta m^2_{23} L}{4 E_\nu}$$

$$\Rightarrow \frac{\delta A}{A} \approx \frac{1}{A\sqrt{N}} \propto \frac{1}{L\sqrt{N}} \approx \text{ independent of } L.$$

Of course, since $N_{\mathrm{events}} \propto 1/L^2$, hard to make other measurements at large L.

But since need to disentangle matter effects from CP asymmetries, this suggests use of 2 detectors at oscillation maxima $n = 0$ and $n = 1$ or 2, $\Rightarrow R = L'/L = 3$ or 5.

Note also that small $s_{13} = \sin\theta_{13} \Rightarrow$ large CP asymmetry, but low rates.

$\Rightarrow$ May be difficult to untangle $\sin\delta$ and s_{13}.